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EXPOSURE ASSESSMENT IN MILLIMETER-WAVE REVERBERATION CHAMBER USING MURINE PHANTOMS

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ABSTRACT

This study deals with design and calibration of the first mode-stirred reverberation chamber (RC) in the 60-GHz-band adapted for in vivo bioelectromagnetic studies. In addition to the interface for electromagnetic and thermal dosimetry, the interfaces for lighting and ventilation were integrated into the RC walls while preserving acceptable shielding. The RC with mechanical and electronic steering capabilities is characterized in the 55-65 GHz range. To this end, murine skin-equivalent phantoms of realistic shape were designed and fabricated. Their complex permittivity is within ±12% of the target value of murine skin (6.19 - j5.81 at 60 GHz). The quality factor of the RC loaded with an animal cage, bedding litter, and five murine phantoms was found to be $1.2 \times 10^4$. The losses inside the RC were analyzed, and it was demonstrated that the main sources of the power dissipation were the phantoms and mice cage. The input power required to reach the average incident power density of 1 mW/cm$^2$ and 5 mW/cm$^2$ were found to be 0.23 W and 1.14 W, respectively. Surface heating of the mice models was measured in the IR range using a specifically designed interface, transparent at IR and opaque at millimeter waves (mmW). Experimental results were compared to an analytical solution of heat transfer equation (HTE) and to full-wave computations. Analytical and numerical results were in very good agreement with measurements (the relative deviation after 90 min of exposure was within 4.2%). Finally, a parametric study was performed to assess the impact of the thermophysical parameters on the resulting heating.

**Keywords**: millimeter waves; in vivo; infrared imaging; dosimetry; tissue-equivalent models.
INTRODUCTION

The number of millimeter-wave (mmW) applications is continuously increasing. In particular, substantial research activities have been focused on development of mmW technologies for wireless high data rate communications in emerging 5G networks, e.g., [MiWaves; MiWEBA; mmMAGIC]. Their near-future deployment raises concerns related to potential health risks [Guraliuc et al., 2017; Wu et al., 2015]. Besides, the Wi-Fi Alliance group created the 802.11ad standard, known as WiGig, for multi-gigabit wireless communications operating in the 60 GHz band [Wi-Fi Alliance, 2016]. Advances in mmW technologies have also triggered research focused on other potential applications including security [Cotton et al., 2009], medical [Rojavin and Ziskin, 1998; Smulders, 2013; Zhadobov et al., 2015], and military applications.

The ICNIRP guidelines and IEEE standard C95.1 provide recommendations on exposure to electromagnetic waves from 0 Hz to 300 GHz [ICNIRP, 1998; IEEE Std, 2005]. ICNIRP recommends to limit exposure of the general public in the 60 GHz band to 1 mW/cm\(^2\) under far-field conditions (averaged over 20 cm\(^2\)), but allows for power density levels up to 20 mW/cm\(^2\) for local exposures (averaged over 1 cm\(^2\)). A safety margin is applied to the general public compared to the occupational exposure; for the latter the limit is 5 mW/cm\(^2\) under far-field exposure (averaged over 20 cm\(^2\)) and 100 mW/cm\(^2\) under local exposure (average over 1 cm\(^2\)). A new release of ICNIRP guidelines is expected to be published in the near future. The IEEE Standard C95.1a recommends to limit the incident power density for general public to 1 mW/cm\(^2\) (averaged over 100 cm\(^2\)) and 20 mW/cm\(^2\) (averaged over 1 cm\(^2\)) for far-field and local exposures, respectively. The occupational exposure limit is 10 mW/cm\(^2\) (averaged over 100 cm\(^2\)) and 100 mW/cm\(^2\)
(averaged over 1 cm²) for far-field and local exposures, respectively. Note that this standard was recently updated and the new release was issued in October 2019 [IEEE Std, 2019].

An overview of exposure systems that have been used to study biological impacts of mmW is provided in Zhadobov et al. [2011]. For in vitro exposure at mmW mainly compact anechoic chambers have been used. However, they are of limited interest for in vivo exposure as to accurately control the exposure conditions animals should be kept in a fixed position, which may stress them and reduce the maximum exposure duration. To overcome the limitations of anechoic chamber based exposure systems, mode-stirred reverberation chamber (RC) has been proposed for animal exposure ensuring isotropic exposure regardless the animal posture and location inside the RC. Most of RC-related research applied to bioelectromagnetics has been conducted at frequencies up to 6 GHz [Jung et al., 2007; Jin et al. 2013, Gong et al. 2017; Wu et al., 2010; Aït-Aïssa et al., 2013; Gong et al., 2016; Chakarothai et al, 2014; Shi et al, 2014; Shi et al, 2015].

In 2015, we proposed the first mmW RC covering the 60 GHz band [Fall et al., 2015]. This proof-of-concept prototype was designed for general purpose electromagnetic compatibility testing and was not adapted for animal exposure.

The main purpose of this study is to develop the first RC exposure system adapted for in vivo isotropic exposure of mice in the 60-GHz band. We present the design and calibration procedure of the exposure system based on RC concept. The RC is characterized in the 55-65 GHz range in the presence of murine skin-equivalent phantoms. Statistical uncertainties and variability of the power density due to positioning of the phantoms are assessed. The heating due to exposure is measured on the phantom surface using a specific interface, transparent at infrared (IR) frequencies and opaque at mmW, and an IR camera. Other interfaces for air circulation and lighting are integrated into the RC while preserving acceptable shielding.
MATERIAL AND METHODS

Exposure system design

Figure 1 represents a 3D computer-aided design (CAD) view of the proposed RC with the inner dimensions of $580 \times 592 \times 595 \text{ mm}^3$. The walls were made of 10 mm – thick aluminum. Two WR-15 open-ended waveguides were used as transmitting and receiving antennas. A metallic mode stirrer connected to a DC motor ensured the random field inside the RC by continuous rotation. It consisted of 8 aluminum blades of $100 \times 90 \times 1 \text{ mm}^3$ in different orientations and spread along a metallic cylindrical axis of diameter 10 mm attached to two sides of the RC. At one of its ends, it was fixed to the DC motor shaft outside the RC, through an interface panel. In addition, an electronic stirring was implemented by the frequency modulation, which can be used independently or together with mechanical stirring.

The exposure system is expected to be located in an air-conditioned room (temperature 20-24 °C; relative humidity 45-65%, air renewal rate 15-20 times per hour, and light intensity 130-325 lux). The RC was designed to ensure that these conditions were also preserved inside the exposure system. To this end, two low noise $25 \times 25 \text{ mm}^2$ fans with a sound level of 31 dB (the reference acoustic pressure level is fixed at 20 µPa) and air flow rate of 5 m$^3$ per hour were integrated into the walls (the air inside the RC renewed about 25 times per hour). The value of the air renewal rate after integration of shielding windows in front of the fans was 16 times per hour.

In order to achieve the targeted light intensity (130-325 lux) inside the RC, 8 windows ($100 \times 100 \text{ mm}^2$) were integrated into the upper wall. Glass diffusers with a transparency of about 70%
in the optical 350-700 nm range were used to illuminate the RC and improve the lighting uniformity. Metallic wire grid covered these windows to ensure electromagnetic shielding in the mmW range. It was made of aluminum with a wire width of 50 µm and a period of 254 µm leading to a simulated level of the power transmittance of -26 dB at 60 GHz (computed using the finite element method implemented in High Frequency Structural Simulator [HFSS]). Aluminum was deposited by sputtering technique and the grid was patterned using photolithography.

Exposure levels and heating of samples under test were monitored using an IR camera following the procedure presented in [Fall et al., 2016]. A specific interface was designed and integrated into the upper wall to ensure simultaneously a high transmittance at IR and acceptable shielding efficiency at mmW. The transmission coefficient measured in the 2.5-5 µm IR range was 82% and shielding efficiency in the 55-65 GHz range was about -10 dB. Due to integration of all interfaces the measured Q-factor of the RC was reduced by less than 10 %.

Experimental set-up

The fabricated experimental set-up is presented in Figure 2. The RC was made of an aluminum and magnesium alloy (AlMg3.5). We used a tunable Gunn diode-based voltage-controlled generator (QuinStar, Torrance, CA) operating in the 58 - 62 GHz range with an output power up to about 4 W. The generator can be operated in swept frequency mode by applying a tuning voltage. The output power level can be adjusted by applying an external DC voltage. Note that, depending on the target application, the system can be used with a different mmW generator (e.g., a source simulating 5G mmW signals). Transmit (Tx) and receiving (Rx) antennas (open-ended waveguides) were fed by WR-15 waveguides. The power in the RC was measured using an Agilent E4418B power meter (Agilent Technologies, Santa Clara, CA). Note that Rx antennas
were not located in the middle of the RC since they were also used in presence of the mouse cage during in vivo experiments. Their apertures were located in the statistically homogeneous field zone at 60 GHz, which encompasses any point at distance over a quarter wavelength of any obstacle in RC, i.e., 1.25 mm at 60 GHz. It was therefore statistically equivalent to locate Rx antenna as shown in Figure 2 or in the middle of the RC. This was checked experimentally but not reported for the sake of brevity.

A high-resolution IR camera FLIR SC5000 operating in the 2.5-5 μm spectral range (FLIR Systems, Torcy, France) was used to record the temperature on the phantom. The thermal sensitivity of the camera was 0.025 °C with a spatial resolution up to 640 × 512 pixels. The IR camera was positioned on the top of the RC, and thermal measurements were performed through a specifically designed IR interface (see section Exposure system).

Five murine-equivalent phantoms of realistic shape were placed in a conventional animal cage (290×175×125 mm³) filled with 30 g of bedding litter. The cage was installed on two aluminum bars mounted in the center of the RC inner volume. Electromagnetic field in the volume of the chamber may be considered as statistically homogeneous at distances greater than a quarter wavelength of any obstacle in RC, i.e., 1.25 mm at 60 GHz. Their impact on the field distribution in the cage was negligible. Therefore, rather than hanging the cage, we opted for a more secured and fixed placement of the cage with animals during in vivo exposure experiments.

**Phantoms**
The effective complex permittivity of murine skin at mmW was reported by Alekseev et al. [2008]. Up to roughly 100 GHz, the complex permittivity of skin is described by the Debye model with single relaxation time:

$$\varepsilon^* = \varepsilon_{\infty} + \frac{\Delta\varepsilon}{1 + j2\pi f \tau} + \frac{\sigma_i}{j2\pi f \varepsilon_0},$$

where $f$ is the frequency, $\Delta\varepsilon = 16.10$ the magnitude of dispersion, $\tau = 6.9 \times 10^{-12}$ s the relaxation time, $\varepsilon_{\infty} = 4.12$ the optical relative permittivity, and $\sigma_i = 1.4$ S/m the ionic conductivity. At 60 GHz, this model yields $\varepsilon^* = 6.19 - j5.81$.

Experimental human skin-equivalent models reported at mmW so far are semi-solid water-based phantoms [Chahat et al., 2011; Aminzadeh et al., 2014; Leduc et al., 2017]. Their complex permittivity is mainly adjusted by concentration of the polyethylene powder. We used a similar approach to design a murine skin phantom; its ingredients are listed in Table 1.

Fabrication procedure of the murine-equivalent phantom of a realistic shape and dimensions consists in three consecutive steps. First, we used a 3D printer to create a plastic murine model. A generic CAD file of a mouse was scaled by a factor of 0.9 and used to print the plastic murine model. Second, the printed plastic model served for manufacturing a silicon mold. Third, the mold was used to fabricate a semi-solid phantom (Fig. 3) as described in [Chahat et al., 2011]. The mass of the fabricated phantom was approximatively 230g. Note that this homogeneous phantom does model the structure of the skin, and in particular the stratum corneum, which was shown to contribute to the reflection coefficient of the skin [Neufeld et al, 2018; Ziskin et al, 2018].

A coaxial probe (DAK, Speag, Zurich, Switzerland) connected to a vector network analyzer (ZVA 67, Rohde & Schwartz, Munich, Germany) was used to measure the complex permittivity of the phantom at 55-65 GHz (Fig. 4). The calibration of the probe was performed...
using open, short and dielectric load according to the DAK Professional Handbook. The phantom complex permittivity was within ±12% of the target murine skin permittivity (±0.4% for the real part and ±12% for the imaginary part). This corresponded to a variation of 2% and 8% in terms of the absorbed power and skin depth in the 55-65GHz range, respectively.

For validation of the methodology we also used as a reference an agar phantom composed of distilled water and 4% agar. The electromagnetic properties of a 4% agar phantom are well known and its fabrication is straightforward. Due to the high water concentration, the permittivity of this phantom is close to that of free water ($\varepsilon^* = 11.9 - j19.5$ at 60 GHz) [Ellison, 2007; Chahat et al., 2012].

Table 2 reports the thermophysical properties of the murine-equivalent phantom, water-equivalent phantom, and murine skin. The thermal properties of the proposed murine equivalent phantom with a polyethylene concentration of 30% were derived by extrapolation from data for 20% and 25% polyethylene phantoms [Chahat et al., 2012]. The thermal conductivity of water-equivalent phantom was investigated by Zhang et al. [2010]. Murine skin thermal conductivity and heat capacity were provided by Gong et al. [2016]. The thermal conductivity of the murine-equivalent phantom was higher compared to the one of in vivo murine skin (the difference is 22.9%). However, the specific heat capacities were almost the same; the deviation was less than 1%.

**Temperature distribution on phantoms**

It was demonstrated that the surface heating of a lossy object placed inside a RC can be predicted from the average power density and vice versa [Fall et al., 2016]. This is achieved by solving the 3D bioheat transfer equation [Foster, 1978]:
\[ \rho C \frac{\partial T}{\partial t} = \frac{\partial^2 T}{\partial x^2} + \frac{\partial^2 T}{\partial y^2} + \frac{\partial^2 T}{\partial z^2} - \frac{V_s}{k_t}(T - T_b) + \frac{q(x, y, z, t)}{k_t}, \]

(2)

where \( T \) is the temperature at the phantom surface [°C], \( T_b \) is the blood temperature, \( \rho \) its mass density [kg/m³], \( C \) its specific heat [J/kg·K], and \( k_t \) its thermal conductivity [W/m·K], \( V_s = f_b \rho_b C_b \) [W/K·m³] where \( f_b \) is the specific blood flow rate (zero for a homogeneous phantom), \( \rho_b \) and \( C_b \) are the density and specific heat of blood, respectively. The source term \( q(x, y, z, t) \) is the heat deposition induced by mmW (W/m³). Heat exchanged between the phantom and air can be described by the following boundary condition:

\[ k_t \frac{\partial T}{\partial x, y, z} = h(T - T_{ext}) \forall x, y, z \in \partial \Omega_{x,y,z} \]

(3)

where \( h \) is the phantom heat transfer coefficient [W/m²·K], incorporating radiation, evaporation and convection effects. \( T_{ext} \) is the ambient temperature [°C] and \( \partial \Omega_{x,y,z} \) defines the boundary surface of the phantom.

In an ideal overmoded cavity (as described by Hill [1998]), the dissipated power in a lossy object is expressed as a function of the average power density, penetration depth and average plane-wave power transmission coefficient.

**Power density inside RC**

Around 60 GHz, the incident power density is used as a dosimetric quantity as the penetration depth of the electromagnetic field inside high water content tissues is shallow [ICNIRP, 1998]. The average power density inside the RC \( S_c \) is related to the power received by an antenna placed inside the RC and the antenna effective area \( \lambda^2/8\pi \) as [Hill et al., 1994]:
\[ S_c = \frac{8\pi}{\lambda^2} \times P_r, \quad (4) \]

where \( \lambda \) is the free-space wavelength. The \( Q \)-factor, one of the main characteristics of a RC, is related to the power received by an antenna \( P_r \) as [Hill et al., 1994]:

\[ Q = \frac{16\pi^2 V}{\lambda^2} \times \left( \frac{P_r}{P_t} \right), \quad (5) \]

where \( V \) is the RC inner volume, \( P_r/P_t \) represents the ratio of the received power to the transmitted power (input power) over \( N \) positions of the stirrer. Brackets \( <> \) stand for averaging over the positions of the stirrer. Thus the average power density can be expressed as:

\[ S_c = \frac{\lambda \times Q \times P_t}{2\pi V}, \quad (6) \]

In an ideal RC, the electromagnetic field is the combination of various independent states obtained though mechanical and frequency stirring. As a result, in a RC, the electromagnetic field tends towards statistically uniform and isotropic. It is described by its statistical distribution and moments. Using the generalized extreme value distribution [Orjubin, 2007], we estimated the ratio of 99.99% quantile of the power density and mean power density to about 8.5 dB.

The calibration of the power density \( S_c \), estimated from equation (6), was performed through the comparison of the measured temperature dynamics on the phantom recorded by the IR camera and analytical or numerical solution of the bioheat transfer equation (2) with boundary conditions given in equation (3).
First, the calibration was performed for a water-equivalent phantom of parallelepiped shape to analytically analyze modification of the $Q$-factor and adjust the transmitted power to reach the target average power density using equation (6). This procedure allowed us to compare the experimental temperature dynamics with analytical calculation. The latter refers to a solution of the bioheat transfer equation, where the calibrated $S_c$ enters the source term $q$ of equation (2) [Fall et al., 2016]. The calculated and measured temperature dynamics were compared accounting for a possible uncertainty in analytical formulation or phantom fabrication.

Second, murine phantoms were used. This step was required to calibrate the power density and check temperature dynamics with realistic phantoms simulating the exposed animals. For such a complex geometry neither the modification of the $Q$-factor nor the solution of the bioheat transfer equation finds an analytical solution. Therefore we started by measuring the $Q$-factor of the RC loaded with murine phantoms to estimate the average power density. Then the bioheat equation was solved numerically with the finite difference time domain (FDTD) technique implemented in Computer Simulation Technology (CST, Darmstadt, Germany) thermal solver. The difference between measured and computed temperature dynamics provides the calibration factor.

RESULTS

Statistical characterization of exposure environment

This section reports the results of the statistical characterization of the electromagnetic field inside the RC. The statistical properties of the electric and magnetic fields in an ideal RC are those of a perfect diffuse field or Gaussian random field as derived by Hill [1998]. An ideal RC is the
result of an adequate combination of mode density according the frequency of operation and modal overlapping which involves some losses. The presence of additional lossy objects modifies the RC performance [Holloway et al., 2006]. Hereafter we analyze the statistical properties of the RC in presence of the lossy murine phantoms, animal cage and bedding litter. Results of statistical distributions are presented for a set of data, which is homogeneous to the square modulus of the electric-field strength. From complex scattering parameters measured with a vector network analyzer, we also retrieved data for testing Gaussian distributions of real and imaginary parts of electric-field strength and for testing Rayleigh distribution of the modulus of electric-field strength at several positions of Rx antenna. These tests confirmed the hypothesis of Gaussian and Rayleigh distribution, respectively. Moreover, they also confirmed that the electric field is statistically uniform within the RC volume. We provide the final synthesis of the statistics of the square modulus the square electric field, which follows an exponential distribution if the modulus of the electric field follows a Rayleigh distribution

A vector network analyzer (ZVA 67, Rohde & Schwartz, Munich, Germany) is used to measure the transfer function between two locations in the RC volume. The vector network analyzer is used due to its high dynamic range instead of the V-band power generator and power meter. The calibration was performed using a standard V-band waveguide calibration kit (open, short, and load). Scattering parameters are measured in the 55-65 GHz range with a frequency resolution of 10 MHz for \( N = 100 \) positions of the mechanical stirrer. The measured data are spread over separate series composed of S-parameters measured in 20 sub-bandwidths of 500 MHz and 100 positions of the mechanical stirrer. This leads to 20 series of 5000 individual measurements \( (P = 50 \text{ frequencies} \times N = 100 \text{ positions}) \).
It is well known that, in an ideal overmoded RC, the real and imaginary parts of each rectangular component of the electric field follow a Gaussian distribution [Hill, 1998]. Therefore the square modulus of each rectangular component is exponentially distributed. Some authors [Holloway et al., 2006b; Lemoine et al., 2007] showed that the stirred component of the scattering component $S_{21}$ follows the same statistics as a rectangular component of the electric field. As a result, the square modulus of the complex transfer function is exponentially distributed. This stirred transfer function of the RC channel when using two antennas becomes:

$$|H| = \frac{|S_{21}|^2 - |\langle S_{21} \rangle|^2}{(1 - |\langle S_{11} \rangle|^2) \times (1 - |\langle S_{22} \rangle|^2) \eta_e \eta_r}$$ \hspace{1cm} (7)$$

where $\eta_e$, $\eta_r$ denote the efficiency of the emitting and receiving open-ended waveguide, respectively.

Prior to the statistical test, the first-order autocorrelation function (FOAF) is calculated from $|H|$ to check the non-correlation between the stirrer positions. The resulting values of the FOAF is averaged over the $P = 50$ samples of $N=100$ stirrer positions. The results presented in Figure 5 show that the stirrer positions are uncorrelated (FOAF almost 0) [Lemoine et al., 2008].

The Anderson-Darling (AD) goodness-of-fit test (GoF) [Lemoine et al., 2007] is used here to test if the modulus transfer function $|H|$ is exponentially distributed. The statistical test consists in accepting or rejecting the hypothesis $H_0$, which claims that the experimental samples are from the assumed distribution. The AD GoF test is applied at each frequency to a sample made of measurements on $N=100$ positions of the stirrer (mode tune), $P = 50$ GoF tests are performed over a bandwidth of 500 MHz. The ratio between the number of rejected tests and the total number of tests is called the rejection rate (expressed as percentage). Figure 6 represents the rejection rate calculated for 20 series uniformly distributed in the 55-65 GHz range. The hypothesis $H_0$ of
exponential distribution is accepted according to the test since the rejection rate is rather small, i.e.
around 10% in average, slightly above the prescribed confidence interval (5%). The estimation of
the standard deviation normalized to the mean (Fig. 7) is also in agreement with the AD GoF test;
it is very close to 1 as expected for such a distribution. Thus, the exposure system behavior is
consistent with the statistical description of Hill [1998].

**Power dissipation inside RC**

The quality factor is a key parameter to evaluate the distribution of the power dissipated
inside the exposure system. Power dissipated in the walls, lossy objects and antennas are included
in the quality factor. The composite quality factor of the exposure system loaded with the
phantoms, the bedding litter and the animal plastic cage is expressed as [Hill, 1994]:

\[ Q^{-1} = Q_{\text{wall}}^{-1} + Q_{\text{phantom}}^{-1} + Q_{\text{litter}}^{-1} + Q_{\text{cage}}^{-1} \tag{8} \]

In equation (8), it is assumed that the individual loss mechanisms are independent. Besides, the \( Q \)-
factor associated to each object can be related to the steady state energy in the chamber \( U_s \) [J], the
pulsation \( \omega \) [rad/s] and the dissipated power \( P_d \) [W] in the object:

\[ Q = \omega \frac{U_s}{P_d} \tag{9} \]

In practice, the experimental composite \( Q \)-factor of the RC is estimated using [Hill, 1994]:

\[ Q = \frac{16\pi^2 V}{\lambda^3} \times \langle |H| \rangle \tag{10} \]

where \( \lambda \) is the wavelength, \( V \) the inner volume of the RC and \( |H| \) denotes the transfer function of
the RC channel.
The composite quality factors of each loss mechanism averaged over a bandwidth of 500 MHz are plotted in Figure 8. Cumulative losses due to the phantoms, animal cage and bedding litter strongly impact the RC quality factor (it is reduced by a factor close to 6). The impact of the presence of the phantoms is roughly the same as the animal cage, and is slightly higher than that of the bedding litter. From the \( Q \)-factor, the ratio of power dissipated in each medium can be evaluated. Results are summarized in Table 3.

The variability of the quality factor and the power dissipated in the phantoms were investigated with respect to the positions of the phantoms inside the animal cage. Figure 9 shows the arrangement of the phantoms in five configurations. The positions of the phantoms are set in order to depict the extreme cases. As expected, the quality factor associated with the case C gives the lowest estimate (Fig. 10). In this configuration, the masking effect between the phantoms is the smallest. The cases A and E give the upper bound of the estimated quality factor. The proximity of the phantoms leads to an important masking effect and consequently reduction of the total power dissipated in the phantoms. The difference between the upper and lower bound of the quality factor at 60 GHz is about 6.3% (in average 7.3% in the 55-65 GHz range).

Validation using water-equivalent phantom

As described above, the power density in the RC can be derived from the quality factor using equation (6). The aim of this section is to check whether the power density estimated from (6) is consistent with that derived from temperature rise measurements. The approach consists in comparing the temperature gradient measured using the IR camera on a phantom to the solution of the 3D heat equation. The exposure system is loaded with a parallelepiped 9.9×9.9×1.4 cm\(^3\) water-equivalent phantom. The phantom is placed on a plastic grid with 0.2 mm linewidth installed.
on the test bench, in front of the camera. Figure 11 shows the temperature increment on the water-
equivalent phantom after 800 s of exposure.

To compare the measured and calculated temperature increase, the temperature is averaged
over the central area on one side of the phantom far from the edges. They are plotted in Figure 12.
A very good agreement is observed between analytical calculation and measured results (the
deviation is about 3.77% and 2.59% for input powers of 3.59 W and 2.85 W, respectively).

These results confirm that the relationship between the Q-factor of the chamber, that of this
simple phantom, and the thermal model is well established under the hypothesis of an ideal random
field. As a consequence the temperature dynamics is well predicted and controlled.

Temperature distribution on murine phantoms

In this section, the temperature rise distribution on the phantoms are determined based on
IR thermometry and numerical simulations using the thermal module of CST. We analyze the
temperature rise induced by exposure to 60-GHz radiation with the incident power densities of 1
mW/cm² and 5 mW/cm².

The transmitted power within the RC (loaded with the five phantoms) to ensure average
incident power densities of 1 mW/cm² and 5 mW/cm² is 230 and 1140 mW, respectively (Equation
6). This estimation accounts for the open-ended waveguide mismatch (1-|Γ|^2 = 0.95) and efficiency
(η_e = 0.95), as well as for the quality factor of the RC loaded with the five phantoms, bedding liter
and animal cage (Q = 1.2×10⁴). From the ratio of dissipated power (27 %) in the five identical
murine phantoms (Table 3), the average power dissipated in each phantom is estimated to 12.2
mW and 61.4 mW, respectively.
In simulations, the dissipated power in murine phantom computed form quality factor measurement is used as a heat source in thermal simulations. The dissipated power is assumed to be uniformly distributed over the phantom surface. In the thermal modeling, we used the thermophysical properties of the murine phantoms reported in Table 2. The radiative heat transfer coefficient is estimated using the Stephan-Boltzmann law $h_r = 5.47 \pm 0.3 \text{ W/(m}^2 \text{K)}$, where the phantom emissivity is assumed to be $e = 0.95 \pm 0.05$ [Leduc et al., 2017; Fall et al., 2016]. The convective heat transfer $h_c$ in the exposure chamber is mainly restricted to natural convection; air motion in the RC is considered to be negligible when the fans are off. The natural heat convection coefficient depends on the difference between the phantom and environmental temperature. By assuming that the phantom temperature rise is between 1 °C and 3 °C, $h_c$ can be predicted from [Wissler, 1961] as 3.3 to 4.4 W/(m$^2$·K).

Thermal measurements were performed for the exposure duration of 5400 s with 1 s resolution. Detailed methodology of the temperature monitoring on semi-solid phantoms during mmW exposure is presented in [Leduc at al., 2017]. Five murine-equivalent phantoms were placed in the animal cage (configuration B, Fig. 9). The mechanical stirrer was rotating continuously (4 tr/min) combined with the frequency stirring with 30 excitation frequencies distributed in 58.65 – 59.15 GHz range.

Figure 13 represents temperature increment on two murine-equivalent phantoms after 5400 s of exposure. The temperature rise distributions on the two phantoms present a similar trend. The discrepancies and asymmetric temperature distribution are mainly due to imperfections of the experimental phantom fabrication and reflections of the IR radiation inside the RC. The mean values of the temperature rise are 2.30 °C and 2.32 °C, while the standard deviation (square root of the variance) are 0.16 °C and 0.22 °C. Note that temperature on the muzzle, ears and back of
the phantom are higher than in other parts of the phantom due to a high surface/volume ratio resulting in a local increase of the power density in the near-surface regions.

The computed temperature profile on the murine phantom under a plane wave spectrum illumination (Fig. 14) is in agreement with measurements. A plane wave spectrum model is an equivalent representation of the random superposition of many modes mimicking the ideal random field of RC. The incident field is equivalent to the superposition of many plane waves of the same field amplitude with random polarization and angle of incidence, having a uniform distribution. Therefore, the source term of the bioheat transfer equation is related to the average electromagnetic power density in RC according to [Fall et al., 2016.]. Figure 15 shows the heat dynamics for the temperature averaged over the surface limited by a rectangle indicated in Figure 13. Error bars on the simulated curve denote the temperature uncertainties resulting from the statistical estimation of the dissipated power ratio (the 95% confidence interval associated to the quality factor estimation). Results show good agreement between the simulated and measured heating; the relative deviation is within 3.7%. Deviations for short durations can be attributed to the sensitivity of the temperature measurement, which is of the order of 0.1-0.2°C, and therefore the results for the first minutes of exposure are less accurate compared to longer exposure durations. The temperature rise dynamics for the murine phantom and murine skin (Table 2) are compared in Figure 16. The results suggest that after 5400 s of exposure use of the murine phantom results in overestimation of heating by about 10% compared to the murine skin.

Note that the presented thermal results for artificial models do not account for the heat transfer related to sweating, a cooling mechanism in in vivo models. However, the proposed methodology for determining $S_c$ and measured temperature rise remains valid as it is independent on the heat transfer coefficient and other parameters used in analytical and numerical models.
**Parametric study**

In this section, we discuss the variations of the temperature rise on the phantom surface due to the uncertainties of the power density, heat transfer coefficient $h$, thermal conductivity $k_t$ and specific heat $C$. Variations of the average power density can be associated to uncertainties on the quality factor. Uncertainty of the volume $V$, frequency $f$ and input power $P_t$ are negligible compared the quality factor statistical uncertainty. The average quality factor is estimated over $N = 100$ positions of the stirrer and $P = 50$ frequency in each 500 MHz band. One can demonstrate using the central limit theorem that the estimated mean value for the quality factor $\hat{\mu}_Q$ is normally distributed with the standard deviation [Kostas et al., 1991]:

$$\sigma_{\mu_Q} = \frac{\sigma_Q}{\sqrt{N \times P}}, \quad (11)$$

where $\sigma_Q$ is the standard deviation of the exponential distribution associated to the modulus of $H$. The confidence interval associated to the mean value estimation can be deduced from normal distribution as

$$I = \hat{\mu}_Q \pm \frac{k \times \sigma_Q}{\sqrt{N \times P}}, \quad (12)$$

where $k$ determines the confidence. For example a confidence of 97.5% corresponds to $k = 1.96$. The normalization of equation (12) enables to calculate the relative variation around the mean value estimation given by
\[ I_n = 1 \pm \frac{k}{\sqrt{N \times P}} \times \frac{\sigma_Q}{\mu_Q} \approx 1 \pm \frac{k}{\sqrt{N \times P}}. \]  

The error over the average quality factor estimation is ±2.8% with 95% of confidence level.

As discussed previously, the variations of the radiative heat transfer coefficient are estimated to \( h_r = 5.47 \pm 0.3 \text{ W/(m}^2\text{K}) \). With regards to the convective heat coefficient, it varies between 3.3 and 4.4 W/(m\(^2\)K). The thermal conductivity and the specific heat of the 30%-polyethylene phantom are derived from linear extrapolation from data for 25%-polyethylene phantom. We assumed that \( k_i \) and \( C \) are varying in a ±10% range, although the actual uncertainty on these parameters is expected to be lower. The uncertainty on the temperature rise of each variable is assessed through simulations with CST. Results are reported in Table 4 for 5400 s of exposure. The temperature change due to the power density variability is ±3.3%, which is nearly the 95% confidence interval on the average power density estimation (±2.8%). This uncertainty can be reduced in future experiments by increasing the number of independent realizations used to estimate the quality factor.

The specific heat has a strong impact on heating (10%) in contrast to the conductivity (less than 2%). These results show that an accurate quantification of the phantom specific heat is of importance. With regard to the heat transfer radiation, its range of variations strongly depends on environmental conditions, including temperature and velocity.

**CONCLUSION**
This paper describes the design and calibration of a reverberation chamber developed as an exposure system for in vivo studies on mice in the 60-GHz band. In addition to the interface for electromagnetic and thermal dosimetry, the interfaces for lighting and ventilation were integrated into the RC walls while preserving acceptable shielding.

To characterize the electromagnetic behavior of the system, the complex power transfer function is retrieved from scattering parameter measured between two WR-15 opened ended waveguides used as transmitting and receiving antennas in the RC loaded with five murine phantoms, animal cage, and bedding litter. The murine-equivalent phantoms were specifically designed for this study, for the first time in the 60 GHz band. Results of the Anderson Darling goodness-of-fit test and empirical estimation of the standard deviation to mean ratio confirm the exponential distribution hypothesis of the modulus transfer function. This demonstrates that the loaded RC provides a nearly-ideal random Gaussian distributed field.

The calibration procedure of the power density was based on the quality factor, which was estimated to $1.2 \times 10^4$ at 60 GHz for the RC loaded with a mice cage, litter, and five phantoms. The main sources of the power dissipation in the chamber were the mice cage and murine phantoms. In particular, roughly 27% of the input power is dissipated in phantoms when the RC is loaded with five mice models. The relationships between, the transmitted power in the RC, average power density, composite quality factor and thermal measurements were investigated. The transmitted power within the RC (loaded with the five phantoms) to ensure average incident power densities of 1 mW/cm$^2$ and 5 mW/cm$^2$ was found to be 0.23 and 1.14 W, respectively.

Surface heating of the mice models was measured in the IR range using a specifically designed interface, transparent at IR and opaque at mmW. Experimental results were compared to an analytical solution of heat transfer equation (HTE) and to full-wave computations. Analytical
and numerical results were in a very good agreement with measurements (the relative deviation after 90 min of exposure was within 4.2%). Finally, a parametric study was performed to assess the impact of the thermophysical parameters on the resulting heating.

The exposure system and methodology reported in this paper can be applied to study potential modifications induced in mice models after mmW exposure. This type of studies are of importance due to near future integration of mmW technologies in 5G as well as due to increasing interest in biomedical applications of mmW [Zhadobov et al, 2015; Orlacchio et al, 2019].

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REFERENCES


IEEE Std C95.1-2005. 2005. IEEE standard for safety levels with respect to human exposure to radio frequency electromagnetic fields, 3 kHz to 300 GHz. International Committee on Electromagnetic Safety, The Institute of Electrical and Electronics Engineers. New York, USA.

IEEE Std C95.1-2019. 2019. IEEE standard for safety levels with respect to human exposure to electric, magnetic, and electromagnetic fields, 0 Hz to 300 GHz. IEEE International Committee on Electromagnetic Safety, The Institute of Electrical and Electronics Engineers. New York, USA.


mmMAGIC “mm-Wave based Mobile Radio Access Network for 5G Integrated Communications (mmMAGIC)”. Available from https://5g-mmmagic.eu [Last accessed 13 August 2019].


Figure captions

Fig. 1. 3D CAD design of the RC designed in solidworks: a) 3D view; (b) side view.

Fig. 2. Experimental set-up. A murine plastic cage is placed in the middle of the RC. It is filled with 30 g of bedding litter and contains five identical mice phantoms.

Fig. 3. Murine-equivalent phantom at 60 GHz.

Fig. 4. Complex permittivity of the murine skin-equivalent phantoms with 30% polyethylene powder concentration: (a) real part; (b) imaginary part. Error bars represent ±12 % with respect to target value of the murine skin permittivity.

Fig. 5. Average first-order autocorrelation function calculated for the transfer function $|H|$.

Fig. 6. Anderson Darling goodness-of-fit test for exponential distribution for the transfer function $|H|$.

Fig. 7. Normalized standard deviation estimated from the transfer function $|H|$.
Fig. 8. Experimental $Q$-factor of the RC for the empty RC, RC loaded with the murine cage, RC loaded with the murine cage and the bedding litter, RC loaded with these elements and one phantom, RC loaded with 5 phantoms.

Fig. 9. The five considered configurations for estimation of the quality factor variability with respect to the positions of phantoms.

Fig. 10. Experimental $Q$-factor of the reverberation chamber with respect to the positions of the phantoms.

Fig. 11. Heating of the water-equivalent phantom surface recorded by the IR camera after 800 s of exposure. Input power of (a) 3.59 W, (b) 2.85 W.

Fig. 12. Measured and calculated temperature rise on the water equivalent-phantom surface for 900 s of exposure.

Fig. 13. Heating of the murine phantoms surface recorded by the IR camera after 5400 s of exposure for an input power of 1.14 W.
Fig. 14. Computed temperature distribution on a murine phantom for an input power of 1.14 W.

Fig. 15. Computed and measured averaged temperature rise on the murine phantoms.

Fig. 16. Temperature rise on the murine-equivalent phantom with thermophysical properties of a 30% polyethylene phantom compared to murine skin thermophysical model.
**Table captions**

Table 1. Composition of the murine-equivalent phantom

Table 2. Thermophysical properties of the murine-equivalent phantom, water-equivalent phantom and murine skin

Table 3. Ratio of the power dissipated in the walls, phantoms, bedding litter, and animal cage.

Table 4. Variability of heating according to uncertainties on thermophysical parameters and power density.
Fig. 1.
Fig. 2.
Fig. 3.
Fig. 4.
Fig. 5.

- Empty RC
- Mice cage
- Mice cage + litter
- Mice cage + litter + 5 phantoms

FOAF vs Frequency (GHz)
Fig. 6.

![Graph showing rejection rate vs. frequency (GHz).](image)

- Empty RC
- Mice cage
- Mice cage + litter
- Mice cage + litter + 5 phantoms
Fig. 7.
Fig. 8. 

- Empty RC
- Mice cage
- Litter
- Phantom

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RC + mice cage + litter + 5 phantoms

Average Q-factor vs. Frequency (GHz)
Fig. 11.
Fig. 12
Fig. 15.
Fig. 16.

- Simulation (phantom)
- Simulation (murine skin)
Table 1.

<table>
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<tr>
<th>Ingredients</th>
<th>Mass (g)</th>
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Table 4.

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<td>$C$ [J/kg.°C]</td>
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<td>± 9.9</td>
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