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# Pulse doublets generated by a frequency-shifting loop containing an electro-optic amplitude modulator

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**Abstract:** We investigate theoretically and experimentally an all-fibered frequency-shifting loop which includes an electro-optic amplitude modulator (EOM) and an optical amplifier, and is seeded by a continuous-wave laser. At variance with frequency-shifted feedback lasers, or Talbot lasers, that contain an acousto-optic frequency shifter, the EOM creates at each round-trip two side-bands that recirculate inside the loop. Benefiting from the high modulation frequency of the EOM, a wide optical frequency comb up to 40 GHz is generated. We demonstrate an original double-pulse regime when the loop length is a multiple of the RF modulation wavelength applied to the modulator. The inter-pulse interval is governed by both the bias voltage and modulation depth of the EOM. Besides, some typical waveforms such as saw-tooth and rectangle are experimentally obtained by properly setting operating frequency, bias voltage and the RF power. The system is modeled by a linear interference model that takes the amplitude modulation function and loop delay into account. The model explains the formation of pulse doublets and reproduces well all the experimental waveforms. Furthermore, the un-seeded loop driven above threshold also generates mode-locked picosecond pulse doublets with a continuously adjustable delay up to the modulation period.

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## 1. Introduction

Microwave photonics is an innovative multi- and interdisciplinary field that investigates the interaction between microwave and optical signals including microwave signal generation and processing [1–3], microwave-photonics systems [4,5], and broadband optical links for high-speed interconnects [6]. In particular, the generation of high repetition-rate optical pulses plays an important role in high-speed optical fiber and microwave photonics systems [7,8]. In this respect, frequency-shifting loops (FSL), that are loop resonators containing both an amplifier and an acousto-optic frequency-shifter (AOFS), have been demonstrated to be promising solutions to generate Fourier-transform-limited pulses with tunable and ultrahigh repetition rates [9–11]. When the frequency shift is tuned to a fraction of the cavity free-spectral range, periodic pulse trains can be generated from a continuous-wave seed laser, leading to a so-called “Talbot laser” due to the complete analogy with the spatial Talbot effect [12]. Similar all-fiber set-ups have also been extended to applications such as high data-rates in radio-over-fiber communications [13,14], real-time Fourier transformation of optical signals [15] and have also recently been shown to produce arbitrary waveform generation [16].

Frequency-shifted loops usually rely on the use of an acousto-optic frequency-shifter. While it features high frequency conversion efficiency in the sub-100 MHz range, AOFS have limited efficiency in the GHz range, and offer limited tunability. In this respect, EOM offer much higher modulation frequency and bandwidth. Besides, EOM are compact and easy to integrate with other fibered devices. Few studies investigated single-sideband EOM

operation in FSLs: a multi-carrier source was built with high power flatness and stability [14], and recently GHz repetition rates were demonstrated in the Talbot configuration [17]. In this article, we investigate an all-fibered frequency-shifted feedback loop when a widely tunable common, dual side-band, electro-optic amplitude modulator (EOM) is employed. Instead of the single side-band AO frequency-shift or SSB-EOM, the loop will produce at each round-trip two side-bands with opposite frequency-shifts. The carrier will also circulate together with the multiple frequency-shifted sidebands. This raises questions about the ability to generate a pulse train from a continuous-wave seed, the so-called continuous-to-pulse conversion regime [11,12], or to generate arbitrary waveforms [16,18]. Furthermore, an analytical model has to be derived in order to take into account the specific transfer function of the EOM.

We first present the method and the corresponding model in Section 2. In particular, we focus on the integer Talbot condition where predictions can be derived from simple algebra. Section 3 presents the experimental results obtained with standard components at 1.55  $\mu\text{m}$  wavelength, looking at the influences of the EOM parameters on the FSL properties. Pulse train generation and specific waveforms are investigated by precisely controlling the modulating frequency, RF power and the bias voltage applied to the EOM. Then Section 4 is devoted to the extension of the method to the un-seeded, mode-locked laser operation, and the comparison with the results of Section 3. Finally, conclusions and perspectives are included in Section 5.

## 2. Method

### 2.1. Set-up principle

We consider the fiber loop depicted in Fig. 1. It contains an electro-optic amplitude modulator (EOM) that induces a dual-sideband frequency shift per round-trip  $f_m$ , and an erbium-doped fiber amplifier (EDFA) providing gain that partially compensates for the loop losses and enhances the number of relevant round-trips inside the loop, as in AOFS-based loops. Besides, an optical filter permits to limit the output bandwidth and efficiently reduces parasitic loop oscillations, while a polarization controller also stabilizes the loop operation. The round-trip time is  $\tau = nL/c$ , where  $n$  is the group index of the loop fiber. This leads to a fundamental loop frequency  $f_c = 1/\tau$ . A  $2 \times 2$  optical coupler enables to seed the loop and to extract a fraction of the circulating laser power. The EOM is driven by a radiofrequency synthesizer (SYN) and a bias voltage (DC). We assume that the loop is below the laser threshold, i.e., the gain does not compensate for the losses. The setup is similar to the one of Refs [11–13] but the frequency-shift is provided by a common EOM instead of an AOFS.

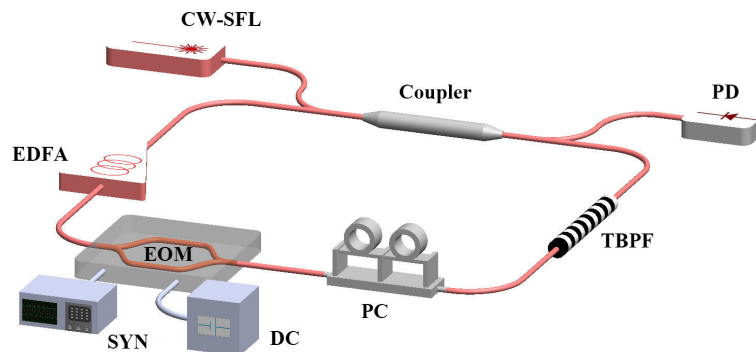


Fig. 1. Sketch of the dual side-band FS loop. CW-SFL: continuous-wave single-frequency laser; PD: photodiode; TBPF: tunable bandpass filter; PC: polarization controller; EOM: Mach-Zehnder intensity modulator driven at frequency  $f_m$  (SYN) and bias voltage  $V_b$  (DC); EDFA: erbium-doped Optical Fiber Amplifier.

## 2.2. Model

In order to predict the output waveform, we derive a time-delayed interference model. Given the transmission matrix of the coupler  $[t_{ij}]$  and  $E_{in}$  the input electric field of the coupler, the output field  $E_{out}$  can be written as follows:

$$\begin{bmatrix} E_{out1} \\ E_{out2} \end{bmatrix} = \begin{bmatrix} t_{11} & t_{12} \\ t_{21} & t_{22} \end{bmatrix} \begin{bmatrix} E_{in1} \\ E_{in2} \end{bmatrix}. \quad (1)$$

In the case of a lossless coupler, the  $t_{ij}$  verify the condition  $t_{11}t_{22} - t_{12}t_{21} = 1$  [19]. At round-trip  $p$ , the real transfer function of the EOM can be modeled as  $Y^{(p)}(t) = \sin[\Gamma + \Gamma_m \sin(2\pi f_m(t - p\tau))]$ , where  $\Gamma_m$  is the modulating depth that depends on the RF power  $P_{dc}$ .  $\Gamma$  is the static phase retardance of the EOM that can be controlled by the applied bias voltage  $V_b$ . If  $\eta$  and  $G$  are the intensity loss of the loop and the intensity gain parameters, respectively, then we write  $\gamma = \sqrt{\eta G}$  the overall amplitude transmission. To find out the field circulating inside the loop, we calculate the electric field at output port 2. From Eq. (1), this field writes:

$$E_{out2}(t) = t_{21}E_{in1} + t_{22}E_{in2}, \quad (2)$$

from which one gets:

$$E_{out2}(t) = t_{21}E_{in1}(t) + t_{22}\gamma E_{out2}(t - \tau)Y^{(1)}(t). \quad (3)$$

This formulation can be expanded using

$$E_{out2}(t - \tau) = t_{21}E_{in1}(t - \tau) + t_{22}\gamma E_{out2}(t - 2\tau)Y^{(2)}(t). \quad (4)$$

Inserting Eq. (4) into the right-hand side of Eq. (3), the equation can be expanded to  $N$  round-trips in the loop:

$$E_{out2}(t) = t_{21}E_{in1}(t) + \sum_{p=1}^N t_{21}t_{22}^p \gamma^p \prod_{l=1}^p Y^{(l)}(t) E_{in1}(t - p\tau). \quad (5)$$

The experimentally accessible and useful signal is at the output port 1. If the input field at port 1 is a single-frequency continuous-wave with power  $P_{in}$ , then

$$E_{out1}(t) = t_{11}\sqrt{P_{in}} + t_{21}t_{12} \sum_{p=1}^N t_{22}^{p-1} \gamma^p \prod_{l=1}^p Y^{(l)}(t) \sqrt{P_{in}}, \quad (6)$$

from which the power  $P_{out}(t)$  can be derived:

$$P_{out}(t) = \left| t_{11} + t_{21}t_{12} \sum_{p=1}^N t_{22}^{p-1} \gamma^p \prod_{l=1}^p Y^{(l)}(t) \right|^2 P_{in}. \quad (7)$$

In the following, we use Eq. (7) to calculate the output waveform. Note that contrary to the theoretical model developed for AOFS loops [11,12], here no simple analytical formula can be deduced. However, under the integer Talbot conditions  $f_m = nf_c$ , where  $n$  is an integer, we find  $\sin[2\pi f_m(t - p\tau)] = \sin(2\pi f_m t)$ . Then, in the limit  $N \rightarrow +\infty$ , the sum of the geometric series in Eq. (7) can be simplified, leading to

$$P_{out}(t) = \left| t_{11} + \frac{t_{21}t_{12}\gamma \sin \theta(t)}{1 - t_{22}\gamma \sin \theta(t)} \right|^2 P_{in}, \quad (8)$$

where we introduced  $\theta(t) = \Gamma + \Gamma_m \sin(2\pi f_m t)$ . Since  $t_{22}\gamma \sin\theta(t) < 1$  (assuming  $t_{22}$  real positive), obviously  $\sin\theta(t)/(1-t_{22}\gamma \sin\theta(t))$  will be a sharp function peaked at  $\theta(t) = \pi/2$ . As in the AOFs-based loops, pulses are found when the Talbot condition is met, i.e., when the modulation frequency is an integer number of times the loop frequency (or, equivalently, when the loop length is an integer number of times the beat length). It is interesting to note that Eq. (8) is independent of  $n$ , which means that the pulse shape is expected to be the same whatever the modulation frequency, and that the pulses will become shorter as frequency increases. According to Eq. (8), the important point, specific to our amplitude modulation case, is that two temporally separated solutions satisfy Eq. (8) in one period  $1/f_m$ . Indeed, we may predict that the response of the amplitude-modulated loop in the time domain delivers a periodic series of pulse *doublets*. The delay  $\Delta t$  between the two pulses in one period  $1/f_m$  is found to be

$$\Delta t = \frac{1}{2f_m} \left[ 1 - \frac{2}{\pi} \sin^{-1} \left( \frac{\pi/2 - \Gamma}{\Gamma_m} \right) \right]. \quad (9)$$

This shows that  $\Gamma$  and  $\Gamma_m$  will have a strong influence on the delay. Sketches of the output time responses with different  $\Gamma$  and  $\Gamma_m$  are depicted in Figs. 2(a)-2(b). For example if  $\Gamma = \pi/2$  then  $\Delta t = 1/(2f_m)$ , leading to a pulse repetition rate equal to twice the modulation frequency (red curve in Fig. 2(a)).

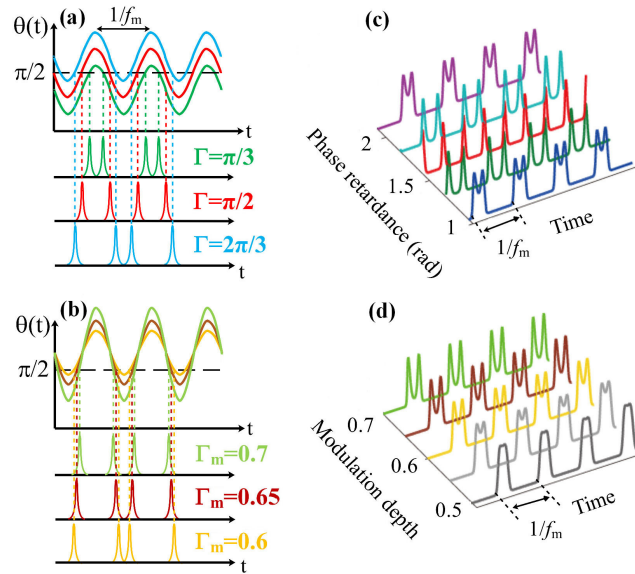


Fig. 2. Sketches of output signal vs time, with (a) different  $\Gamma$  and (b) different  $\Gamma_m$ . Simulation output power with (c)  $\Gamma = \pi/3$  (blue),  $5\pi/12$  (green),  $\pi/2$  (red),  $7\pi/12$  (light blue), and  $2\pi/3$  (purple), and (d)  $\Gamma_m = 0.5$  (black),  $0.55$  (grey),  $0.6$  (yellow),  $0.65$  (brown), and  $0.7$  (green).

To further illustrate the influence of  $\Gamma$  and  $\Gamma_m$  on the double-pulse operation, we perform simulations based on Eq. (7) with  $N = 30$  round-trips. Figure 2(c) depicts the simulation results, with  $\Gamma_m = 0.7$  and  $\gamma = 0.9$  for example, showing that the delay between the two pulses increases with  $\Gamma$ . Then the influence of  $\Gamma_m$  on the double-pulse is also simulated and depicted in Fig. 2(d) when  $\Gamma = 2\pi/3$ . With the increase of  $\Gamma_m$ , the delay gradually approaches one half period. Note that  $\Gamma_m$  also has an influence on the pulse width. Indeed, lower values of  $\Gamma_m$  will directly reduce the width of the optical-carried RF comb in the optical frequency domain, hence leading to pulse widening. These predictions are tested experimentally in the following.

### 3. Pulse doublets experiments

#### 3.1 Experimental parameters

We experimentally investigate the time response of the dual side-band frequency-shifting loop as depicted in Fig. 1. Experiments are performed with a continuous-wave tunable single-frequency semiconductor laser, which delivers 0.5 mW in the C band, with a linewidth of about  $\Delta\nu = 100$  kHz. In order to avoid parasitic oscillations when the EDFA gain is raised, we use a 40 GHz-bandwidth (0.3 nm) optical filter inside the loop. Here, at variance with the FS loop of Refs [10–12] where the wavelength of the seed laser is at one edge of the optical filter (single-sideband frequency comb), we set the wavelength of our laser at the center of the optical filter around 1552 nm (dual-sideband frequency comb). From the measured values of the four intensity transmission coefficients,  $|t_{ij}|^2$  the coupling matrix is set to

$$\begin{bmatrix} t_{ij} \end{bmatrix} = \begin{bmatrix} 0.44 & 0.65i \\ 0.43i & 0.67 \end{bmatrix}. \text{ The loop fundamental frequency is measured to be } f_c = 6.737 \text{ MHz,}$$

corresponding to a loop delay time  $\tau = 0.148 \mu\text{s}$  and an optical length of 44.53 m. Note that the coherence length  $L_c = c/\Delta\nu$  ( $c$  is the velocity of light in the medium) of the seed laser corresponds to more than 60 round-trips, exceeding the  $N = 30$  round-trips used in the simulation. The polarization controller (PC) is utilized to stabilize the polarization state of the laser signal to make the modulation depth higher and waveform more stable. In order to minimize the output pulse width (or maximize the optical bandwidth), the polarization state of the laser and the pump current of the EDFA are adjusted jointly. The detection setup consists in a 40 GHz-bandwidth photodiode and a high-resolution optical spectrum analyzer. The signal in time domain is monitored with an 11 GHz-bandwidth and 40 Gs/s sampling-rate oscilloscope.

Finally, the EOM is a 10 GHz-bandwidth Mach-Zehnder modulator with a half-wave voltage of 4 V. The FS loop output characteristics depend on RF frequency  $f_m$ , RF power  $P_{dc}$ , and bias voltage  $V_b$ .

#### 3.2. Dual-pulse regime

In agreement with the theoretical results obtained with  $f_m = n f_c$ , we find that the time response of the dual side-band FS loop is a periodic train of the pulse doublets with a temporal period equal to the inverse of the RF frequency applied to the EOM, as shown in Fig. 3. Figures 3(a)-3(d) report the experimental results when  $n = 1$  ( $f_m = 6.737$  MHz), 10 (67.37 MHz), 100 (673.7 MHz), and 500 (3.369 GHz), respectively. The delay is also shown to be continuously adjustable from  $\Delta t = 0$  to  $\Delta t = 1/(2f_m)$  by changing the bias voltage  $V_b$ , hence the static retardance of the EOM, in agreement with Eq. (9). Different traces are selected and depicted in Fig. 3. By comparing Figs. 3(a)-3(c), a striking observation here is that the pulse pattern remains the same, regardless of the value of  $n$  over three orders of magnitude, in agreement with the model. Of course the repetition rate scales as  $n$ , but it appears that the pulse duration  $\tau_p$  scales as  $1/n$ , leading to a constant duty cycle  $\tau_p f_m$ . This is because the harmonics content does not depend on the modulation frequency. Indeed, when  $V_b$  and  $P_{dc}$  are kept constant, from  $n = 1$  to  $n = 100$  the pulse width decreases from 13 ns down to 130 ps (see Figs. 3(a)-3(c)), yielding a constant  $\tau_p f_m = 0.087$ . At higher values of  $n$  the measurement of the pulse width is limited by the 28 ps-rise time of the detection (see Fig. 3(d) when  $f_m = 3.369$  GHz).

We measure the optical output spectrum by using a 0.06 pm-resolution OSA. As expected, the output optical spectrum contains a dual side-band RF comb, with the seed wavelength at the center and  $f_m$ -harmonics on both sides. In our experimental conditions, we could generate a few dozen harmonics. For example, when  $f_m$  is 673.7 MHz, the total width of the optical-carried RF comb is  $39 \times f_m = 26.3$  GHz, as shown in Fig. 4 (a). Raising the gain to higher values leads to parasitic oscillations. When  $f_m = 3.369$  GHz, Fig. 4(b) shows a 40.4 GHz-wide optical frequency comb. In this case, the optical bandwidth is not limited directly by the gain,

but by the optical filter edges. Moreover, we could observe that changes in the bias voltage influences the harmonics intensities. Namely, at  $V_b = 4$  V when the repetition rate is doubled, odd harmonics are lower than even harmonics. Precisely measuring the short picosecond pulse width (e.g. with an autocorrelator) would permit further analysis of the spectral-temporal relationship.

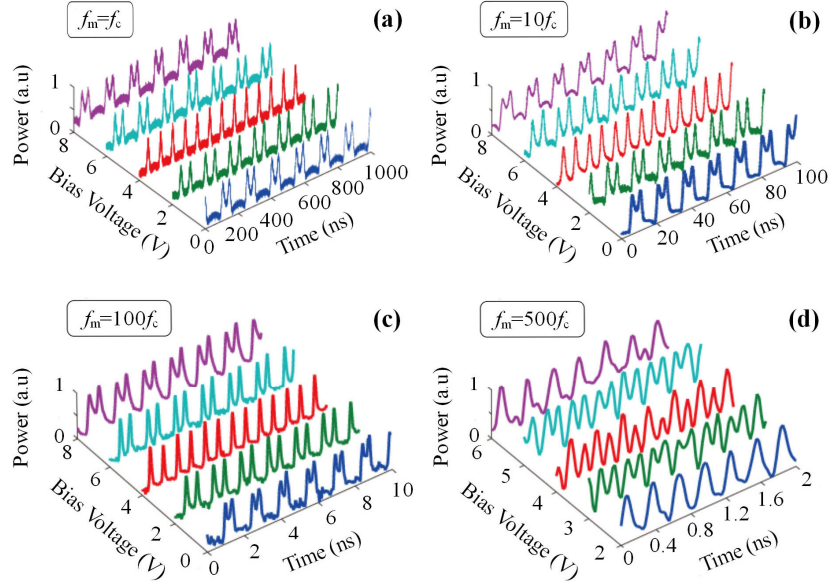


Fig. 3. Experimental pulse doublet regime when  $f_m = nf_c$ : influence of the modulation frequency  $f_m$  and the bias voltage  $V_b$ .  $P_{dc} = 25$  dBm; (a)  $n = 1$ ; (b)  $n = 10$ ; (c)  $n = 100$ ; (d)  $n = 500$ . In (a)-(b)-(c),  $V_b = 0$  V (blue lines), 2 V (green lines), 4 V (red lines), 6 V (light blue lines), 8 V (purple lines). In (d),  $V_b = 2$  V (blue line), 3 V (green line), 4 V (red line), 5 V (light blue line), 6 V (purple line). Pulse FWHM  $\tau_p$  measured when  $V_b = 4$  V: (a)  $\tau_p = 13$  ns, (b) 1.3 ns, (c) 130 ps, (d) 80 ps (detection limit).

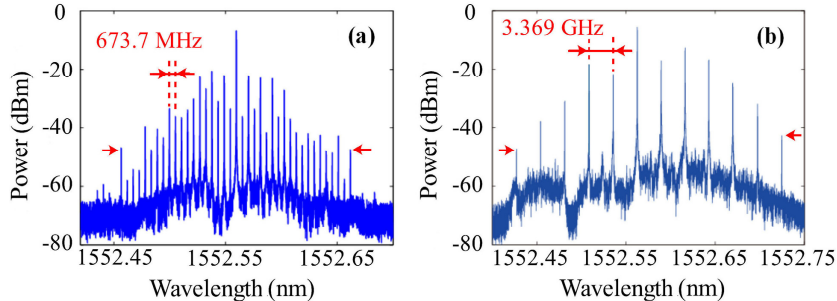


Fig. 4. Optical spectrum of the dual side-band FS loop. (a)  $f_m = 673.7$  MHz, the two arrows show the  $\pm 19^{\text{th}}$  harmonics. The total comb width is  $39 \times f_m = 26.3$  GHz. (b)  $f_m = 3.369$  GHz and the two arrows show the  $-5^{\text{th}}$  to  $+6^{\text{th}}$  harmonics. The total comb width is  $12 \times f_m = 40.4$  GHz.

The RF power applied to the EOM is another important factor influencing the double-pulse properties. We first keep  $f_m = f_c = 6.737$  MHz and  $V_b = 2$  V; Figs. 5(a)-5(c) show that by decreasing  $P_{dc}$ , which corresponds to decreasing the modulation depth  $\Gamma_m$ , we find that (i) the pulse width significantly increases and (ii) the delay decreases. The first feature (i) comes from spectral narrowing due to reduction in the harmonics amplitudes, leading to pulse widening. The second feature (ii) can be understood from the sketch of Fig. 2(b) and Eq. (9): the delay depends on  $\Gamma_m$ , except for the particular point  $\Gamma = \pi/2$  where  $\Delta t = 1/(2f_m)$  whatever the value of  $\Gamma_m$ . This is confirmed by repeating the experiment with  $V_b = 4$  V: Figs. 5(d)-5(f)

show an increase in the pulse width while the delay remains constant, in agreement with Eq. (9).

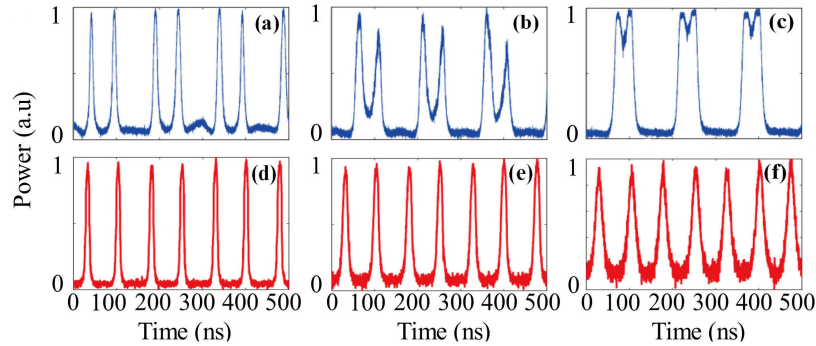


Fig. 5. Influence of RF power on the pulse train. (a),(d)  $P_{dc} = 25$  dBm; (b),(e) 23 dBm and (c), (f) 21 dBm. Upper row (blue curves):  $V_b = 2$  V; lower row (red curves):  $V_b = 4$  V.

### 3.3. Rectangle and triangle waveform generation

Following the preceding conclusions, we find a simple means to generate a rectangle waveform with an adjustable duty cycle. By precisely adjusting  $V_b$  and  $P_{dc}$  to make the falling-edge of the first pulse coincides with the rising-edge of the second, we can obtain a rectangle waveform with different duty cycles. As a typical example, we set  $f_m = 1.0039$  GHz ( $149f_c$ ), and adjust  $V_b$  (resp.  $\Gamma$ ) and  $P_{dc}$  (resp.  $\Gamma_m$ ) in the experiments (resp. in the simulation). Figure 6 reports the rectangle waveforms. The FS loop with  $P_{dc} = 21$  dBm generates a double-pulse pattern with  $\tau_p \sim 300$  ps. We first choose the bias to  $V_b = 1.5$  V in order to transform the double-pulse into a rectangle waveform with a duty cycle of 1:3 (see Fig. 6(a)). When  $V_b$  increases to 2.6 V and  $P_{dc}$  decreases to 20 dBm simultaneously, we obtain the rectangle waveform with a duty cycle of 1:2, i.e. a square wave, as shown in Fig. 6(b). As a last example, Fig. 6(c) shows a rectangle waveform with a duty cycle of 2:3 in the case of  $V_b = 3.3$  V and  $P_{dc} = 19$  dBm. Corresponding simulations are depicted in Figs. 6(d)-6(f) showing a good agreement with the experimental results.

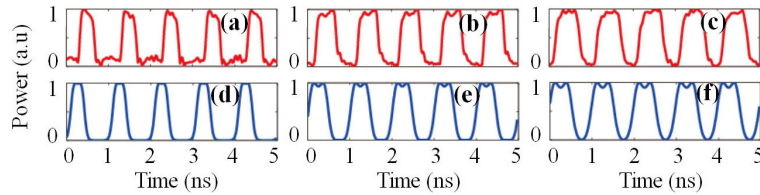


Fig. 6. Rectangle waveform generation; influence of the bias voltage and the RF power on the duty cycle. (a)-(c): Experiment results with (a)  $V_b = 1.5$  V,  $P_{dc} = 21$  dBm; (b)  $V_b = 2.6$  V,  $P_{dc} = 20$  dBm and (c)  $V_b = 3.3$  V,  $P_{dc} = 19$  dBm. (d)-(f): Simulation results with (d)  $\Gamma = 1$  rad,  $\Gamma_m = 0.6$ ; (e)  $\Gamma = 1.2$  rad,  $\Gamma_m = 0.5$  and (f)  $\Gamma = 1.4$  rad,  $\Gamma_m = 0.3$ .

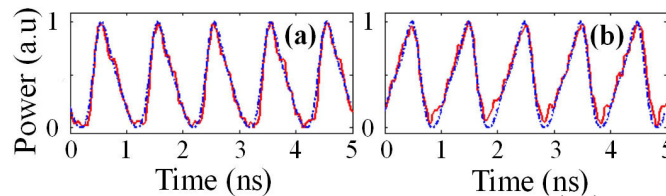


Fig. 7. Saw-tooth waveforms with (a)  $f_m = 1.0028$  GHz, (b)  $f_m = 0.99835$  GHz. (red line: experiment; dotted blue line: simulation).



The waveform generation is not limited to the rectangle case. It is well known that AOFS loops output waveform relies on the shifting frequency  $f_m$ , and RF power, and the loop length. Here, we find saw-tooth waveforms when we slightly detune the modulation frequency of the EOM off an integer value  $nf_c$ . For example, we set  $f_m = 1.0028$  GHz and 0.99835 GHz, respectively, and find the triangle waveforms reproduced in Figs. 7(a)-7(b). In the experiment, we keep  $V_b = 3$  V and  $P_{dc} = 25$  dBm. A good agreement with the experiment is obtained when  $\Gamma_m = 0.6$  and  $\Gamma = 1.2$  in the simulations (see blue dotted lines in Fig. 7), confirming the validity of the linear model.

#### 4. Mode-locked pulse doublets generation from the un-seeded loop

For the sake of completeness, we investigate shortly the loop behavior without the seed laser when the gain exceeds the losses, i.e., when the loop is driven above laser threshold. It has long been shown that phase or loss modulation of lasers lead to the mode-locked regime when the modulation frequency is a multiple of the cavity free-spectral range [20,21]. In particular picosecond pulse generation was demonstrated in erbium-doped fiber lasers using phase modulators [22–24]. However, contrary to phase-modulated mode-locked lasers, here it appears that amplitude modulation leads to picosecond pulse doublet operation, a situation that, to the best of our knowledge, has never been reported. The EDFA in our set-up allows us to raise the gain up to the laser threshold. We show at first the experimental results when  $f_m = f_c$  in Fig. 8 (in this case the fiber loop was slightly reduced, leading to  $f_c = 7.611$  MHz). Obviously, the double-pulse regime still exists in this un-seeded mode-locked operation. Furthermore, it is interesting to note that the delay time is continuously tunable and also obeys Eq. (9), as shown for example in Fig. 8 with two different values of the bias voltage. At variance with the seeded case of Section 3, in which the pulse width is about 13 ns, here the laser pulses can be reduced down to  $\tau_p = 425$  ps (when  $V_b = 4$  V). Also in agreement with the linear model, the un-seeded FS ring laser generates sub-nanosecond pulses when  $f_m = nf_c$  with  $n \neq 1$  (harmonic mode-locking). Figure 9 evidences this double-pulse regime, without seed laser, up to  $n = 100$ , where harmonic mode-locked pulses have a 70 ps duration.

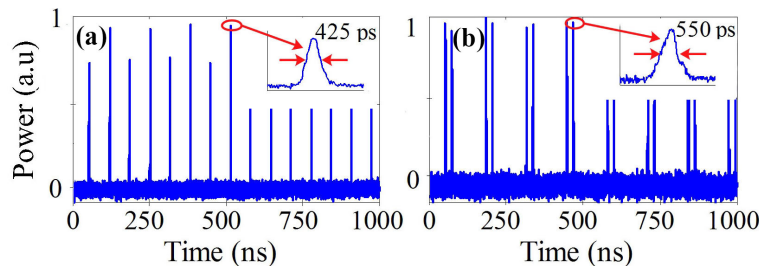


Fig. 8. Resonant mode-locked double-pulse operation with  $f_m = 7.611$  MHz. (a)  $V_b = 4$  V. (b)  $V_b = 0$  V.

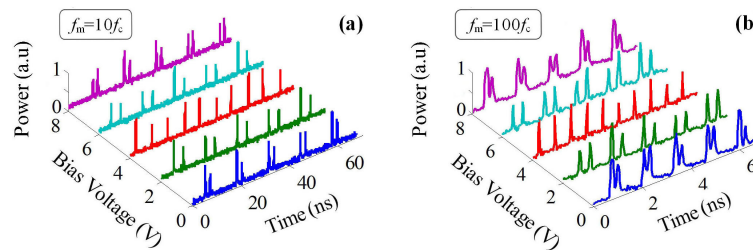


Fig. 9. Harmonic mode-locked double-pulse operation. Experimental laser output when (a)  $f_m = 76.11$  MHz,  $\tau_p = 210$  ps (b)  $f_m = 761.1$  MHz,  $\tau_p = 70$  ps.

## 5. Conclusion

To sum up, a FSL containing an amplitude modulator and an amplifier produces pulses in the sub-nanosecond range when seeded by a cw laser, if the loop length is a multiple of the RF modulation wavelength applied to the modulator. This experiment shows an alternative approach to AOFS loops, taking advantage of the inherent bandwidth and tunability of the EOM. We have evidenced analytically and experimentally an original regime of pulse doublets that finds its origin in the transfer function of the EOM. It is found that the delay between the pulses is simply governed by the modulator's bias. In addition, by properly setting the modulation frequency, adjustable rectangle and saw-tooth waveforms can be obtained. Finally the double-pulse regime survives to above-threshold operation: without the seed, mode-locked picosecond pulse doublets are also generated with an adjustable delay.

Beyond this first demonstration, careful characterization and reduction of jitter issues need further work that is under progress. Designing a loop with all polarization-maintaining fiber components, as well as acoustic and thermal isolation, would improve the stability.

The proof-of-concept demonstrated here could be extended to integrated photonics since optical rings, filters, and EOMs can be integrated on photonic platforms. This EOM-based FS loop could address applications already envisioned with FS loops, like high-repetition rate pulse trains [11], RF waveform generation [13,25] and processing [14], or ranging [18,26,27]. Besides, such a scheme may be considered when designing pump-probe experiments, since the delay can be voltage-controlled without using moving delay lines.

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