

Rare-earth Metal Borosilicides R9Si15-xB3 (R = Tb, Yb): New Ordered Structures Derived from the AlB2 Structure Type

Volodymyr Babizhetskyy, Volodymyr Levytskyi, Régis Jardin, Josef Bauer, Roland Guérin, Regis Gautier, Bruno Fontaine, Jean-François Halet

▶ To cite this version:

Volodymyr Babizhetskyy, Volodymyr Levytskyi, Régis Jardin, Josef Bauer, Roland Guérin, et al.. Rare-earth Metal Borosilicides R9Si15-xB3 (R = Tb, Yb): New Ordered Structures Derived from the AlB2 Structure Type. Journal of Inorganic and General Chemistry / Zeitschrift für anorganische und allgemeine Chemie, 2020, 646 (14), pp.1168-1175. 10.1002/zaac.202000046. hal-02797030

HAL Id: hal-02797030 https://univ-rennes.hal.science/hal-02797030

Submitted on 9 Jun 2020

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

Rare-earth metal borosilicides $R_9Si_{15-x}B_3$ (R = Tb, Yb): New ordered structures derived from the AIB₂ structure type

Volodymyr Babizhetskyy,*^[a] Volodymyr Levytskyy,^[a] Régis Jardin,^[b] Josef Bauer,^[b] Roland Guérin,^[b] Régis Gautier,*^[b] Bruno Fontaine,*^[b] and Jean-François Halet*^[b]

Dedicated to a long-time friend and occasional collaborator, Prof. Yuri Grin, on the occasion of his 65 Birthday.

Abstract: Two novel ternary borosilicides $R_9Si_{15-x}B_3$ (R = Tb, x =1.80, R = Yb, x = 1.17) have been synthesized from the initial elements using tin flux method. Their crystal structures were determined by means of X-ray single crystal diffraction. Both refer to space group R32, Z = 1: a = 6.668(2) Å, c = 12.405(4) Å ($R_1 = 0.027$, $wR_2 = 0.031$ for 1832 reflections with $I_0 > 2\sigma (I_0)$) for Tb₉Si_{15-x}B₃, and a = 6.5796(3) Å, c = 12.2599(5) Å ($R_F = 0.052$, wR = 0.090 for 1369 reflections with $I_0 > 2\sigma(I_0)$) for Yb₉Si_{15-x}B₃. The structures represent a new structure type, derived from the AIB2, with ordering in the metalloid sublattice resulting in distorted [Si₅B] hexagons. The presence or absence of boron in this ordered structure is discussed on the basis of difference Fourier syntheses, interatomic distances, structural analysis, and theoretical calculations in relation with the parent structures of the binaries AIB2 and Yb3Si5 (Th3Pd5 type of structure). Theoretical calculations show substantial covalent interactions between the metal and nonmetal elements. The small percentage of silicon atoms, which are missing in these nonstoichiometric compounds, probably allows strengthening boronmetal and boron-silicon bonding.

Introduction

Ternary rare-earth metal boride silicide compounds are not numerous although their synthesis and investigation of their properties may constitute an interesting field for thermoelectricity application for instance. Indeed, a handful of boron-rich boride silicide compounds such as $GdB_{18}Si_5$ have been reported generally obtained by addition of small amounts of silicon to higher borides. A few more have been synthesized with high silicon content. Defended, full investigations on phase relations in the R-Si-B systems (R = rare-earth metal) are scarce. Ternary phase diagrams R-Si-B were reported a while ago for R = La, Ce, Er, and Y at 1070 K by Kuz'ma and colls.

- [a] Dr. V. Babizhetskyy,* Dr. V. Levytskyy Department of Inorganic Chemistry Ivan Franko National University of Lviv Kyryla & Mefodiya Str. 6, UA-79005 Lviv, Ukraine E-mail: v.babizhetskyy@googlemail.com
- [b] Dr. R. Jardin, Dr. J. Bauer, [†] Prof. Dr. R. Guérin, Prof. Dr. R. Gautier, Dr. B. Fontaine, Prof. Dr. J.-F. Halet Univ Rennes, Ecole Nationale Supérieure de Chimie de Rennes, CNRS, Institut des Sciences Chimiques de Rennes-UMR 6226 F-35000 Rennes, France E-Mail: regis gautier@enc-rennes.fr, bruno.fontaine@ensc-rennes.fr, halet@univ-rennes1.fr
 [†] Deceased 9 Aug 2016

Supporting information for this article is available on the WWW under... or from the authors.

However, no evidence was given concerning the existence of ternary phases, with the exception of narrow homogeneity ranges around some binary compositions. More recently, some of us have reported the isothermal sections of some ternary systems $R-{\rm Si-B}$ (R=Y, Nd, Gd, Dy, Ho, Er) at the temperature of 1270 K. $^{[2-4]}$ In general, three ternary phases were found in each system, except for Nd: The stoichiometric compound $R_5{\rm Si}_2{\rm B}_8$ (Gd $_5{\rm Si}_2{\rm B}_8$ structure type), $^{[5,6]}$ the boron-inserted Nowotny phase $R_5{\rm Si}_3{\rm B}_x$ (Mn $_5{\rm Si}_3$ -type structure), $^{[7]}$ and the solid solution $R{\rm B}_{2-x}{\rm Si}_x$ (AlB $_2$ -type structure). $^{[8]}$ For the Nd–Si–B system, only Nd $_5{\rm Si}_3{\rm B}_x$ was found. $^{[3]}$

Over the last two decades, it has been demonstrated that metal flux is a powerful technique for the synthesis of binary or ternary compounds.[12] It provides substantial advantages for exploration of novel solid-state compounds, some of which could never be formed by conventional solid-state synthetic techniques. Indeed, numerous phases have been obtained as single crystals after removing the metallic flux matrix with moderately diluted hydrochloric acid or by electrochemical dissolving of resulted molten ingots. Using flux techniques we were ourselves able to synthesize a new series of binary silicides of formula $RSi_{1.7}$ (R = Dy, Ho), [13] which show ordered structures derived from the AIB₂ structure type. [14] Tin as metal flux was used to obtain one of the first ternary boride silicide of the silicon-rich part of the Er-Si-B phase diagram, namely $R_8 Si_{17} B_3$ (R = Ho, Er). [8] The insertion of boron atoms within the silicon slabs in these structures generates ordered commensurate arrangements in the c direction, which are derived from the AIB₂ structure type.

Using the same synthesis route, new ternary borosilicides of formula $R_9 \mathrm{Si}_{15 \text{-} x} B_3$ have been synthesized with R = Tb, Yb (see the Experimental section). Their crystal structures were solved from single-crystal X-ray diffraction data. Results indicate that they adopt a new structure type, which is derived from the AlB $_2$ structure arrangement. Main results are reported here. The presence or absence of inserted boron in this ordered phase is discussed on the basis of difference Fourier syntheses, interatomic distances, structural analysis, and theoretical calculations in relation to the parent structures of the binaries AlB $_2$ and Yb $_3\mathrm{Si}_5$ (Th $_3\mathrm{Pd}_5$ type of structure). [15-17]

Results and Discussion

From preliminary X-ray studies on single crystals of $R_9\mathrm{Si}_{15\text{-}x}\mathrm{B}_3$ (R = Tb, Yb) hexagonal symmetry was found. The presence of some weak reflections leads to the consideration for tripling the c parameter of the basic unit cell. X-ray intensity data collected on an image plate or a CCD diffractometer confirm the existence of a unit cell, which can be derived from those of the AlB₂ and Th₃Pd₅ structure types. Tripling of the c parameter compared to

scepted Manuscrib

the unit cell of Yb_3Si_5 $(Th_3Pd_5 type)^{[13, 16]}$ was found. The collected diffraction data revealed a decrease in the unit cell parameters and volumes from Tb to Yb, thus a good agreement with the lanthanide contraction law. The Laue groups $\overline{3}$ and $\overline{3}m$ led to the possible space groups R3, R $\overline{3}$, R32, R3m, and R $\overline{3}$ m. The best solution and the structure refinements were reached using the non-centrosymmetric space group R32. Crystal structure and refinement details are given in Table 1.

Table 1. Crystal data and structure refinement details for Tb₉Si_{15-x}B₃ and YboSi15-xB3.

Composition Crystal system Space group Pearson symbol Formula per unit cell, Z Lattice parameters	Tb ₉ Si _{15.x} B ₃ ($x = 1.80$) trigonal R32 (No 155) hR27	Yb ₉ Si _{15-x} B ₃ (x = 1.17) trigonal R32 (No 155) hR27
a/Å c/Å	6.668(1)	6.5896(3)
Unit cell volume / Å ³	12.404(4) 477.7(2)	12.2599(5) 459.64(4)
Calculated density /	6.373	7.146
(g/cm ³)		
Absorption coefficient /	39.911	45.23
(1/mm)		
Crystal size / mm ³	0.01 x 0.017 x 0.23	0.02 x 0.02 x 0.18
Radiation and	Mo <i>K</i> α, 0.71073	Mo <i>K</i> α, 0.71073
wavelength / Å Diffractometer	STOE IPDS II	Nonius Kappa CCD
Refined parameters	18	18
Refinement	F ²	F
$2\theta_{\text{max}}$ and $(sin\theta/\lambda)_{\text{max}}$	63.06, 0.736	70.0, 0.807
h, k, I	-9< h <9	-10< <i>h</i> <5
Collected reflections	-9< k <9	0< <i>k</i> <10
Independent	-18< / <15	0 <17</td
reflections	1832	1369 438
Reflections with $I_0 > 2\pi(I_0)$	$364 (R_{int} = 0.047)$ 210 ($R_{cr} = 0.030$)	230
$2\sigma(I_0)$ Final $R_1^{[a]}$ indices $(R_1^{[a]})$	$210 (N_{\sigma} - 0.000)$	200
all data)	0.027 (0.046)	0.053
Weighted wR ₂ ^[b] factor	, ,	
(wR ₂ ^[b] all data)	0.061 (0.070) ^[c]	$0.090^{[d]}$
Goodness-of-fit on F ² :	0.96	1.1
Flack parameter	0.07(15)	0.05(17)
Largest diff. peak and hole / (e/Å ⁻³)	1.41/-1.01	2.39/-2.36

 $[\]begin{array}{l} ^{[a]}R_1(F) = [\Sigma(|F_0|-|F_c|)]/\Sigma|F_0|. \\ ^{[c]}[w^1 = \sigma^2(F_o)^2 + (0.0122P)^2 + 0.000P], \text{ where } P = (F_o^2 + 2F_c^2)/3. \\ ^{[d]}R_w, \text{ where } w = 1/(\sigma^2(F_o)^2 + (0.0056F_o^2). \end{array}$

The atomic coordinates and isotropic displacement parameters are listed in Table 2 whereas the anisotropic displacement parameters are given in Table 3. In the crystal structure of these compounds, the rare-earth metal atoms occupy the special 9d Wyckoff positions. For the ordered metalloid sublattice, three positions were found: 9e (Si1) and 6c (Si2) for silicon atoms and 3b for boron atoms. In order to locate the boron atoms, difference Fourier maps have been established and a residual electronic density peak in the 3b site of the trigonal unit cell was revealed. The attribution of this peak to boron led to the decreasing of the weighted reliability factor R_w from 0.070 to 0.061. The final difference Fourier analyses gave no indications for additional atomic sites. The isotropic displacement parameters for Si1 atoms located in the 9e site in both refinements for $Tb_9Si_{15}B_3$ and $Yb_9Si_{15}B_3$ crystal structures showed rather large values. We therefore refined the occupation factor for Si1 (SOF = 0.80(2) and SOF = 0.87(4) for Tb₉Si₁₅B₃

and Yb₉Si₁₅B₃, respectively). Final difference Fourier synthesis did not mention any significant residual electronic density peaks (Table 1). The final formula of these boride silicides deduced from the structure refinements, are $Tb_9Si_{15-x}B_3$ (x = 1.80) and $Yb_9Si_{15-x}B_3$ (x = 1.17), respectively. The corresponding ratios Tb/Si = 40.54/59.46 and Yb/Si = 39.42/60.58 agree well with the nominal composition obtained by EDS measurements: R/Si = 40.06/59.94 (see the Experimental section). Observed and calculated structure factors can be obtained from the authors on request.

Table 2. Atomic coordinates and isotropic displacement parameters (in Å²) for Tb₉Si_{15-x}B₃ and Yb₉Si_{15-x}B₃.

Atom	Site	SOF	X	У	z	$U_{\sf eq}^{\;\;[a]}$
Tb ₉ Si _{15-x} B ₃						
Tb1	9 <i>d</i>		0.6707(1)	0	0	0.0059(1)
Si1	9 e	0.80(2)	0.291(2)	0	1/2	0.018(2)
Si2	6 <i>c</i>		0	0	0.1704(5)	0.019(2)
B1	3 <i>b</i>		0	0	1/2	0.015(3)
Yb ₉ Si _{15-x} B ₃						
Yb1	9 <i>d</i>		0.6711(5)	0	0	0.0095(2)
Si1	9 <i>e</i>	0.87(4)	0.282(2)	0	1/2	0.025(3)
Si2	6 <i>c</i>		0	0	0.1700(2)	0.020(3)
B1	3 <i>b</i>		0	0	1/2	0.024(8)

^[a] U_{eq} (Å²) is defined as one third of the trace of orthogonalized U_{ii} tensor.

Table 3. Anisotropic displacement parameters for $Tb_9Si_{15-x}B_3$ and $Yb_9Si_{15-x}B_3$.

Atom	U ₁₁	U ₂₂	U ₃₃	U ₁₂	U ₁₃	U ₂₃
$Tb_9Si_{15-xB_3}$						
Tb1	0.0051(1)	0.0051(1)	0.0056(1)	0.0009(3)	-0.0001(1)	0.0001(1)
Si1	0.016(3)	0.016(3)	0.007(6)	0.0000(2)	-0.0001(7)	-0.0003(14)
Si2	0.023(3)	0.023(3)	0.010(4)	0.011(1)	0	0
B1	0.04(2)	0.04(2)	0.02(1)	0.017(12)	0	0
$Yb_9Si_{15\text{-}x}B_3$						
Yb1	0.0100(4)	0.0100(4)	0.0083(6)	0.0050(2)	-0.0013(2)	-0.00013(2)
Si1	0.034(4)	0.034(4)	0.019(2)	0.026(4)	0.0003(4)	-0.0003(4)
Si2	0.023(4)	0.023(4)	0.015(3)	0.012(2)	0	0
B1	0.04(2)	0.04(2)	0.02(1)	0.02(1)	0	0

A projection of the $Yb_9Si_{15-x}B_3$ structure onto the crystallographic ab plane and the coordination polyhedra for all atoms are shown in Figure 1. The Yb atoms are surrounded by 12 metalloid atoms, which form a hexagonal prism and 8 additional metal atoms outside the faces of the prism (Figure 1b). Their coordination number (CN) is therefore 20. The boron and silicon atoms are situated in trigonal prisms formed by ytterbium atoms, with additional metalloid atoms outside the rectangular faces of the prisms (CN = 9, Figure 1, c and d).

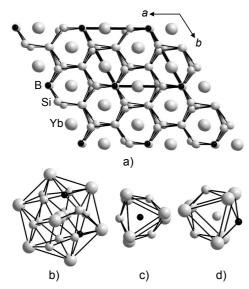


Figure 1. Projection of the $Yb_9Si_{1,5-x}B_3$ crystal structure onto the crystallographic ab plane (a) and coordination polyhedra of the Yb (b), B (c), and Si (d) atoms.

The structure of Yb₉Si_{15-x}B₃ can be considered as a ternary derivative of the AIB2 and Th3Pd5 types of structures over a mechanism of ordering in the metalloid sublattice. The tripling of the c parameter presents a relationship to the Yb₃Si₅ (Th₃Pd₅ type) arrangement)^[7] with $a \approx a'$ and $c \approx 3c'$ with respect to the cell parameters of Yb₃Si₅ (a' = 6.504, c' = 4.092 Å). [16] Owing to the vacancies, the silicon slab in the Yb₅Si₃ structure consists of twelve-membered rings, which share common edges and extend infinitely in the ac plane. Such rings are observed also in the RSi_{1.7} structures but they only extend along the [001] direction. [13] Vacant sites in the structure of Yb₃Si₅ are occupied with boron atoms in the structure of Yb₉Si_{15-x}B₃. Consequently, the presence or absence of inserted boron atoms in the new structure was the subject of a careful examination of the difference Fourier syntheses, interatomic distances and structural analysis. Insertion of boron atoms into the vacancies of the silicon slab induces a weak deformation of the [Si₅B] hexagons and some weak corrugation of the metalloid network. Figure 2 displays three layers formed by [Si₅B] hexagons of the structure Yb₉Si_{15-x}B₃ along [001]. Ideal z coordinates of silicon and boron atoms are shown on the left hand-side of Figure 2b for a fully planar metalloid network. The slight deviation from planarity observed in the real structure is shown on the righthand side of Figure 2b. Each B1 atom is bonded to three silicon atoms Si1 with distances of $d_{\text{B1-Si1}}$ = 1.93(1) and 1.850(11) Å in Tb₉Si_{15-x}B₃ and Yb₉Si_{15-x}B₃, respectively. These distances are rather short, ca. 3% and 8% shorter, respectively, than those measured in β -SiB₃, [18, 19] SiB₋₃₀, [20] MgB₁₂Si₂, [21] or Li₂B₁₂Si₂ [22] for instance. Indeed, DFT optimization gives slightly longer Si-B bond distances, closer to those experimentally measured in the latter compounds (*vide supra*). With $d_{Si1-Si2} = 2.378(9)$ in Tb₉Si₁₅₋ _xB₃ and 2.384(12) Å in Yb₉Si_{15-x}B₃, Si-Si distances are close to the sum of the covalent radius of silicon (r_{Si} = 1.17 Å). Tb-Tb distances of 3.803(1) and 4.135(1) Å and Yb-Yb distances of 3.748(1) and 3.824(1) Å are measured. R-Si and R-B distances

are close to the average distances generally encountered in corresponding binary rare-earth metal borides and silicides. The alternate stacking of the [Si_5B] hexagons above and below the R layer leads to many different R–Si and R–B distances (Table 4).

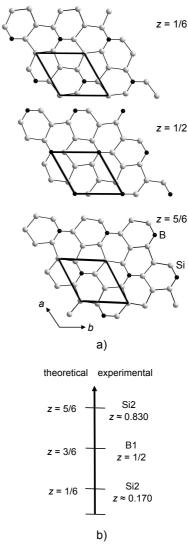


Figure 2. Projection of the three different layers of the $Yb_9Si_{15-x}B_3$ structure (a) and the sequence of the boron and silicon atoms in the different layer (b) along [001].

Table 4. Selected interatomic distances (*d*, Å) for Tb₉Si_{15-x}B₃ and Yb₉Si_{15-x}B₃.

Atom	d	Atom	d	Atom	d
$Tb_9Si_{15-xB_3}$					
Tb1-2Si1 2Si1 2Si1 2Si2 2Si2 2Si2 2B1	2.936(4) 2.962(4) 3.239(1) 3.015(4) 3.048(5) 3.045(1)	Si1-2Tb1 2Tb1 2Tb1 2Si2 2B1	2.936(4) 3.237(1) 2.962(4) 2.378(9) 1.93(1)	Si2–3Tb1 3Tb1 3Si1 B1–6Yb1 3Si1	3.015(4) 3.048(5) 2.378(9) 3.045(1) 1.93(1)
$Yb_9Si_{15-x}B_3$					
Yb1-2Si1 2Si1 2Si1 2Si2 2Si2	2.882(12) 2.911(5) 3.25(1) 3.004(2) 2.981(2)	Si1-2Yb1 2Yb1 2Yb1 2Si2 2B1	2.882(12) 3.2446(7) 2.911(12) 2.384(2) 1.850(11)	Si2–3Yb1 3Yb1 3Si1 B1–6Yb1	3.004(12) 2.981(17) 2.384(12) 3.047(1)

ARTICLE WILEY-VCH

2B1 3.047(1) 3Si1 1.850(11)

The structural relationship between the crystal structures of the hettotype YbSi_{15-x}B₃ and the aristotype AlB₂ can be derived from a Bärnighausen tree. [23, 24] The corresponding group-subgroup scheme is shown in Figure 3. The symmetry reductions from AIB2 to YbSi15-xB3 structure may be subdivided into three steps. A translationsgleiche transition of index 2 leads to the simplest ternary SrPtSb structure of space group $P\overline{6}m2$, an ordered variant of the AlB₂ structure type. [25] Here (Figure 3), each planar hexagon is built up from three platinum and three antimony atoms in an ordered manner. The following translationsgleiche step lowers the symmetry to the trigonal space group P312 (Nr. 149). The last and most important step is again a klassengleiche transition of order 3, corresponding to the transformation a-b, a+2b, 3c. Lowering the symmetry to the trigonal system R32 (Nr. 155) leads to a splitting of the 1f site into a six-fold 6c site (0, 0, 0.17) and a threefold 3b site (0, 0, 1/2) occupied by silicon and boron atoms, respectively. The different nature of the non-metal atoms forming the hexagons in the structure leads to the puckering of the initial planar metalloid net. From another hand, the simple filling by boron atoms of the vacancies in the silicon slab of the Yb_3Si_5 structure, $^{[16]}$ cannot be simply reduced from the group-subgroup relation over the Th₃Pd₅ structure.

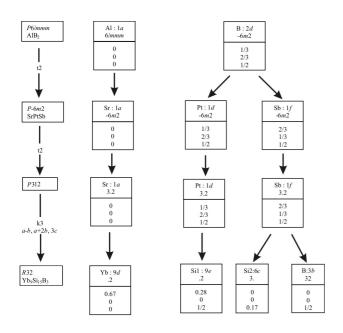


Figure 3. Group-subgroup scheme in the Bärnighausen formalism for the structures AlB_2 , SrPtSb, and $R_9Si_{15.x}B_3$. The indices for the *translationsgleiche* (t) symmetry reductions, the unit cell transformations, and the evolution of the atomic parameters are given.

Assuming in a first approximation full occupation of Si1 in 9e position and a simple Zintl–Klemm ionic bonding scheme^[25] between the metal and the non-metal atoms, anionic

silicon atoms and dianionic boron atoms can be considered resulting in the ionic formulation $[R_9]^{21+}[Si^*]_{15}[B^2^*]_3$. If we assume such a charge distribution, some electrons must remain available for metal–metal bonding in the compounds $R_9Si_{15-x}B_3$. Indeed, negative charges attributed to the three-connected sp^2 Si and B atoms come from the fact that only single Si-Si or Si-B bonds are observed in the Si/B network. Therefore, it is assumed that they obey the octet rule although they violate the hybridization rule.

Periodic density functional theory (DFT) calculations were carried out in order to gain insight on their structural and electronic properties (see the Experimental section for computational details). Full occupation of Si1 in 9e position (see above) was considered to reduce the computational effort, i.e., computations were performed on $R_9 Si_{15}B_3$ model structures and on the related binary compound $Yb_3 Si_5^{[16]}$ for comparison.

Optimized unit cell parameters and interatomic distances are given and compared to the experimental ones in Table 5. The computed values quite satisfactorily mimic those of the crystallographically characterized compounds. Especially, the M-M bond lengths are well reproduced and are consistent with the lanthanide contraction law experimentally ascertained. Overall, as often computed for crystal structures relaxed using LDA or GGA functionals, a slight overestimation of all metrical parameters (ca. 1 %) is noted.

Table 5. Selected optimized interatomic distances and cell parameters (Å) for Yb_3Si_5 and " $R_9Si_{15}B_3$ " (R = Yb, Tb) compounds. Experimental values are given in brackets.

	Yb ₃ Si ₅	"Yb ₉ Si ₁₅ B ₃ "	"Tb ₉ Si ₁₅ B ₃ "
а	6.5348 (6.5049)	6.5909 (6.5896)	6.6961 (6.6681)
С	4.1295 (<i>4.0923</i>)	12.2946 (<i>12.2599</i>)	12.5009 (12.4040)
R-R	3.704 (<i>3.632</i>)	3.824 (<i>3.748</i>) 3.857 (<i>3.825</i>)	3.861 (<i>3.809</i>) 3.869 (<i>3.871</i>)
R-Si1	3.007 (<i>3.006</i>) 3.180 (<i>3.261</i>)	2.939 (2.882) 2.938 (2.911) 3.213 (3.250)	2.984 (<i>2.936</i>) 2.988 (<i>2.962</i>) 3.204 (<i>3.239</i>)
R-Si2	2.938 (<i>2.929</i>) 2.958 (<i>2.930</i>)	3.046 (2.981) 3.067 (3.004)	3.051 (<i>3.015</i>) 3.054 (<i>3.048</i>)
<i>R</i> –B1		3.065 (3.008)	3.055 (<i>3.045</i>)
Si1-Si1	3.094 (3.033)		
Si1-Si2	2.453 (2.404)	2.340 (2.384)	2.340 (<i>2.379</i>)
B-Si1		2.025 (1.850)	2.029 (1.930)

The total and atom-projected density of states (DOS) for Yb_3Si_5 , $Yb_9Si_{15}B_3$, and $Tb_9Si_{15}B_3$ were computed (see Figure 4 and Figure S1). Except the position of the Fermi level ε_F in the sharp peak deriving from the f orbitals, comparable results are observed for $Yb_9Si_{15}B_3$ and $Tb_9Si_{15}B_3$ (compare Figures 4b and S1). Consequently, only the results obtained for the former are commented here. A comparison of the total and atom-projected

ARTICLE WILEY-VCH

DOS of the binary phase Yb_3Si_5 and the ternary phase $Yb_9Si_{15}B_3$ (Figure 4) indicates more dispersed DOS, especially below ε_F in the energy window [-5; -2.5] eV for the former. Nevertheless, in both cases, metallic conductivity is expected with ε_F lying in a pronounced peak of DOS made from all the constituting elements, reflecting substantial metal–nonmetal covalent interaction. Interestingly, no holes in the DOS are observed close to ε_F which could favor specific electron counts and therefore specific stoichiometries. On the other hand, some homogeneity range might be possible, reflected by the refined occupancy factors of Si1, which differ in $Yb_9Si_{15-x}B_3$ and $Tb_9Si_{15-x}B_3$, (see Table 2). We will come back to this point later.

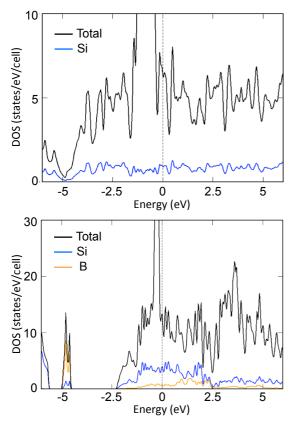


Figure 4. Total and atom-projected DOS for Yb_3Si_5 (top) and $Yb_9Si_{15}B_3$ (bottom). ε_F set at 0 eV.

Covalent character between the metal and the non-metal atoms is confirmed by the analysis of crystal orbital Hamiltonian population (COHP) curves which indicate energetic contributions of crystal orbitals between atoms. [26] Those computed for the Yb-Si1, Yb-Si2, Yb-B1, Yb-Yb, Si1-Si2, and Si1-B1 contacts in the Yb₉Si1₅B₃ structure are sketched in Figure 5. Their inspection shows that the bonding between metal and non-metal atoms is nearly maximized in this compound, except that between the atoms Si1 and B1, the COHP curve of which shows some antibonding states below $\varepsilon_{\rm F}$. This is an important result. Although the value of the corresponding integrated COHP is a rather high (ICOHP = -0.402 Ry/cell), fractional occupancy of Si1 should

shift down the Fermi level – a rigid band model is assumed – and diminish the number of occupied Si1-B1 antibonding states. This is probably why full occupancy of Si1 is not observed in $Yb_9Si_{15-x}B_3$ (x=1.17) and $Tb_9Si_{15-x}B_3$ (x=1.80). It is noteworthy that the Yb-Yb and Si1-Si2 COHP curves compare very well with the corresponding ones in the binary Yb_3Si_5 compound (Figure S2)

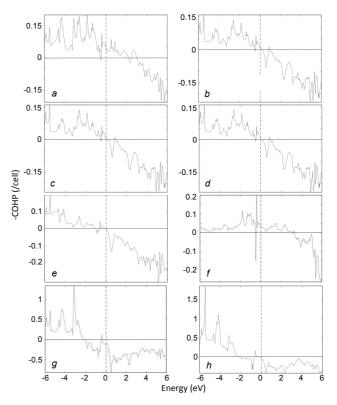


Figure 5. COHP curves for Yb-Si1 = 2.938 and 3.213 Å (a, b), Yb-Si2 = 3.046 and 3.067 Å (c, d), Yb-B1 = 3.065 Å (e), Yb-Yb = 3.824 Å (f), Si1-Si2 = 2.340 Å (g), and Si1-B1 = 2.025 Å (h) contacts in Yb₉Si₁₅B₃. ε_F set at 0 eV.

As expected, strong covalent interactions occur between the non-metals atoms. This is supported by the large ICOPH values computed for both Si1-Si2 and Si1-B1 (-0.191 and -0.402 Ry/cell, respectively). Although a strict comparison cannot be made, the value of the former is of the same order than the Si1-Si2 ICOHP value computed for the binary Yb₃Si₅ (-0.175 Ry/cell). ICOHP values for Yb-Si (-0.032 and -0.057 Ry/cell for Yb-Si1 and (-0.054 and -0.056 Ry/cell for Yb-Si2) and Yb-B1 (-0.031 Ry/cell) contacts are of the same order of magnitude and substantial metal-non-metal interactions. interactions are also supported by the atomic net charges computed for $Yb_9Si_{15}B_3$ ($[Yb^{0.56+}]_3$, $[Si1^{0.14-}]_9$, $[Si2^{0.13-}]_6$, $[B1^{1.00-}]_3$), which indicate some electron transfer from the metal to the nonmetal atoms somewhat in agreement with the Zintl-Klemm ionic formulation proposed above. Slightly weaker charge transfer is computed in the binary Yb_3Si_5 ($[Yb^{0.32+}]_3$, $[Si1^{0.15-}]_3$, $[Si2^{0.26-}]_2$).

ARTICLE WILEY-VCH

Conclusions

Two novel ternary borosilicides of formula $R_9Si_{15.x}B_3$ were prepared with R = Tb, Yb using tin flux method. Their crystal structure was solved from single-crystal X-ray diffraction data, indicating a new structure type, which can be derived from the structure of the binary silicide Yb_3Si_5 (nonstoichiometric AlB_2 type) with partial occupancy of Si atoms and filling of the vacant site. The silicon and boron atoms form a two-dimensional planar network made of Si_5B hexagons. Theoretical calculations show substantial covalent interactions between the metal and nonmetal elements. The small percentage of silicon atoms, which are missing in these nonstoichiometric compounds, probably allows strengthening boron-metal and boron-silicon bonding.

Experimental Section

Synthesis and analysis: Single crystals of the title compound were obtained using tin as a metal flux. First, suitable amounts of silicon (purity 99.999%) and boron (99.99%) as powders and rare-earth metals (99.9%) as chips, in the nominal atomic ratio R/Si/B = 3/1/2 (R = Tb, Yb), were mixed together and cold-pressed into pellets (each sample of about 1 g). A large excess of tin as granules was then added in order to obtain a tin content of about 80% in weight. Then, the mixtures were sealed in silica tubes under vacuum and annealed at 1173 K during 5 days. After quenching in air, the molten buttons were slowly dissolved in diluted hydrochloric acid. The yield of the title materials from a synthesis batch is about 60%, according X-ray powder data and only REB4 is detected as byproduct. Then, shiny grey truncated platelet-like single crystals were extracted for structure determination. Electron probe microanalyses on single crystals, using energy-dispersive spectroscopy (EDS) with the help of a scanning electron microscope (Jeol JSM-6400), confirmed terbium, ytterbium and silicon being present in nominal overall content (in at.%): R/Si = 40.1/59.9 (standard deviations estimated less than 1 at.%). Unfortunately, no boron content could be determined by disposable quantitative microanalysis.

X-ray diffraction and structure refinement: The structure determination was performed on single crystals. Platelet-like metallic luster single crystals non-reactive to air were obtained for all samples. First, single crystals were studied by conventional X-ray photographic methods (oscillating crystal and Weissenberg). Second, X-ray intensity data collection of Yb₉Si₁₅B₃ was performed from a hemisphere of 197 images in a total exposure time of 144 min on a four-circle Nonius Kappa diffractometer, equipped with a CCD area detector employing graphitemonochromatized Mo $K\alpha$ radiation ($\lambda = 0.71073$ Å). The orientation matrix and the unit cell were derived from the first 10 data frames using the program DENZO. [27] Absorption correction was applied with the help of the program NUMABS^[28] with T_{min} = 0.008 and T_{max} = 0.054. Single crystal diffraction data of Tb₉Si₁₅B₃ was collected at room temperature on a STOE IPDS II image plate diffractometer with monochromatized Mo $K\alpha$ radiation. X-ray intensity data collection of Tb₉Si₁₅B₃ was performed from a hemisphere of 180 images in a total exposure time of 360 min. Crystal structures of $Yb_9Si_{15}B_3$ and $Tb_9Si_{15}B_3$ were solved by direct methods (SIR97), and least-squares refinements and difference Fourier syntheses were run with the beta version of the JANA2000 software [30] (full matrix least-squares on F) and the program SHELX-97^[31] within the WinGX program package^[32] (full matrix least-squares on F^2) with anisotropic atomic displacement parameters for all atoms. The refinements converged well, and the light atoms could be located from

the difference Fourier maps. Crystal structure and refinement details are given in Table 1. The atomic coordinates and displacement parameters are listed in Table 2, selected interatomic distances and bond angles are summarized in Table 3. The drawings were prepared with the program DIAMOND.^[33]

Computational procedures: Geometry optimizations of Yb_3Si_5 , $Yb_9Si_{15}B_3$ and $Tb_9Si_{15}B_3$ were carried out using density functional theory (DFT) using the Perdew-Burke-Ernzerhof (PBE) functional $^{[34]}$ implemented in the CASTEP16.1 code. $^{[35]}$ The structures were fully optimized (lattice vectors and atomic positions) and the maximum gradient threshold was set to 0.05 eV/Å. All ultra-soft pseudopotentials were generated using the OTF ultrasoft pseudopotential generator included in the program. Relativistic effects were taken into account for all elements by using scalar relativistic pseudo-potentials. The cut-off energy for plane-waves was set at 500 eV. The electronic wave function was sampled with 110 k-points in the first Brillouin zone using the Monkhorst-Pack method. $^{[36]}$

Density of states (DOS) were obtained using the full-potential linearized augmented plane wave (FLAPW) approach as implemented in the WIEN2K code $^{[37]}$ in the GGA-DFT approximation with spin-orbit coupling. The PBE $^{[34]}$ functional was used for the exchange correlation energy functional. A plane wave cut-off corresponding to $R_{MT}K_{max}=7$ was used. The charge density was Fourier expanded up to $G_{max}=16$ Å $^{-1}$. Total energy convergence was achieved with a Brillouin zone (BZ) integration mesh of 500 k-points and the density of states was shifted in order that the Fermi level lies at 0 eV.

Finally, crystal orbital Hamiltonian population (COHP) and integrated COHP (ICOHP) were obtained with the scalar relativistic tightbinding linear muffin-tin orbital method (LMTO) in the atomic sphere approximation including the combined correction obtained with TB-LMTO-ASA code^[38] for the Yb₉Si₁₅B₃ compound. Exchange-correlation was treated with LDA using the von Barth-Hedin local exchangecorrelation potential. [39] Within the LMTO formalism, interatomic space is filled with interstitial spheres. The optimal positions and radii of these additional empty spheres are determined by the procedure described by von Barth et al.[40] Six nonsymmetry-related empty spheres were introduced in these calculations. The eigenvalue problem was solved using a minimal basis set obtained from the Löwdin downfolding technique removing all empty spheres functions from the calculations. The k-space integration was performed using the tetrahedron method. [41] Charge self-consistency and average properties were obtained from 96 irreducible k-points. As recommended, a reduced basis set (in which empty sphere LMTOs were down-folded) was used the COHP calculations. COHP curves were shifted so that the Fermi level lies at 0

Supporting Information (see footnote on the first page of this article): DOS curve for $Tb_9Si_{15}B_3$ and COHP curves for Yb_3Si_5 can be found in the supporting information.

Acknowledgements

The authors thank W. Hölle (MPI FKF, Stuttgart) for X-ray intensity data collection.

Keywords: borosilicide • crystal structure • density functional calculations • electronic structure • rare-earth metal borosilicide

References

- [1] T. Mori, Higher borides. In Handbook on the Physics and Chemistry of Rare Earths (Eds: K. A. Gschneidner Jr., J.-C. Bunzli and V. Pecharsky), North-Holland, Amsterdam 2008. Vol. 38. P. 105–173.
- [2] J. Roger, V. Babizhetskyy, T. Guizouarn, K. Hiebl, J.-F. Halet, R. Guérin, The ternary RE-Si-B systems (RE = Dy, Ho, Er and Y) at 1270 K: Solid state equilibria and magnetic properties of the solid solution REB_{2-x}Si_x (RE = Dy and Ho). J. Alloys Compd. 2006. 417, 72–84.
- [3] J. Roger, V. Babizhetskyy, K. Hiebl, J.-F. Halet, R. Guérin, Solid state phase equilibria in the ternary Nd-Si-B system at 1270 K. J. Alloys Compd. 2006, 415, 73–84.
- [4] V. Babizhetskyy, J. Roger, J. Bauer, S. Députier, R. Jardin, R. Guérin, Solid State Phase Equilibria in the Gd-Si-B System at 1270 K. J. Solid State Chem. 2004, 177, 415–424.
- [5] V. Babizhetskyy, J. Roger, S. Deputier, R. Guérin, R. Jardin, J. Bauer, K. Hiebl, C. Jardin, J.-Y. Saillard, J.-F. Halet, Synthesis, crystal structure, physical properties and chemical bonding of Gd₅Si₂B₈: An unprecedented example of a ternary rare earth metal silicide boride compound. Angew. Chem. Int. Ed. 2004, 43, 1979–1983.
- [6] J. Roger, V. Babizhetskyy, S. Cordier, J. Bauer, K. Hiebl, L. Le Pollès, S. E. Ashbrook, J.-F. Halet, R. Guérin, Crystal structures, physical properties and NMR experiments on the ternary rare-earth metal silicide boride compounds RE₅Si₋₂B₈ (RE Y, Sm, Gd, Tb, Dy, Ho). J. Solid State Chem. 2005, 178, 1851–1863.
- [7] J. Roger, M. Ben Yahia, V. Babizhetskyy, J. Bauer, S. Cordier, R. Guérin, K. Hiebl, X. Rocquefelte, J.-Y. Saillard, J.-F. Halet, Mn₅Si₃-type host-interstitial boron rare-earth metal silicide compounds RE₅Si₃: Crystal structures, physical properties and theoretical considerations. J. Solid State Chem. 2006, 179, 2310–2328.
- [8] R. Jardin, V. Babizhetskyy, R. Guérin, J. Bauer, Crystal structure of the rare earth borosilicide Er₈Si₁₇B₃. J. Alloys Compd. 2003, 353, 233-239.
- [9] Yu. B. Kuz'ma, N. F. Chaban, Binary and Ternary Systems Containing Boron, Metallurgiya, Moscow, 1990 (in Russian).
- [10] N. F. Chaban, Yu. B. Kuz'ma, Phase equilibria in Er-Si-B. *Inorg. Mater.* 2000, 36, 1057–1058.
- [11] N. F. Chaban, Yu. B. Kuz'ma, X-ray investigation of ternary system {Y, La, Ce}-{AI, Si}-B. Dopov. AN. URSR. 1971, 11, 1048–1050 (in Ukrainian).
- [12] M. G. Kanatzidis, R. Pöttgen, W. Jeitschko, The metal flux: a preparative tool for the exploration of intermetallic compounds. *Angew. Chem.*, Int. Ed. 2005, 44, 6996–7023.
- [13] J. Roger, V. Babizhetskyy, R. Jardin, R. Guérin, C. Moinet, U. Burkhardt, J.-F. Halet, Tin flux synthesis of rare-earth metal silicide compounds RESi_{1.7} (RE Dy, Ho): A novel ordered structure derived from the AlB₂ type. Z. Kristallogr. 2006, 221, 502–510.
- [14] W. Hofmann, W. Jäniche, Der Strukturtyp von Aluminiumborid (AlB₂). Naturwissenshaften, 1935, 50, 851.
- [15] J. R. Thomson, The crystal structure of Th₃Pd₅ and Th₃Pt₅. Acta Crystallogr. 1963, 16, 320–321.
- [16] R. Pöttgen, R.-D. Hoffmann, D. Kussmann, The binary silicides Eu_5Si_3 and Yb_3Si_5 synthesis, crystal structure, and chemical bonding. *Z. Anorg. Allgem. Chem.* **1998**, *624*, 945–951.
- [17] A. Grytsiv, D. Kaczorowski, A. Leithe-Jasper, V. H. Tran, A. Pikul, P. Rogl, M. Potel, H. Noël, M. Bohn, T. Velikanova, On the System Silicon'Ytterbium: Constitution, Crystal Chemistry, and Physical Properties. J. Solid State Chem. 2002, 163, 178–185.
- [18] J. R. Salvador, D. Bilc, S. D. Mahanti, M. G. Kanatzidis, Stabilization of β-SiB₃ from Liquid Ga: A Boron-Rich Binary Semiconductor Resistant to High-Temperature Air Oxidation. *Angew. Chem., Int. Ed.* 2003, 42, 1929–1932.
- [19] D. Eklöf, A. Fischer, A. Ektarawong, A. Jaworski, A. J. Pell, J. Grins, S. I. Simak, B. Alling, Y. Wu, M. Widom, W. Scherer, U. Häussermann.

- Mysterious SiB₃: Identifying the Relation between α- and β-SiB₃. ACS Omega **2019**, 4, 18741–18759.
- [20] J. Roger, V. Babizhetskyy, J.-F. Halet, R. Guérin, Boron-silicon solid solution: synthesis and crystal structure of a carbon-doped boron-rich SiB_n (n-30) compound. *J. Solid State Chem.* 2004, 177, 4167–4174.
- [21] T. Ludwig, H. Hillebrecht, Synthesis and crystal structure of MgB₁₂Si₂— The first ternary compound in the system B/Mg/Si. J. Solid State Chem. 2006, 179, 1623–1629.
- [22] N. Vojteer, M. Schroeder, C. Röhr, H. Hillebrecht, Li₂B₁₂Si₂: The First Ternary Compound in the System Li/B/Si: Synthesis, Crystal Structure, Hardness, Spectroscopic Investigations, and Electronic Structure. Chem. - Eur. J. 2008, 14, 7331–7342.
- [23] H. Bärnighausen, Group-subgroup relations between space groups: a useful tool in crystal chemistry. Commun. Math. Chem. 1980, 9, 139– 175.
- [24] R.-D. Hoffmann, R. Pöttgen R., AlB₂-related intermetallic compounds a comprehensive view based on group-subgroup relations. Z. Kristallogr. 2001, 216, 127–145.
- [25] G. Wenski, A. Mewis, Trigonal-planar koordiniertes Platin: Darstellung und Struktur von SrPtAs (Sb), BaPtP (As, Sb), SrPt_xP_{2-x}, SrP_xtAs_{0.9} und BaPt_xAs_{0.8}. Z. Anorg. Allg. Chem. 1986, 535, 100–122.
- [26] (a) E. Zintl, Intermetallische Verbindungen. Angew. Chem. 1939, 52, 1;
 (b) W. Klemm, Metalloids and their compounds with the alkali metals. Proc. Chem. Soc. (London) 1958, 329–364.
- [27] R. Dronskowski, P. E. Blöchl, Crystal Orbital Hamilton Populations (COHP): Energy-resolved Visualization of Chemical Bonding in Solids Based on Density-Functional Calculations. J. Phys. Chem. 1993, 97, 8617–8624.
- [28] Nonius Kappa CCD Program Package COLLECT, DENZO, SCALEPACK, Nonius BV, Delft, The Netherlands, 1998.
- [29] P. Coppens, in Crystallographic Computing, (Eds.: F.R. Ahmed, S.R. Hall, C.P. Huber) Munksgaard, Copenhagen, 1970, pp. 250–270.
- [30] A. Altomare, M. C. Burla, M. Camalli, B. Carrozzini, G. L. Cascarano, C. Giacovazzo, A. Guagliardi, A. G. G. Moliterni, G. Polidori, R. Rizzi, SIR97: A new tool for crystal structure determination and refinement. *J. Appl. Crystallogr.* 1999, 32, 115–119.
- [31] V. Petricek, M. Dusek, JANA2000, Program for Crystal Structure Refinement, Institute of Physics, Academy of Sciences of the Czech Republic, Praha.
- [32] G. M. Sheldrick, SHELXL-97. Program for the Refinement of Crystal Structures. University of Göttingen. Germany 1997.
- [33] L. J. Farrugia, WinGX (Version 1.64.05), J. Appl. Crystallogr. 1999, 32, 837–838
- [28] K. Brandenburg, *Diamond* (version 2.1c), Crystal and Molecular Structure Visualization, Crystal Impact - H. Putz & K. Brandenburg GbR, Bonn (Germany) 1999.
- [34] J. P. Perdew, K. Burke, M. Ernzerhof, Generalized Gradient Approximation Made Simple. Phys. Rev. Lett., 1996, 77, 3865–3868.
- [35] S. J. Clark, M. D. Segall, C. J. Pickard, P. J. Hasnip, M. J. Probert, K. Refson, M. C. Payne, First principles methods using CASTEP. Z. Kristallogr. 2009, 220, 567–570.
- [36] H. J. Monkhorst, J. D. Pack, Special Points for Brillouin-Zone Integrations. Phys. Rev. B 1976, 13, 5188-5192.
- a) K. Schwarz, P. Blaha, G. K. H. Madsen, Electronic structure calculations of solids using the WIEN2k package for material sciences. *Comp. Phys. Comm.* 2002, 147, 71–76. b) P. Blaha, K. Schwarz, G. K. H. Madsen, D. Kvasnicka, J. Luitz, WIEN2K, An Augmented Plane Wave + Local Orbitals Program for Calculating Crystal Properties. Tech. Univ. Wien, Austria, 2001.
- (a) O. K. Andersen, Linear methods in band theory. Phys. Rev. B 1975, 12, 3060–3083. (b) O. K. Andersen, New methods for the one electron problem. Europhys. News 1981, 12, 4–8. (c) O. K. Andersen, O. Jepsen, Explicit, First-Principles Tight-Binding Theory. Phys. Rev. Lett. 1984, 53, 2571–2574. (d) O. K. Andersen, O. Jepsen, M. Sob,

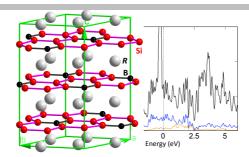
- Electronic Band Structure and its Applications (Ed.: M. Yussouff) Springer, Berlin, Germany, 1987; pp 1–57.
- [39] H. L. Skriver, The LMTO Method; Springer, Berlin, Germany, 1984.
- [40] U. von Barth, L. Hedin, A local exchange-correlation potential for the spin polarized case. J. Phys. C: Solid State Phys. 1972, 5, 1629–1642.
- [41] O. Jepsen, O. K. Andersen, Calculated electronic structure of the sandwich d¹ metals Lal₂ and Cel₂: Application of new LMTO techniques. Z. Phys. B: Condens. Matter 1995, 97, 35–47.

Entry for the Table of Contents (Please choose one layout)

Layout 1: V. Babizhetskyy et al., Rare-earth metal borosilicides $R_9Si_{15-x}B_3$ (R = Tb, Yb)

FULL PAPER

Two novel ternary borosilicides $R_9 Si_{15-x} B_3$ (R = Tb, Yb) have been synthesized from the initial elements using tin flux method.



Volodymyr Babizhetskyy,* Volodymyr Levytskyy, Régis Jardin, Josef Bauer, Roland Guérin, Régis Gautier,* Bruno Fontaine,* and Jean-François Halet*

Page No. – Page No.

Rare-earth metal borosilicides $R_9 Si_{15-x}B_3$ (R = Tb, Yb): New ordered structures derived from the AlB₂ structure type

Additional Author information for the electronic version of the article.

Author:Volodymyr Babizhetskyy
Author: Volodymyr Levytskyy
Author: Régis Gautier
Author: Jean-François Halet
ORCI
ORCI

ORCID identifier: 0000-0002-0267-0206 ORCID identifier: 0000-0003-0874-8833 ORCID identifier: 0000-0002-8104-4982 ORCID identifier: 0000-0002-2315-4200