

Recent advances in modeling and simulation of nanofluid flows-Part II Applications

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Recent Advances in Modeling and Simulation of Nanofluid Flows-Part II: Applications

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Abstract

Modeling and simulation of nanofluid flows is crucial for applications ranging from u. cooling of electronic devices to solar water heating systems, particularly when compared to the high expense of experimental studies. Accurate simulation of a thermal-fluid system requires a deep understanding of the underlying physical phenomena occurring in the system. In the case of a carplex nanofluid-based system, suitable simplifying approximations must be chosen to strike a balance between the nano-scale and macro-scale phenomena. Based on these choices, the corrupttatic all approach-or set of approaches-to solve the mathematical model can be identified, implement and validated. In part I of this review [1], we presented the details of various approaches use are used for modeling nanofluid flows, which can be classified into single-phase and two-phase approaches. Now, in part II, the main computational methods for solving the transport equations associated with nanofluid flow are briefly summarized, including the finite difference, finite volume, finite element, lattice Boltzmann methods, and Lagrangian methods (such as dissipative particle dynamics and molecular dynamics). Next, the latest studies on 3D simulation of nanofluid flow in various regimes and configurations are reviewed. The numerical studies in the literature mostly focus on prious forms of heat exchangers, such as solar collectors (flat plate and parabolic solar collectors), microchannels, car radiators, and blast furnace stave coolers along with a few other important nanofluid flow applications. Attention is given to the difference between 2D and 3D simulation the e fect of using different computational approaches on the flow and thermal performance pred ctions, and the influence of the selected physical model on the computational results. Finally, the Pnox edge gaps in this field are discussed in detail, along with some suggestions for the next step, in this field. The present review, prepared in two parts, is intended to be a comprehensive reference at researchers and practitioners interested in nanofluids and in the many applications of nanofluid n. vs.

Keywords: Nanofluids, phy. al r.odels, 3D modeling, CFD techniques

Table of Contents

1- Introduction	4	
2. CFD techniques for nanofluid flow solution	4	
2.1. Macroscale based techniques	5	
2. 1.1. Finite difference method		
2.1.2. Finite volume method		
2.1.2.1 Common FVM based Software		
2.1.3. Finite element method	10	
2.1.3.1. Common FEM based Software	11	
2.1.4. Other macroscale based techniques	12	
2.1.4.1. Control Volume Finite Element Method	12	
2.1.4.2. Boundary Element Method	13	
2.1.4.3. Spectral Method	13	
2.1.4.4. Meshless methods	14	
2.2. Mesoscale based techniques		
2.2.1. Lattice Boltzmann method	17	
2.2.2. Dissipative particle dynamics method	18	
2.3. Microscale based techniques (Molecular dynamic st. nutation)	23	
3. Three dimensional computational modeling of na. Affluid flows	26	
3.1. Natural convection of nanofluid flow	28	
3.1.1. Two dimensional versus three dimensional nodeling	28	
3.1.2. What role does the CFD techniq e play ** the modeling results?	30	
3.1.3. What is the effect of nanofluid 'vp' on 'ie heat transfer rate?	31	
3.1.4. What is the effect of a magnetic field applied to natural convection nanofluid flow?		
3.1.5. What is the effect of cavity configuration on natural convection?	35	
3.2. Forced convection of nanof aid low	50	
6.2.1. Studies using the single- _r ' ase approach.	51	
3.2.2. Studies using the t vo-r tase approach	59	
3.3. Mixed convection of nanc quie flow	83	
3.3.1. Studies using ne sing. 3-phase approach.	83	
3.3.2. Studies using the two phase approach	86	
4. Conclusions	98	
5- Gaps and future w -k	99	
Acknowledgmen	101	
References	102	

1- Introduction

Although the study of thermal systems through experimental physics is always a valuable approach, it has some limitations and disadvantages. One of the drawbacks might be the a. Fully in determining the contribution of various physical phenomena to the system efficacy. No over, high costs of experiments are often a barrier for doing in-depth experimental studies. Modeling and simulation of the desired system increasingly offer a suitable alternative to experiments. I s mentioned in Part I of this review [1], experiments on nanofluids are sometimes probablive due to the high expense of nanofluid preparation, and information gained from such experiments is limited by difficulties in imaging at the nanoscale in flowing systems. These challeng's motivate researchers to use computational fluid dynamics (CFD) techniques to simulate namefluids-based systems, which can often be done at far lower expense and yield highly data on system performance and its relationship to microscale physics. For modeling of panofluids-based systems, it is critical that the dominant physical phenomena affecting the performance of the system are first determined, following which a suitable model to describe these phenomera can be selected. Part I of this review gave a comprehensive discussion of various physical phenomena responsible for heat transfer enhancement in nanofluid flows along with associate physical models. In part II of the review, the aim is to summarize the most popular computational fluid dynamics (CFD) techniques that are used for simulation of nanofluids. Following this, recent studies on 3D modeling of thermal systems employing a nanofluid is as the working fluid are reviewed Fine 11v gaps and challenges in modeling of nanofluid flows are presented and some proposals are give. for future work.

2. CFD techniques for Manon Sid flow solution

Generally, it is difficult to so we the nanofluid flow problems analytically because of the nonlinear nature of the go erning equations. Therefore, to find the velocity and temperature fields, computational fluid dynamics (CFD) techniques may be used. In this part, the main CFD techniques that are used to department the flow and heat transfer characteristics in nanofluid flows are briefly reviewed.

These techniques can be classified into three main groups as follows[2]:

- Macroscale based techniques
- Mesoscale based techniques
- Microscale based techniques

Figure 1 presents different CFD techniques for solution of nanofluid flow.

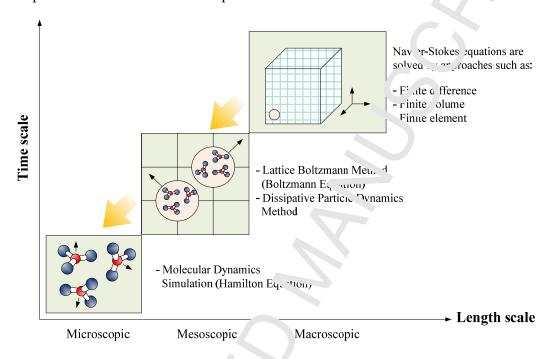


Figure 1. Different CFI tec' niques for solution of nanofluid flows.

Since the aim of the present work is a simple to focus on physical aspects of nanofluid flows, in the following just a brief description of each CFD technique is presented.

2.1. Macroscale based techniques

Macroscale based tech iques such as finite difference, finite volume, and finite element deal with converting partial differential equations to algebraic equations through discretization. Here, the common macroscale based approaches are briefly reviewed.

2. 1.1. Finite di contra method

Euler was probably the first one who introduced "finite difference method" to solve differential equations in more than 200 years ago. Finite difference method (FDM) is the oxiest and easiest numerical approach to solve the flow and heat transfer problems where the do nan of solution is not complicated. To use this method, first, the governing equations should be conv. ted (discretized) to algebraic form using the Taylor series (for example $(\frac{\partial u}{\partial x})_i$ becomes $\frac{u_{i+1}-v_{i-1}}{2\sqrt{x}}$ where index of i stands for the node number in the x direction). Next, the computational domain should be divided into a series of nodes in each coordinate direction. Finally, the linear al, ebraic equations are solved by iterative techniques and the value of desired parameters are obtained at and node. The FDM is easy to use and effective on structured meshes. On the other hand, it is not as he oful an approach for complex flows and geometries [3,4], where it is generally required to discretize the flow field using a body-fitted grid in order to use FDM. For example, Astanina et al. [5] used FDM to simulate the mixed convection of nanofluids in a lid-driven porous cavity. Sheremet al. [6] employed FDM to simulate natural convection of nanofluids in a lid-driven cavity when boundary conditions are as a function of temperature. Astanina et al. [7] studied MHD flow in a square cavity with variable properties of nanofluids using FDM. Using FDM, Ismael et al. [8] investigated the mixed convection of nanofluids in a square cavity where a heater was installed in one of its corners. Alsabery et al. [9] applied FDM to solve the conjugate natural convection in a square cavity where the temperature boundary conditions in top and bottom walls change as a sinu pidal function. Hassan and Harmand [10] used FDM to analysis the flow of nanofluids in a heat pipe under periodic heat load. Figure 2 displays schematic of some problems that have been solve, by 171.

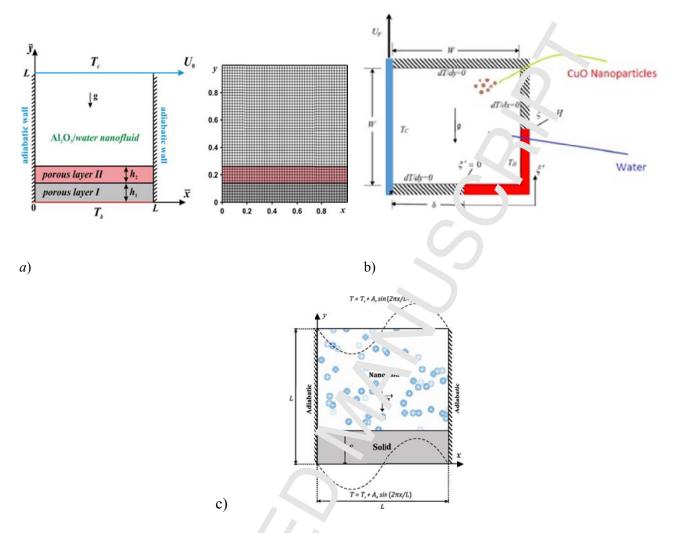


Figure 2. Schematics of some problems in ...l.ch f nite difference method is employed as the CFD technique (a) porous cavity [5], (b) cavity with a heaver at the corner [8], (c) cavity with sinusidoal boundary conditions [9] (figures are reprinted with permission from publisher).

2.1.2. Finite volume method

The finite volume met! od (FVM) was introduced as an alternative to FDM to better handle complex flow domains. A review of the literature shows that FVM is the most common CFD procedure used in solving nanofluid flow problems. In this approach, first the differential equations are converted into integral form. For the approach, after integrating over any volume V, becomes

 $\frac{\partial}{\partial t} \int_{V} u dx + \oint_{\partial V} f_i n_i ds = 0$ where n_i is the unit outward normal and s is the control surface. Next, the

domain of solution is divided into continuous control volumes, and the governing quation is applied to each of them. The values of desired parameters are calculated at the center of with control volume, then at the surfaces of control volumes the parameter values are estimend this ugh interpolation. Finally, for each control volume, the achieved integral terms are conversed to algebraic equations by using quadrature formulae. The finite volume approach is easy to understand because every term has a clear physical description [3,4]. The advantage of FVM is its flexibility for use in complex flows. On the other, one of its main disadvantage is the difficulty of exter line on a method for higher than 2nd order accuracy in 3D modeling.

As mentioned earlier, most numerical studies on nanofluids now used FVM, several examples of which are given in the following. Cho et al. [11] emplor and to model the natural convection of nanofluids in a cavity with wavy walls. Ismael et al. [12] used TVM to simulate the nanofluid flow in a cavity under magnetic field by considering partial slip at the heat flux on sidewalls. Mohammadian et al. [13] numerically simulated conjugate heat transfer of anofluids in a microchannel heat exchanger under the laminar regime. They employed FVM and the single-phase model in their study. Tang et al. [14] employed FVM to model free convection of nanofluids in a cavity with double sinusoidal wavy walls where the Eulerian-Lagrangian technique was applied. Minea and El-Maghlany [15] solved the natural convection of an ionanofluid farrixture of ionic liquids and nanoparticles) inside a square cavity under different sets of bound to conditions. They employed FVM and single-phase homogenous approach model with the proper time of properties in the simulation. In another work, Minea and El-Maghlany [16] employed FVM for modeling of a receiver of a parabolic trough collector. Figure 3 shows the scholartics of abovementioned problems that have employed FVM.

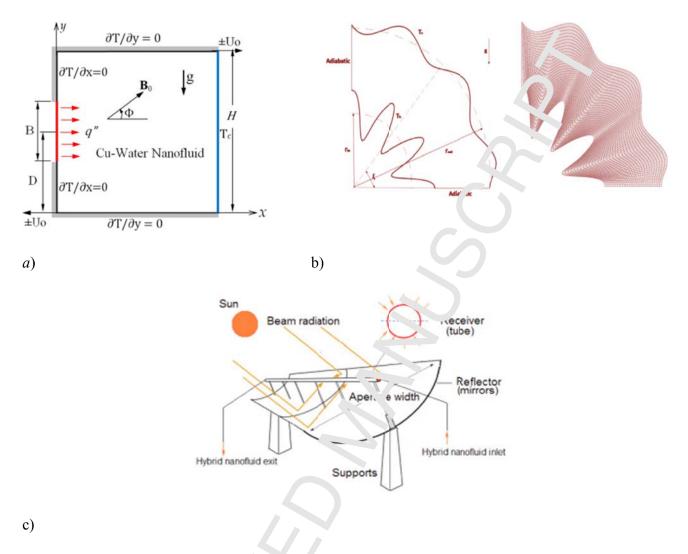


Figure 3. Schematics of some problem, in wn. finite volume method is employed as the CFD technique (a) cavity with a heater under magnetic fiela [21, (b) cavity with double sinusoidal wavy walls [14] (c) parabolic trough collector [16] (figures are r prir ed with permission from publisher).

2.1.2.1 Common FVM b and Soji ware

Two common FV 1 base software packages used for simulation of nanofluid flows are ANSYS FLUENT and ANSYS CFX. For example, Esfahani et al. [17] simulated nanofluid flow in a wavy channel using ANSYS FLUENT and the single-phase approach. Effects of various models for thermophysical properties on the forced convection turbulent flow in a tube was investigated by Minea

[18] where ANSYS FLUENT was used. Minea and Lorenzini [19] employed ANSYS FLUENT to solve natural convection of ZnO/water nanofluid in a cavity by assuming single place homogenous model for nanofluid flow. Minea [20] utilized ANSYS FLUENT to analysis the variations of Brinkman number in a partially heated tube in which Al₂O₃/water nanofluid was used as coolant. Chereches et al. [21] employed ANSYSY FLUENT to simulate the flow of place in one of luid in a circular tube in both laminar and turbulent regimes while the flow was assumed by single-phase. In another study, Kaloudis et al. [22] used ANSYS CFX to model the nanofluid flow in a parabolic trough collector by two-phase approach (Eulerian-Eulerian). Figure 4 shows selematics of the problems considered by [17,22]. Researchers are increasingly using open sources, flware, such as OpenFOAM, which provides a C++ toolbox for solving nanofluid-based problem. The advantage of open-source software is both the reduced cost as well as the ease of adapting and modifying the software for specific problems. For example, Meng et al. [23] utilized OpenFOAM to model nanofluid flow in a square cavity using both single-phase and two-phase approaches.

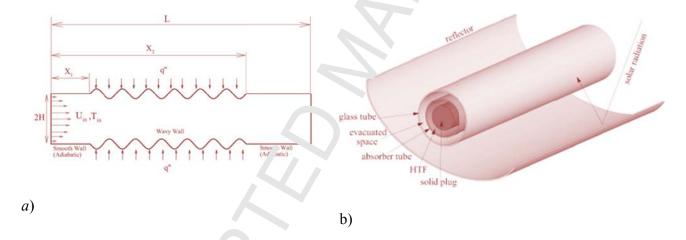


Figure 4. (a) Flow in a wavy charge solved by ANSYS FLUENT[17] (b) flow in a parabolic trough collector solved by ANSYS CFX[22] (figures are reprinted with permission from publisher).

2.1.3. Finite element m anod

In the finite element method (FEM), the domain of solution is divided into a series of finite elements (often unstructured mesnes) and the governing equations are solved as weighted integrals over these elements. Before in egrating the governing equations, each term is multiplied by a weight function, the use of which is one of the main differences between FEM and FVM. The final equations are in the

form of non-linear algebraic equations. The main advantage of FEM is its flexibility for dealing with complicated geometries[3]. One of disadvantages of FEM may be related to round of the cross and error accumulation.

2.1.3.1. Common FEM based Software

Two FEM based software packages that have been used for nanofluid now simulation are COMSOL Multiphysics and FlexPDE, although the former package is more componly used.

For example, Nasrin et al. [24] used COMSOL to model the petramar ce of a photovoltaic thermal (PV/T) system using nanofluids with the single-phase approach. They compared the results of the numerical simulation with experimental data and found good for ement between them. In another work, Bianco et al. [25] investigated thermal efficiency and entry, y generation in a PV/T system using COMSOL where nanofluid flow was considered as a single-phase fluid. Gunjo et al. [26] investigated melting and solidification in a shell-and-tube regenerative type latent heat storage system where the working fluid was a mixture of paraffin and nanopatholes. They used COMSOL for the modeling by considering the temperature-dependent of properties (see Fig. 5 (a)).

Hatami and Jing [27,28] used FlexPDE to value to the performance of direct absorber solar collectors by nanofluids (see Fig. 5 (b)).

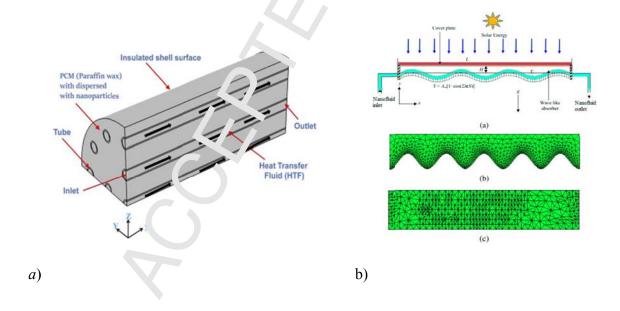


Figure 5. (a) Flow in a shell and tube regenerative type latent heat storage system solved by COMSOL Multiphysics [26] (b) analysis of a direct solar absorption collector by FlexPDE [27] (figures are reprinted with permission from publisher).

2.1.4. Other macroscale based techniques

There are some other macro scale based techniques that have been used a solve nanofluid flows which are briefly reviewed here.

2.1.4.1. Control Volume Finite Element Method

Control Volume Finite Element Method (CVFEM) is a powerful STD technique to solve fluid flows in complex geometries. Indeed, CVFEM is a combination CTLIM and FVM so that it has the benefits of these two techniques in itself [29]. Sheikholeslami is a pioneer researcher in the use of CVFEM to solve nanofluid problems (for example see [30–36]). Sneikholeslami and his collogues have used CVFEM to solve flow and heat transfer of nanofluid. In complex geometries by both the single-phase and two-phase approaches. For example, Sheikholeslami and Ganji [35] considered the geometry shown in Fig. 6(a) and investigated the effect of electric field on nanofluid flow in the presence of porous media and radiation. In another work, Sheikholeslami [37] simulated the effect of magnetic field on natural convection inside a prious curved cavity by CVFEM (schematic is shown in Fig. 6 (b)).

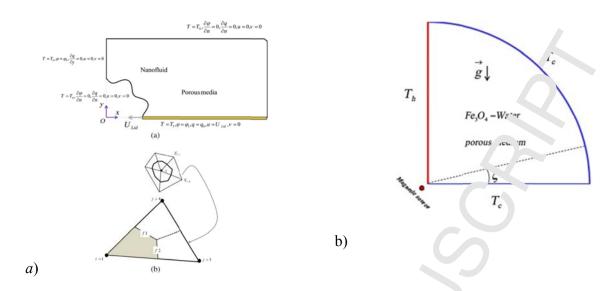


Figure 6. Schematics of problems solved by CVFEM (a) Porous rectangle ar enclosure [35] (b) Porous curved cavity [37] (figures are reprinted with permission from publisher).

2.1.4.2. Boundary Element Method

The term "boundary element method" (BEM) is used to describe a numerical approach that uses a Green's function formulation to convert a 3D partial differential equation to an integral equation over a surface, typically the bounding surface of r body "mmersed in the flow field (typically called the 'boundary integral equation' [38]. This boundary integral equation can then be discretized to obtain a matrix system. When applicable, BEM entails very significant reduction of computation time since it is necessary only to solve for the vartie of the unknown variables on the bounding surface, rather than throughout the domain. For example, Oğlakkaya and Bozkaya [39] employed BEM to solve natural convection of water-based nanafluids inside an inclined semi-annulus cavity under a magnetic field by considering nanofluids as a single-phase working fluid (See Fig. 7 (a)). Applicability of BEM, however, is limited to problem for which a Greens function solution exists.

2.1.4.3. Spectral Method

The spectral method is a global approach (unlike FDM) that is based on expansion of the dependent variables in eigentenction expansions, which must be selected to be compatible with the differential equation, the boundary conditions and the coordinate system used for numerical solution. In a spectral

method, the value of a parameter at each point is obtained by inversion of the eigenfunction expansions, and so it depends on information obtained from the whole computational domain and not only neighboring nodes. When applicable to a given problem, spectral method as the extremely fast, easy to formulate and exhibit exponential accuracy, which provides convergence dister than any other numerical method with algebraic accuracy [40]. Due to the restrictions on existence of the eigenfunction expansion, however, spectral methods are limited to very simple geometries, such as channel flow between infinite flat walls or flow in a triply periodic quare. A few studies have used spectral methods to solve nanofluid problems. For example, Wakif et all fulfill atilized a spectral method to study the effect of a magnetic field on the onset of convection of the object of the plates where the space between the two plates was saturated with popular media (see Fig. 7 (b)). The authors have used the Buongiorno model in their study.

2.1.4.4. Meshless methods

To use common CFD techniques such as FDM, FVM, and FEM, a mesh must first be generated, which can sometimes be a challenge. To solve the proposed are scattered throughout the solution domain [42,43]. The most common meshless methods are [43]:

- Meshfree local Petrov-Galerkin
- Finite point methods
- Radial basis function approached
- Meshfree boundary schemes

In comparison with a standard FLM, a reshless approach is easier to use for modeling 3D problems and can have higher accuracy On the other hand, the computational cost of a meshless approach is often greater than a standard £EM [12].

As an alternative, Lagrangian solvers are another example of meshless methods where no mesh is used in the solution. Generally, a set number of fluid molecules are distributed randomly in the flow domain. For example, in Molecular Dynamics (MD) and Dissipative Particle Dynamics (DPD), the motion of these molecules is governed by Newton's second law of motion where a set of forces are acting on the fluor and locales [44,45]. In MD, the forces between the molecules are calculated by using the inter-particle potentials, such as the Lennard-Jones potential. In the DPD approach, the forces consist of friction forces, conservative forces, and random forces. Based on knowledge of the forces

acting on molecules, the acceleration, velocity, and position of the particles can be calculated. This allows statistical averaging to be implemented to calculate the bulk properties of the new domain such as density, viscosity, mass diffusivity, velocity, pressure, stream function, and vo. icity. For thermal transport problems, the first law of Thermodynamics is applied to the fluid more, the which can then be solved for the molecules temperature in the flow domain. Similarly, the burk properties such as thermal conductivity, thermal diffusivity, internal energy, and enthalpy of the flow domain can be calculated using statistical averaging [46]. Another Lagrangiar method is Smooth Particle Hydrodynamics (SPH) [47], which is also a meshless method. 1. this method, the continuum conservation laws governing the flow, i.e., Navier-Stokes equation, re transformed from partial differential form into integral using an interpolation function that calculate the kernel of the flow variables at any given point. The main difference between SPH ar 1 MD methods is that the interparticle forces in SPH are derived from the continuum conse, ration laws, as opposed to using interparticle potentials in MD [48,49]. The SPH is appropriate for studying large discontinuities in the flow and has the advantage that bulk fluid properties are an inpute the solution (unlike MD, where they are outputs). However, its application to mimic me, cale and nanoscale applications is not as well established as MD. Other meshless methods 2rd the discrete element method [49] and the Smooth Dissipative Particle Dynamics (SDPD) [50]. The SDPD was introduced to combine the advantages of both DPD and SPH, where it retains the thermal fluctuation features found in DPD and has the flexibility in discretizing the Navier-Stokes (N-3) equation governing of the system using the SPH approximations [50].

In the literature, there are a limited number of papers on nanofluids that have employed meshless methods. For instance, Nikfar and Mahmoodi [51] used the meshless local Petrov–Galerkin approach to solve natural convection in a phase cavity filled with alumina/water nanofluid. Figure 7 (c) shows the domain, boundary conditions and nodes distribution in the problem considered by Nikfar and Mahmoodi [51]—as can be seen, there is no connection between grids. Ooi and Popov [52] studied the effect of shape of Cuna poparticles suspended in water in terms of natural convection heat transfer in a cavity utilizing a radial basis integral equation method. Bourantas et al. [53] employed a meshless approach (combination of point collocation method with the moving least squares approximation) to solve the natural convection of nanofluids in a porous cavity.

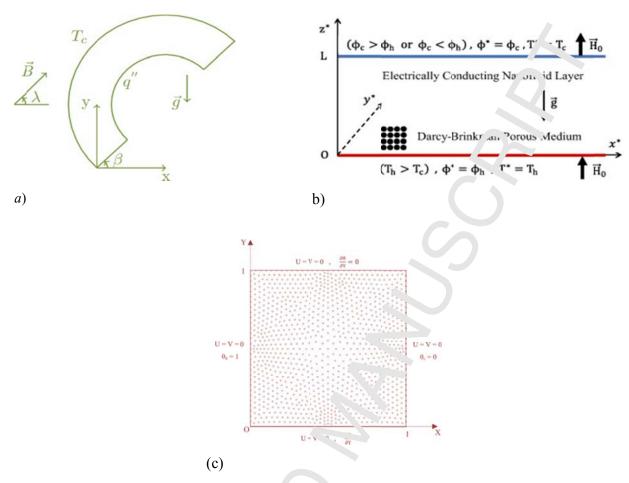


Figure 7. (a) Natural convection in an inclir d semi unnulus cavity solved by boundary element method [39] (b) Flow between two infinite plates solved by special method [41] (c) Domain, boundary conditions, and node distribution for the problem considered in N.kfar and Mahmoodi [51] (figures are reprinted with permission from publisher).

2.2. Mesoscale based techriqu's

Mesoscale techniques a tempt to simulate systems at a scale in-between molecular scale and the macroscopic scale. The is tice Boltzmann method and the dissipative particle dynamics method are the main mesoscale technique. that are used to simulate the nanofluid flows. Both of these methods are based on solution of a dynamical system that can be shown to converge to the Navier-Stokes equations in a certain limit.

2.2.1. Lattice Boltzmann method

The lattice Boltzmann method (LBM) was first introduced in the 1980s. The application of this method in simulating heat and mass transfer of fluids, especially in complex geometries and multicomponent flows, has increased in intervening years due to its enfectiveness, flexibility and simplicity in comparison to the traditional computational fluid dynamics in thods. The fundamental idea of LBM is based on the discrete movement theory of a set of a tificial fluid particles' placed on lattices. The motion of these fluid particles is simulated by following the evolution of a prescribed Boltzmann equation. The most essential advantage of the LBM is the incorporation of microscopic physical interactions of the fluid particles in the numerical sundation and reveal the mesoscale mechanism of hydrodynamics. Taking the Boltzmann equation into consideration, the density distribution function $f(x,\zeta,t)$ is introduced to represent a doma y number of the particles with the microscopic velocity ζ at the position x and the time t and the particles distribution can be expressed as $f(x,\zeta,t)$ [54]. The most common models used for 3D sundations are the D3Q19 and D3Q41 lattices, providing 4^{th} and 8^{th} order isotropy in three dimensions are respectively, which is illustrated in Fig. 8 [55]. The standard notation DnQm for m discrete resoccious in n spatial dimensions is used throughout.

In order to simulate the nanofluid flow by the LBM, the dynamic parameters affecting the nanofluid flow behavior should be analyzed from the meroscopic point of view due to various forces on the nanoparticles. Sidik and Razali [56] provined concise review of research studies on the use of LBM for analyzing the convective heat transfer of nanofluids. In another study, Sidik and Mamat [57] summarized recent advances of LBM in estimating the hydrodynamic and thermal behavior of nanofluids and discuss several challenging problems that have been encountered in this issue. Kalteh and Hasani [58] studied the nanofluid free convection in an L-shaped cavity using LBM and the influences of nanoparticle convents ation and diameter as well as Rayleigh number on the temperature and flow fields were evaluated. Mliki et al. [59] applied LBM to evaluate the MHD natural convection of nanofluid in an incline. Conaped cavity and the impact of relevant parameters on the hydrothermal characteristics of the nanofluid was investigated. Zhou et al. [60] developed a 3D LBM model to analyze the mixed convection heat transfer and flow dynamics of alumina nanofluid in a cubic cavity under magnetic 1 al. Mohebbi et al. [61] employed LBM to simulate the forced convection of TiO2/water, Al₂O₃/water, and CuO/water nanofluids in an extended surfaces channel. Ghasemi and

Siavashi [62] studied the first and second laws of thermodynamics for natural convection of nanofluids (Cu/water) in a porous cavity employing LBM.

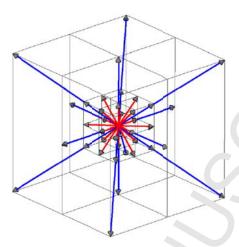


Figure 8. 4th order isotropic 19 velocities lattice (red arrows) and of order isotropic 41 velocities lattice (red and blue arrows) [55] (figure is reprinted with permission from publisher).

2.2.2. Dissipative particle dynamics method

The continuum Navier-Stokes equations (NSE) are generally used to study energy transport in micro/nanoscale heat transfer applications such as in anofluids. The major concern-particularly with nanoparticle aerosols-is whether the scale of nanoscale should be simulated or if the continuum assumption is still applicable. This issue can be resolved by comparing the mean free path of the base fluid to the scale of the problem under nor order ation. For aerosol systems for which mean free path is of order of tens of nm (e.g. the mean free path of air is 60nm) the no-slip assumption may begin to break down, even for microscale systems. A similar breakdown of the continuum assumptions can occur in liquid nanofluid systems for problems involving length scales on the order of about 10nm or less.

The most familiar approal in among discrete particle simulation methods is molecular dynamics (MD), where the procest starts from tracking individual atoms of the fluid and calculating their velocities, accelerations and forces. From these microscopic details, further bulk properties such as temperature, pressure viso osity, density, mass diffusivity, and flow rates can be recovered using statistical sampling. Such analysis gives comprehensive data about microscopic details of the simulated system. However, the primary drawback of this method is the extremely small physical and time scales, which are not appropriate for tracking larger temporal and spatial scales that occur in the

bulk heat transfer applications. In general, the MD method is computationally expensive and time consuming, even for cutting-edge supercomputers. The time and spatial scales of the most transfer at the nanoscale are larger than MD, yet smaller than the conventional continuum has scales. Thus, intermediate spatial and temporal scales must be captured. These scales can be captured using mesoscopic particle-based methods, so-called "coarse-graining" methods, volume each simulated particle represents a group of actual fluid molecules. These methods possume the unique capacity to model relatively bulk physical systems and efficiently capture the essential details of the pertinent interactions within fluid molecules. A relatively recent coarse-grained archail and this type is the dissipative particle dynamics (DPD) method.

The dissipative particle dynamics (DPD) method is a coarse-trained version of MD where each DPD particle represents a group or packet of actual moleculas [62]. The DPD particles are randomly distributed in the flow domain, and particle interaction obegones. Levation of mass, momentum and energy, as is shown Fig. 9. The figure shows a schematic for the fluid particles and wall particles where each particle represents a group of fluid moleculary fluid particles and wall particles where each particle represents a group of fluid moleculary for drive the flow in the domain, a body forces is used and a periodic boundary condition is applied at the domain inlet and outlet to guarantee mass conservation. Further, a bounce back boundary condition is applied at the walls to produce the no-slip boundary condition. The DPD method can predict complex hydrodynamics at micro/nanoscale with a much higher computational efficiently than raditional MD [63]. During recent years the method was applied to several heat transfer applications, including conduction [64,65] and convective heat transfer applications for pure fluids and in turn convection [66–68], and heat transfer with temperature-dependent properties '05].

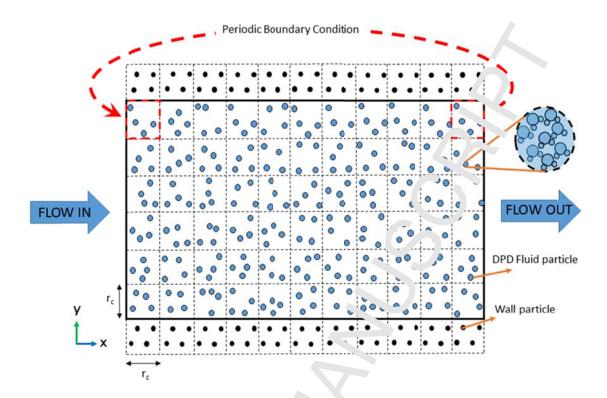


Figure 9. Schematic for DPD domain showing fluid and wall particles with appropriate boundary anditions

Recently, Abu-Nada [70,71] advanced the DPD approach to model heat transport within nanofluids. The method was able to mimic energy transfer mechanisms by studying thermal fluctuations induced by Brownian motion. Also, the method investigated the inter-particle energy transport between neighboring fluid particles [69]. The results indicated that the DPD method is well suited for nano/microscale applications, and it can be further extended to other practical heat transfer applications.

In nanofluid heat transport applications, the most influential properties are the thermal conductivity and viscosity. To unders and the heat transfer mechanism that takes place microscopically within nanofluids using D'D, there two properties must be linked to the microscopic interactions between DPD particles. Abu-1011 [70,71] described the linkage procedure between nanofluid's bulk viscosity and the microscopic interaction between DPD particles. He also described the linkage of nanofluids's bulk thermal conductivity and the microscopic heat conduction fluxes occurring between

DPD particles. In other words, he transformed the macroscopic bulk values of viscosity and thermal conductivity into microscopic particle-particle force and heat flux interactions between interacting DPD particles.

The interaction between DPD particles, shown in Fig. 9, is governed by the following equations:

$$\frac{d\vec{r_i}}{dt} = \vec{v_i} \tag{1}$$

$$\frac{d\vec{v}_i}{dt} = \left(\vec{f}_{ij}^{C} + \vec{f}_{ij}^{D} + \vec{f}_{ij}^{R}\right) + f_{ext}$$
(2)

$$mC_{v} \frac{dT_{i}}{dt} = \left(q_{ij}^{\text{visc}} + q_{ij}^{\text{cond}} + q_{ij}^{R}\right)$$
(3)

where the conservative force \vec{f}_{ij}^C , dissipative force \vec{f}_{ij}^D and and one force \vec{f}_{ij}^R are given in [70]. Also, f_{ext} accounts for any external force applied to the DPD parameters such as body force, pressure gradient, etc. The terms, q_{ij}^{cond} , q_{ij}^{visc} , q_{ij}^R are conductive, viscous an analom heat fluxes, respectively, as given in [70]. The conservative interaction between the Driv particles, which regulates the potential energy between the particles, is determined from the standard on of the DPD system. Also, the strength of dissipative and random forces within the system of DPD follows the fluctuation-dissipation theorem to warranty conservation of the total momentum in system [70].

Generally, weighting functions are used in the conservative and dissipative forces where they decline monotonically with the inter-particle servative distance, becoming zero at a critical cut-off radius. The DPD conservative forces have a fine repulsive nature-one which does not account for attraction between DPD particles. The more emmonly used weighting function for the conservative force is the Groot and Warren soft repulsion of odel [63]:

$$w(r_{j}) = \begin{pmatrix} -r_{ij} \\ r_{c} \end{pmatrix} \qquad (r_{ij} < r_{c})$$

$$(r_{ij} \ge r_{c}). \qquad (4)$$

As for the dissipative and random forces weighting functions, Fan's et al. [72] generalized weighting function (which is one of the most famous models) has proven accurate for high viscosity fluids which mimic high Sch. number mass transport applications and high Prandtl number thermal applications. Fan's nodel is given as [72]:

$$w^{D}(r_{ij}) = (w^{R}(r_{ij}))^{2} = \begin{cases} \left(1 - \frac{r_{ij}}{r_{c}}\right)^{S}, & (r_{ij} < r_{c}) \\ 0, & (r_{ij} > r_{c}) \end{cases}$$
(5)

This weighting function can mimic greater DPD viscosity by either raising the exponent, S, or by modifying the value of r_c as cut-off radius. This weighting function plays a λ v role in mimicking thermal transport in water where $S = \frac{1}{2}$ and $r_c = 1.1$ [73].

The incorporation of experimental data for the bulk nanofluid viscosity in the DPD model can be done by updating the dissipative force as proposed by Abu-Nac'a [70,71]. Abu-Nada's technique improves Fan's et al. [72] weighting function to account for the nanofluid's viscosity variation with the domain's concentration and temperature. Abu-Nada proposed the following analogy [70,71]:

$$\frac{\Omega^{D}(T,\varphi,r_{ij})}{w^{D}(r_{ij})} = \frac{\mu(T,\varphi)}{\mu_{C}}$$
(6)

Where $\mu(T,\phi)$ is the experimentally measured viscosity is a function of nanoparticles concentration and the local temperature of the nanofluid. Note that the parameter, $\Omega^D(T,r_{ij})$, is a modified weighting function and the parameter, $w^D(r_{ij})$ is weighting function [72], while μ_C is the pure fluid viscosity. Consequently, dissipative and random forces can be obtained by:

$$\vec{f}_{ij}^{D}(T,\varphi) = \sum_{j} - \sum_{ij} \Omega^{D}(T,\varphi,r_{ij}) (\vec{e}_{ij} \cdot \vec{v}_{ij}) \vec{e}_{ij}$$

$$(7)$$

$$\vec{f}_{ij}^{R}(T \mid \rho) = \sum_{i \neq i} \sigma_{ij} \Omega^{R}(T, \varphi, r_{ij}) \zeta_{ij} \Delta t^{-1/2} \vec{e}_{ij}$$
(8)

The incorporation of the bulk thermal conductivity of experimentally collected data for a given nanofluid can be included by dap and the conductive heat fluxes. Thus, the typical DPD conductive heat flux model can be asscribed as [73]:

$$q_{ij}^{cond} = \sum_{j \neq i} \kappa_{ij} \ w^2(r_{ij}) \left(\frac{1}{T_i} - \frac{1}{T_j}\right)$$

$$\tag{9}$$

The revised value of the least flux is achieved by alteration of the κ_{ij} parameter, given in the former relation. This parameter is calculated as [70,71]:

$$\kappa_{ij} = \frac{C_v^2 \mathbf{K} (T, \varphi) (T_i + T_j)^2}{4k_R}$$
(10)

in which $K(T, \varphi)$ is a modified heat friction function. In the typical DPD constant properties formulation, a constant value (k_o) , called heat fraction, is used instead of $K(T, \varphi)$. The amount of heat fraction (k_o) is usually estimated by tuning until it matches the value of the all diffusivity. Here it is assumed that the function $K(T, \varphi)$ changes with domain's temperature and nonfluid concentration and, consequently, a relationship was suggested as:

$$K(T,\varphi) = k_o k(T,\varphi) \tag{11}$$

where $k(T, \varphi)$ is experimental measured bulk thermal conductivity C^{ϵ} nanofluid. Using this function, the final set of equation for the DPD heat fluxes are given by the following:

$$q_{ij}^{\text{cond}} = \sum_{j \neq i} \kappa_{ij} w^2(r_{ij}) \left(\frac{1}{T} - \frac{1}{T_i} \right)$$
(12)

$$q_{ij}^{visc}(T) = \sum_{j \neq i} \frac{1}{2C_{v}} \left(\Omega^{D}(T, \varphi, r_{ij}) \left[\gamma_{ij} \left(\vec{e}_{ij} \cdot \vec{v}_{ij} \right) - \frac{c^{2}}{m} \right] - \sigma_{ij} \Omega^{R}(T, \varphi, r_{ij}) \left(\vec{e}_{ij} \cdot \vec{v}_{ij} \right) \zeta_{ij} \right)$$

$$(13)$$

$$q_{ij}^{R}(T) = \sum_{j \neq i} \alpha_{ij}(T, \varphi) \Omega^{\Lambda}(T, \varphi, r_{ij}) \Delta t^{-1/2} \zeta_{ij}^{e}$$
(14)

The relation between parameters γ_{ij} an σ_{ij} s as [73]:

$$\nu_{ii} = \frac{\sigma_{ij}^2 \left(T_i + T_j \right)}{4k_{\scriptscriptstyle B} T_i T_i} \tag{15}$$

Finally, the factor in the rando. The it flux can be expressed as:

$$\alpha_{ij} = \sqrt{2k_B \kappa_{ij}} \tag{16}$$

where k_B is the Boltzma in contant.

2.3. Microscale ba. ed tec iniques (Molecular dynamic simulation)

The fluid flow 1 usually solved for nanofluids using the continuum theory, which involves the hypothesis of continuum medium. A mentioned in the previous section, the continuum approximation

can begin to break down for problems at the smaller end of the nanometer size range (e.g. flow around carbon nanotubes, etc.) due to comparable characteristic dimensions of the fluid con and space and the molecular free path. In this regard, methods to directly solve for the fluid motion at the molecular scale were introduced. The molecular dynamic simulation (MDS) method was first introduced by Alder and Wainwright at the end of 1950. In this method, the molecules and atoms are regarded as 'fluid particles' whose dynamic and interactions are computed over a time portion. The period of time for the calculation is defined according to the time needed to reac's a dynamic evolution between system components. MDS solves a system of interacting particles using the Newton's equations of motion and specifies the trajectories of molecules and atoms. In a function, molecular mechanics or interatomic potential force fields are used to calculated forces between the particles and their potential energies.

Recent advance and progress in nanofluidics has made MDS a promising simulation approach in this field for problems on appropriately small length and time scales. A schematic of a water-based nanofluid containing carbon nanotubes is given in Fig. 10 [7.1]. The MDS method is known as a viable method to investigate the flow physics in na. Small problems since it is able to properly determine the molecular structure of the fluid and surfaces, and to predict the atomistic interactions. Jabbari et al. [75] and Lee et al. [76] quantitatively received recent advances of MDS in nanofluidic systems, including enhancements in measurement of nanofluid thermophysical properties, thermal wall modeling, the cut-off radius, and initial conditions, etc. These review papers provided very critical discoveries and proposed important are is needed to be taken into consideration in future research, and thus the reader is recommended to refer to these articles for further detailed information on this matter. The MDS method was here to used in various investigations on nanofluids. It is used for measuring the viscosity and the rma conductivity of nanofluid at different temperatures and using different particle sizes [77], investing heat transfer characteristics of nanofluid [78] and their surface nanostructures [79], Poiseum floy of a nanofluid [80], chaotic movements of nanoparticles [81], etc. According to Wei et al. [77], a olecular motion without temperature gradient are found to be responsible for heat transitaring the area of low viscous heat using a non-equilibrium MDS. Toghraie et al. [80] used MDS o simu ate the Poiseuille flow of nanofluids containing platinum and copper particles and were able to successfully employ the Large-scale Atomic/Molecular Massively Parallel Simulator (LAMN, 'S) code for this purpose. In this method, the Lennard–Jones potential governs the atomic interaction. Table 1 summarizes some advantages and limitations of different CFD approaches.

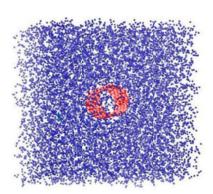


Figure 10. Nanofluid molecular dynamic model: Carbon nanotube nan 'parti-12 (red-colored) and surrounding water (blue-colored) [74] (figure is reprinted with permission 'com publisher).

Table 1 advantages and limitations of different CFD approaches

Method	Advantages	V mitations
Finite Volume	 Simplicity. Relatively small convergence time Numerical evaluation of the difference equation is simple Simple code structures Intuitive and easy to implement for simple problems Complexes geometries can be considered [83] Neumann B.C can be easily established. Suitable for Unstructured Grids Governing equations are written as integral form 	- In large scale problems small time steps are necesed [82] Compared to FEM needs high number of grids to give good output Difficult to employ for complicated fructures - Irr gular geometries require far more effort than FEM
Finite Element	 Very general method and used for solving a variety of problems The stiffness matrix and the load vector and be computed for each element. Allowing attention to be confined to a single typical element [82]. Spatial variation of properties can be handled with relative ease. Irregular regions can be 1. Adelled with greater accuracy. Suitability for non-linear quadions. High flexibility in changing dement sizes Mixed-boundary- the problems are easier to handle [84]. Any shaped ge and ry can be modelled with 	 Equations are much more mathematically complex. Numerically intensive and can take more CPU time and memory storage space [84]. More mathematics involved - less physical significance Complex code structures
Boundary Element	the same effort Less data is required to run a program efficiently 85? Small system of quations, discretization takes place only on the surface of body Well-stited to problems with open domains [85]. God agreement between BEM and FEM Mondafficient in modelling due to the real tion of dimensions. Advantageous in the case of problems with infinite or semi-infinite domains Less data preparation time	 Programming complexity BEM is not successfully applied to non-linear fluid flow problems. Matrices are asymmetric, dense and not easy to solve[85]. Solution time is long and memory size is large. Poor for thin structures In non-linear problems, the interior must be modelled

Lattice Boltzmann

- The method is scalable, stable and suitable for parallel computing
- Suitable for complicated geometries.
- Suitable for multiphase flows calculations
- Suitable for mesoscale applications such as colloids and flow in small pores encountered in porous media.
- Suitable for applying microscopic interactions between fluid molecules.
- Modeling vari' ble thermo-physical properties (sight as viscosity and thermal conductivity) is not straightfo wa d.
- The method's limited to uniform grid where the modeling of very fine grading is encountered at boundaries required in treatment which makes the inchod computationally demanding, examples in shear layers and in boundary layers.
- bu!!. viscosity is not a direct input ρa. ameter to the method, but it is re'ated to the relaxation time of the method
- Axisymmetric flows implementations are not straightforward.
- Multiphase flows with large variation in density is problematic

Dissipative Particle Dynamics

- Grid less method with a Lagrangia (atua)
- Brownian motion is intrinsic in the termulation of the method
- Suitable for complicated geometries
- Suitable for microfluidics ρ_{PP} : ations as it contains thermal fluctuations
- A coarse-grained partic'e mc. o suitable for spatial and temporal scale that are larger than the molecular dynamic cales and much smaller than the continuum based models (i.e., Navier-Stokes)
- Suitable for sus sion flows and colloids
- Suitable for multir hase flows
- Straightforv ard examsion from twodimension, to aree dimensions
- Suitable for iter particle interactions at micros opic level by including attraction and repuls on forces between fluid molecules and the surrounding media.

- There is no direct connection between DPD parameters and the physical parameters of the system under simulation (i.e., thermophysical properties are not input parameters)
- Computationally demanding when compared with finite difference and finite volumes.

3. Three dimensional computational modeling of nanofluid flows

The following review of 3D numerical studies of nanofluid flow and heat trans arised divided into three main sections. The first section deals with simulation of natural convection flow of nanofluids where the buoyancy effect is considered. In the second part, forced convection studies are reviewed. In the third, part mixed convection flows of nanofluids are discussed.

3.1. Natural convection of nanofluid flow

For natural convection problems, the buoyancy force is added to the momentum equation which couples the momentum and energy equations. Many studies have been done to analyze natural convection in enclosures because of its importance in solar collectors, thermal energy storage systems, electronics equipment, and buildings [86]. The physical parameters affecting the 2D and 3D modeling results as well as the influence of different CFD technique on the accuracy of results are compared. Next, the effects of using different nanofluids, bour conditions, and even some external fields are reviewed from the literature on nanofluid natural convection.

3.1.1. Two dimensional versus three dimensional modeling

Obviously, it is tempting to find cases or 'hic' 2D simulation can provide accurate results since these are less computationally expensive than tu.'. 3D simulations (for the same resolution). Even for 3D simulations, several simplifications are 'ypically made (including limiting the domain) to obtain a tractable model of reasonable cost. Along these lines, several studies have been done to investigate the agreement between 2D and 'D simulations. These types of studies show that the results of 2D and 3D modeling can be quite different cepending on the range of physical parameters employed, such as Rayleigh number, nane particle volume fraction, and size of the thermal system (aspect ratio). For example, Boutra et al. [271 cpplied LBM coupled with FDM to solve the three dimensional natural convection flow of Ag/wa er nanofluids (with volume fractions up to 10%) in an inclined cube cavity with differentically heated side walls. In this simulation, Maxwell and Brinkman models were implemented to calculate the thermal conductivity and viscosity of nanofluids, respectively. Their findings revealed that at low Rayleigh numbers (i.e. 10³) the average Nusselt number can be estimated

via 2D modeling with high accuracy; however, with increasing Rayleigh number, the 2D model overestimated the average Nusselt number compared to a 3D simulation. More we, the difference between 2D and 3D results increased with the increment of nanofluid concentration (See Fig. 11).

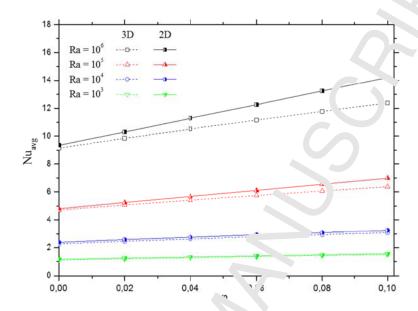


Figure 11. Comparison between 2D and 3D model. Figure 11. Comparison between 2D and 3D model. Figure 12. For average Nusselt number at various Rayleigh numbers and nanofluid concentrations [87] (figure is reprinted with permission from publisher).

In another study, Ravnik and Škerget [88]. Alved a atural convection of nanofluids in a cube cavity where a hot cylindrical body was installed at its center while front and back surfaces of cavity were insulated, and other sides were kept at low temperature (i.e. cold walls). The cross section of this body varied from circular to elliptical. Three types of water -based nanofluids containing Al₂O₃, Cu, and TiO₂ nanoparticles with volume tractions of 10 and 20% were considered in the analysis where the Rayleigh number varies between and 10⁶. They used a boundary element method to simulate the flow of nanofluids. In addition, the Maxwell and Brinkman models were implemented to estimate the thermal conductivity and viscosity of nanofluids, respectively. Comparison between 2D and 3D simulations reveals that with ir creasing the Rayleigh number, the difference between 2D and 3D results increased, and in gineral the estimated heat transfer rate by 3D modeling is lower than that of 2D. However, it was an auded that the difference between 2D and 3D results is not significant, so apply 2D modeling a vas suggested to be suitable for similar problems.

In another study, Sheremet et al. [89] used FDM to simulate free convention of nancfluids in a porous cavity with partially heated sidewalls. They implemented the Buongiorno model (discussed above) in which Brownian motion and the effect of thermophoresis have been included. The results were presented for various parameters including Rayleigh and Lewis numbers as well as buoyancy-ratio, Brownian motion, thermophoresis, and aspect ratio parameters. They concluded that as the aspect ratio increases the difference between 2D and 3D results for average Number on a hot wall decreases. In the limit, the difference tends to zero for aspect ratio $s \ge 2$ (See Fig. 12). They also emphasized that considering the non-homogenous distribution of nancipartic es leads to more accurate predictions of flow and heat transfer characteristics in the cavity.

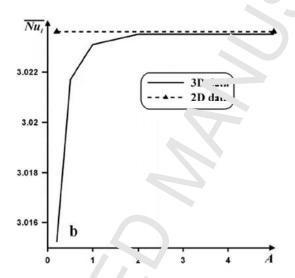


Figure 12. Comparison between 2D at d 3D r, alts for variation of average Nusselt number with aspect ratio for Le = 1, Nr = Nb = Nt = 0.1 [89] (rigure is reprinted with permission from publisher).

3.1.2. What role does the CFL te innique play on the modeling results?

There are not enough comparative studies that investigate the effect of both the CFD technique and 3D simulation on the accuracy of results. To date, only one paper was published in this regard in the literature. Saghir (α al. [70] investigated the natural convection of Al₂O₃/water nanofluids (with volume fractions up α 30/3) in a cubic cavity where the sidewalls were differentially heated. They used the Ho et al. [51] correlations for thermal conductivity and viscosity. For the simulations, they implemented three well-known approaches including FDM, FEM, and LBM. The results of simulations were compared against experimental data for volume fraction of 3% at $Ra = 5.6 \times 10^7$

where the temperature difference between sidewalls was 12 °C. As is shown in Fig. 13, in the case of 2D simulation, FEM was more accurate than FDM and LBM. Moreover, the companient of 2D and 3D results for finite element technique reveals that the results of 2D modeling are 10. Fr to experimental data.

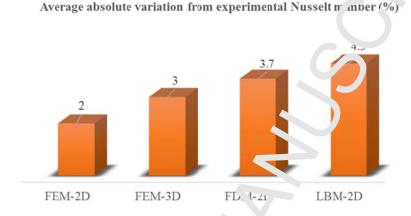


Figure 13. Comparison between the results of different numerical models for volume fraction of 3% at $Ra = 5.0 \times 10^{190}$].

From just one study it is hard to conclude which CFD technique is better, so more studies should be done to discover this issue.

3.1.3. What is the effect of nanofluid type on the heat transfer rate?

The effective thermal cor.duc.ivity and viscosity of nanofluids strongly depend on the type of nanoparticles and base fluid. Using nanoparticles with higher thermal conductivity increases the effective thermal conductivity of nanofluids. To date, two studies have dealt with the effect of nanofluid type on ratural convection. In both studies the Brinkman model [92] was used to calculate the effective viscosity so shanging the type of nanoparticle has no effect on the effective viscosity. Of course, other p. ppeness including density, thermal expansion coefficient, and viscosity vary by changing the kind of nanoparticles.

In this regard, Purusothaman et al. [93] solved the natural convection of nanofluids in a cavity, which its schematic has been shown in Fig. 14, using single-phase approach and FVM. They presented the results for Rayleigh number in the range 10⁵-10⁷, cavity aspect ratio between ¹ and 7.5, nanoparticle volume fractions up to 10%, and for two different nanofluids including Cu/waller and Al₂O₃/water. They concluded that Cu/water nanofluid is more effective than Al₂O₃ ater ^cor cooling of hot elements installed on the enclosure wall; one reason behind the beginning performance of Cu/water nanofluid could be its higher effective thermal conductivity. They utilized the Maxwell and Brinkman models to calculate the thermal conductivity and viscosity of nano ruids, respectively.

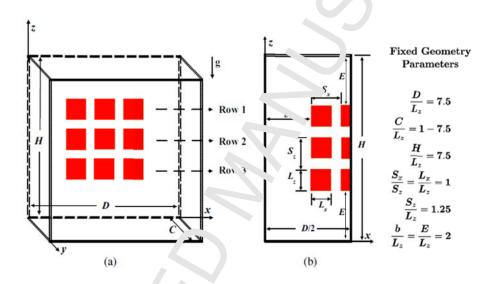


Figure 14. Physical configuration and general configuration and genera

Snoussi et al. [94] studied the stea y state free convection of two water-based nanofluids containing Al₂O₃ and Ag nanoparticle; (w₁C's maximum volume fraction up to 8%) in a cube cavity with differentially heated sidew. Its They used FLUENT software (based on FVM) to simulate the natural convection flow while Maxwell and Brinkman equations were utilized to estimate the thermal conductivity and viscos. V of r anofluids, respectively. They found that particle loading diminishes the heat transfer rate at d the reduction was highlighted when the convection mode is the dominant regime of heat transfer. In all it on, the results revealed that Ag nanoparticles provide higher heat transfer rates.

3.1.4. What is the effect of a magnetic field applied to natural convection nanoflyid flow?

Magnetic fields are utilized in many engineering applications (e.g. micropur ps, electronic devices, and nuclear reactors). Therefore, nanofluids should also be studied with respect to MED flow, to see if there is any additional effect on heat transfer characteristics of thermal system 5 [95–99]. From the 3D studies on MHD flow effect on natural convection of nanofluids, it seen that with increasing Hartmann number (a dimensionless number that indicates the ratio of magnet c to vi cus forces), the average Nusselt number reduces. This was attributed to the decrease of fluid relocity induced when MHD flow field acts as a barrier to heat transfer enhancement.

In another study, Sheikholeslami and Ellahi [100] investigated the natural convection flow of Al₂O₃/water nanofluids in a cube cavity under MHD flow where the temperature of bottom surface was higher than that of top surface and other surfaces were adicatic. They used LBM to simulate the problem. To calculate the thermal conductivity and viscosic, Koo–Kleinstreuer–Li (KKL) models were utilized. The results were presented for different volume fractions (up to 4%), Hartmann numbers, and Rayleigh numbers. They concluded that applying magnetic field reduces the magnitude of velocities in the cavity, and, consequently, the masselt number decreases. On the other hand, Nusselt number would be enhanced through particle loading and boosting the buoyancy forces. Figure 15 presents the effects of Rayleigh and Hartmann numbers on average Nusselt number and heat transfer enhancement in the cavity. Heat transfer enhancement parameter is the ratio of heat transfer rate in the case of nanofluid to the case of fluid. As seen heat transfer enhancement index raises with increasing the magnetic field the other hand, as seen heat transfer enhancement index raises with increasing the magnetic field the other hand, as seen heat transfer enhancement index raises with increasing the magnetic field the other hand, as seen heat transfer enhancement index raises with increasing the magnetic field the other hand, as seen heat transfer enhancement index raises with increasing the magnetic field the other hand, and have a second transfer enhancement index raises with increasing the magnetic field the other hand, and have a second transfer enhancement index raises with increasing the magnetic field the other hand.

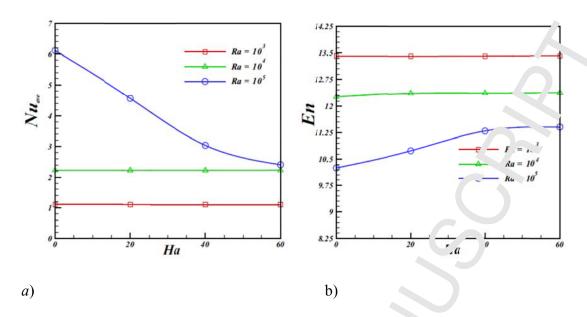


Figure 15. Effects of Rayleigh number and Hartmann number on (a) rage Nusselt number ($\phi = 4\%$) and (b) heat transfer enhancement [100] (figure is reprinted with permission from publisher).

Al-Rashed et al. [101] modeled the effect of the anti- in which an inclined magnetic force applies to a partially heated cavity filled with CNT/water nanofluids. The magnetic source angle with respect to horizontal was measured by α ($0 \le \alpha \le 90^{\circ}$). The modeling was done for Hartmann numbers of 0, 50, and 100, volume fractions up to 5%, and Regleig's numbers between 10^{3} and 10^{5} . The maximum and minimum values of Nu number were obtained for different conditions as shown in Fig. 16. They used Brinkman model for calculating viscosity and Yiue model [102] for estimating the thermal conductivity of CNT/water nanofluids.

In a continuation of the work of [101], Al-Rashed et al. [103] analyzed the second law of thermodynamics for the same protect. They found that the effect of magnetic field inclination on entropy generation is more visi¹ to a^{4} Ra = 10^{5} .

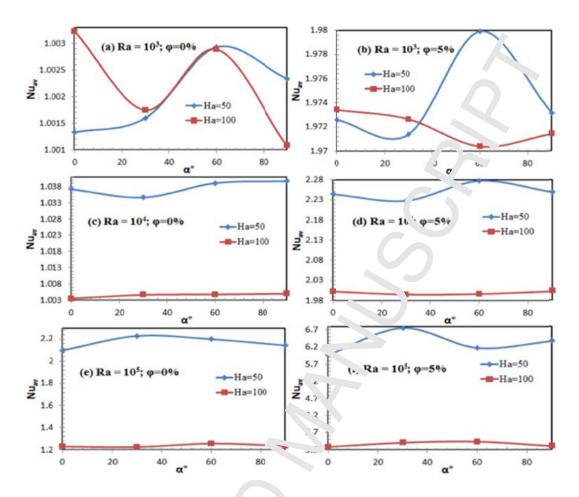


Figure 16. Effect of the angle of magnetic for 'e applie 1 to a partially heated cavity on Nu number[101] (figure is reprinted with permission from publisher).

Kolsi et al. [104] studied the effects of mag etic field, and an inclined fin on natural convection in an open cavity filled with CNTs/water natioallides. The results were presented for different values of Rayleigh number, nanoparticle concentrations up to 5%, Hartmann numbers between 0 and 100, and inclination angles of fin ranging 0 to 360 degrees. It was found that heat transfer rate reduces linearly with increasing the magnetic field intensity. It was also concluded that by adding nanoparticles the heat transfer augments linearly, moreover when the fin is at an angle of 180°, the heat transfer is maximized. The problem was solved with the FVM and a single phase approach.

3.1.5. What is the iffect of cavity configuration on natural convection?

Changing the slope of cavities and heating area as well as using internal fins (or blocks) can affect the heat transfer due to natural convection in cavities. In the following, the effects of new parameters on discussed.

Kolsi et al. [105] simulated heat transfer and entropy generation due to natural convection of Al₂O₃/water nanofluids with volume concentrations up to 15% in a cube cave, by implementing the FVM and single-phase homogenous approach. Solid panels with three different positions were installed at corners of the cavity. They used Maxwell and Brinkmar model to calculate the thermal conductivity and viscosity of nanofluids, respectively. It was found that with increasing nanofluid concentration, the heat transfer rate enhances. Moreover, partical loading into the base fluid is not advantageous from the second law viewpoint. By using the solid parels one can adjust the rate of heat transfer in the cavity.

Kolsi et al. [106] studied transient natural convection next transfer and entropy generation due to Al₂O₃/water nanofluid flow (with volume fractions on a 20%) in a cube cavity with differentially heated walls. The problem was solved via the FVI where the Maxwell and Brinkman relations were used to estimate the thermal conductivity and viscos v of nanofluids, respectively. They concluded that with increases in Rayleigh number and nanofluid concentration both average Nusselt number and entropy generation increase.

Meng and Li [107] simulated the free convection of Al₂O₃/water nanofluids with two volume concentrations of 1 and 4% in a horizonal sylinder where the sizes of length and diameter are the same. The ends of circular cylinder in d a finite temperature difference to create free convection in the cavity. The problem was solved by OpenFOAM (FVM). They found that at a given Rayleigh number, the Nusselt number decreases with the increase of nanofluid concentration. They also observed that when a temperature-dependent solver was used for simulation, the results of water, and nanofluid with a concentration of 1% are closed to experimental data. On the other hand, a temperature-independent solver should be utilized to simulate the results at the concentration of 4% to minimize the deviation from experimental data. Ternik and Rudolf [108] solved the natural convection of non-Newtonian nanofluids (Au nanopartices with volume fractions up to 10% dispersed in carboxy methyl cellulose) in a cube cavit, was differentially heated walls for Rayleigh numbers between 10 and 10⁶. The problem was again solved with the FVM and assuming power law behavior for nanofluids. They found that by loading nanoparticles to the base liquid the onset of natural convection prolongs. In

addition, after the onset of free convection in the cavity, the average Nusselt number reduces with increases in nanofluid concentration independent of Rayleigh number magnitude.

Kolsi et al. [109] examined the natural convection and entropy generation of Al₂C ₃/water nanofluids with volume fractions up to 15% in a cube cavity where two adiabatic blocks were installed inside it, as shown in Fig. 17. The modeling was conducted by using finite volume inches were presented for Rayleigh numbers between 10⁴ and 10⁶. They found that Nuss ¹⁴ number increases with increases in Rayleigh number and with the nanofluid concentration. On the other hand, when blocks with a smaller size were mounted in the cavity, the average Nussel number ameliorates.

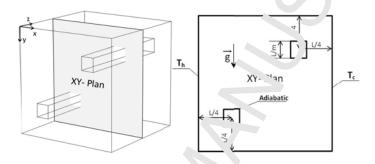


Figure 17. Schematic of the problem considered by Volsi et al. [109] (figure is reprinted with permission from publish. r).

Salari et al. [110] analyzed 3D flow, heat uses fe and entropy generation in an inclined cavity that is partially filled with MWCNTs/water ranofacid and the rest space on the top of nanofluid was occupied with air. A single-phase homogenous model was used to simulate the problem. The results were presented for volume fractions of 0.2, 0.5, and 1%, Rayleigh numbers between 10³ and 10⁶, and cavity slopes between 0 and 60 degrees. The main results of this study can be summarized as:

- When the cavity is 'n v rtical position (0°), two secondary eddies are formed in the vicinity of bottom side of carity. These two eddies are converted to one eddy with an increase in the slope angle (see Fig. 18).
- With increasing a volume fraction of nanoparticles the heat transfer rate increases while entropy generation reduces.

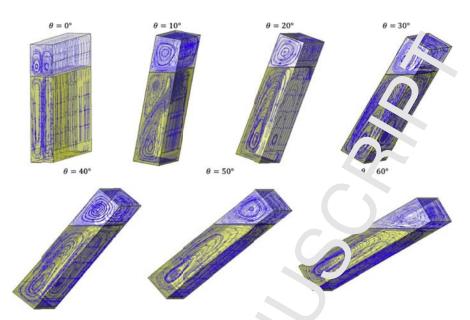


Figure 18. Three-dimensional flow pattern for enclosures with different tilt angles at $Ra = 10^5$ and = 1% [110] (figure is reprinted with permission 11.77 publisher).

Al-Rashed et al. [111] simulated the natural convection of CNTs/water nanofluids in an inclined cube cavity using finite volume method where Ahmed body is anstalled inside it (See Fig. 19). It should be mentioned that an Ahmed body is a simplified or applied of car that is used for simulation purposes in automotive industry. The simulation was performed for volume fractions up to 5%, Rayleigh numbers between 10³ and 10⁶, inclination angles between 0 and 180 degrees, and thermal conductivity ratio between 0.01 and 100. The authors concluded that the maximum average Nusselt number was achieved in inclination angles of 30 or d 100 degrees whereas the average Nusselt number was minimized at 90 degrees. Thermal conductivity ratio has no significant effect on the heat transfer rate compared to other parameters. Moreover, particle loading increased heat transfer rate inside the cavity.

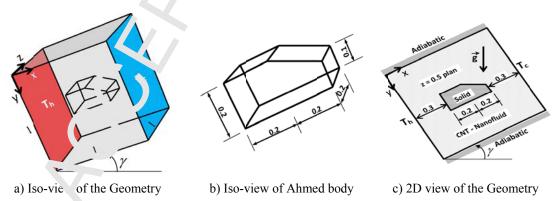


Figure 19. Geometrical representation of the problem considered by Al-Rashed et al. [111].

In another study with the same geometry and nanofluid given in [111], Al-Rashed et al. [112] analyzed entropy generation in the cavity. They found entropy generation increases with increases in volume fraction of nanoparticles.

Kolsi et al.[113] applied the FVM to study the natural convection and entropy generation of Al₂O₃/water nanofluids with volume fractions up to 15% inside an open cube swity where a diamond shaped body is installed in the middle of cavity. Maxwell and Brinkman equations were employed to estimate the thermal conductivity and viscosity of nanofluids, respectively. They concluded that from the first law of thermodynamics viewpoint, adding nanoparticles to the case fluid is advantageous, however, from the second law of thermodynamics viewpoint parts. Took ing is not beneficial since the entropy generation increases in the cavity.

Kolsi et al. [114] solved the natural convection and entropy goveration of Al₂O₃/water nanofluids with volume fractions up to 20% in a cube cavity in the prescence of Marangoni effect (or called thermocapillary force). Maxwell and Brinkman equations were used to estimate the thermal conductivity and viscosity of nanofluids, respectively. Two sidewall of casity were partially heated and the top surface of cavity was open and in contact with free stream of the analysis was done by employing finite volume method for Marangoni numbers between -1000 to 1000 and a constant Rayleigh number equal to 10⁵. It should be mentioned that a positive relationary force has a positive relationship the convection flow intensifies, on the other hand, a negative Marangoni number means that the transaction force acts against the buoyancy force. It was found that at a given value of Marangoni number, the Nusselt number increases via particle loading. The results also revealed that the increase of Nusselt number with an increase in Marangoni number and entropy generation rises with particle loading.

Al-Rashed et al. [115] investigated the MHD natural convection inside a partially heated cavity where the active zone of magnetic field was variable (the magnetic field could be applied to a part or whole of the cavity). The working fluid was CNT/water nanofluid and the method of solution was FVM. It was found that adding punoparticles increases the heat transfer rate. Moreover, the heat transfer reduced with extension of active zane and Hartmann number.

Rahimi et al. [116] employed LBM to model natural convection and entropy production of CuO/water nanofluid(volume fractions up to 4%) in a cavity with four different sets of thermal boundary

conditions. Figure 20 shows the schematic of the problem considered by Rahimi et al [116]. The authors used a single-phase approach to solve the problem while KKL model has been used to obtain the properties. Figure 21 shows a sample of their results for temperature field an . an ferent cases. It was found that adding nanoparticle to the base fluid increases the heat transfer and reduces the entropy generation.

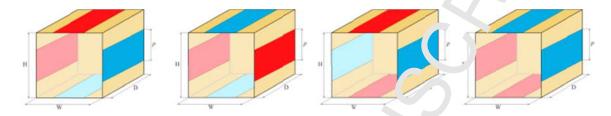


Figure 20. Schematic of the problem considered by Rahimi et al. [116] (figure is reprinted with permission from publisher).

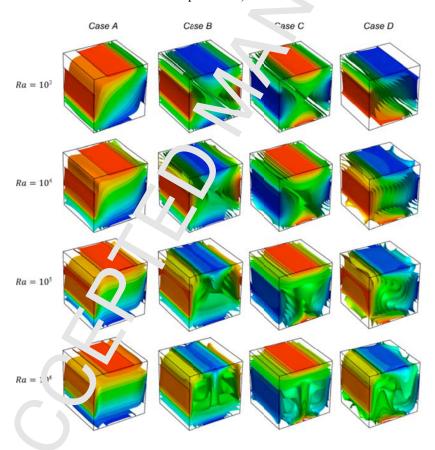


Figure 21. 1. ree- :: ensional temperature field for different arrangements of discrete active walls and Rayleign numbers at $\phi = 4\%$ [116] (figure is reprinted with permission from publisher).

In another work, Rahimi et al.[117] conducted experiments to investigate the natural convection in a cubic cavity with partially heated walls filled by DWCNTs/water (in six alreferent volume concentrations including 0.01, 0.02, 0.05, 0.1, 0.2, and 0.4%). They measured the properties of nanofluids experimentally. A three-dimensional code was developed based on the FVM and single-phase approach where for properties the measured data were used. They found that the heat transfer coefficient is maximized at a volume fraction of 0.05%. Sheremet the already model, the FDM, and a non-uniform mesh.

As can be appreciated at this stage, most papers model natural convection in nanofluids with single-phase approaches (mostly the homogenous temperature-independent technique). Table 2 summarizes the studies on 3D simulation of natural convection of nanofluids.

Table 2. Summary of studies on 3D simulation of natural convection of nanofluids (figures are reprinted by permission from publishers)

	ACCEPTED MANUSCRIPT	
With increasing Ranumber, 2D modelling overestimates the amount of Nu number compared to 3D. The difference between 2D and 3D results increases with increasing nanofluid concentration	- With increasing the Ra number, the difference between 2D and 3D results increases - Heat transfer rate estimated by 3D modelling is lower than that of 2D -Cu/water nanofluid gives higher heat transfer enhancement because it has highest thermal conductivity.	With increasing the differ at between 2D and 3D results for N: number on hot wall decreases. The difference tends to zero for aspect ratios
Higher thermal conductivity	Higher thermal conductivity	Hi ner th xm i conduct' ity Brownian diffusion
Natural convectio n- Laminar	Natural convection n-Laminar	Natural convectio n- Laminar
The Named The Head of	cold walls, T_c $\int_{\gamma} \frac{z}{z^2}$ $\int_{\gamma} \frac{z}{z^2}$ $\int_{\gamma} \frac{z}{z^2}$ $\int_{\gamma} \frac{z}{z}$	T_s
Ag/water	Al ₂ O ₃ ; C ₄ and TiO ₂ nanoparticle suspended in water.	ı
-Single phase, homogenous model, Temperature independent preverties	-Single phase, homogenous model, Temperature independent properties	Single phase, Buongiorno model
ГВМ	BEM	FDM
Boutra et al. [87]	Ravnik and Škerget [88]	Sheremet et al. [89]

2,	In the case of 2D simulation, FEM was more accurate than FDM and LBM. Comparison of 2D and 3D results for FEM unveils that the results of 2D modelling are closer to experimental data.	Cu/water nanofluid gives higher heat transfer enhancement than Al ₂ O ₃ /water.
	Higher thermal conductivity	Higher thermal conductivity
	Natural convectio n- Laminar	Natural convectio n- Laminar
	Adiabatic wall, $n = \nu = 0$ T_A F_C $A = \frac{1}{2}$ F_C $A = \frac{1}{2}$ $A = \frac{1}{$	Cavity with embedded discrete heaters
	Al ₂ O ₃ /water	Al ₂ O ₃ /water Cu/water
	phas., homog.nous mod., Tempcture independent properties	-Single phase, homogenous model, Temperature independent properties
	F.Jr FEM LBM	FVM
	Saghir et al. [90]	Purusothaman et al. [93]

	7.002	
- Particle loading diminishes the heat transfer rate especially at high Ranumbers Silver nanoparticles provides slightly higher Nu number.	Nusselt number would be enhanced through particle loading and boosting the buoyancy forces.	Optimum angle of magnetic force applied to the cavity to reach the maximum heat transfer rate was obtained for different concentrations and Ra numbers.
Higher thermal conductivity	Higher thermal conductivity Brownian motion	Higher thermal conductivity and greater magnetic field. mwsh
Natural convectio n- Laminar	Natural convectio n- Laminar	Natural convectio n- Laminar
Te Te The The Te	$\mathcal{E} \downarrow \qquad $	Cubic Cavity under magnetic field
water-based nanofluids containing Al ₂ O ₃ and Ag nanoparticles	Al ₂ O ₃ /water	CNT/water
-Single phase, homogenous model, Temperature independent properties	-Single physe hor genous model, Temperature dependent properties	-Single phase, homogenous model, Temperature independent properties
FVM/ ANSYS FLUENT	LBM	FVM
Snoussi et al. [94]	Sheikholeslami and Ellahi [100]	Al-Rashed et al [101]

	//OOLI ILD II	7.11.10001111 I
Inclination angle is more significant at high Rayleigh numbers.	By adding nanoparticles the heat transfer augments linearly - When the fin is at an angle of 180° the heat transfer is maximized.	Modelling the problem as 3D is more helpful to understand the heat transfer mechanism compared 2D modelling.
Higher thermal conductivity and greater magnetic field.	Higher thermal conductivity and changing the fin angle.	Higher thermal conductivity
Natural convectio n- Laminar	Natural convectio n- Laminar	Natural convection-
Cubic cavity under magnetic field	B ₀ . \vec{e}_{x} CATT-Manofluid $z = 0.5 \text{ plan}$ $T_{n} = 0.5 $	The plane of the p
CNT/water	CNT/water	Al ₂ O ₃ /water
-Single phase, homogenous model, Temperature independent properties	-Sin le phase, word, Temperature independent properties	-Single phase, homogenous model, Temperature independent properties
FVM	FVI	FVM
Al-Rashed et al [103]	Kolsi et al. [104]	Kolsi et al. [105]

With increases in Ranumber and nanofluid concentration both average Nusselt number and entropy generation increase.	- For water and φ = 1%, using temperature-dependent solver gives closer results to experimental data For φ = 4%, temperature-independent solver provides the minimum deviation from experimental data.	- By loading nanoparticles, the onset of natural convection prolongs Nu number reduces with increases in nanofluid concentration.
Higher thermal conductivity	Higher thermal conductivity	Higher thermal conductivity
Natural convectio n- Laminar	Natural convectio n- Laminar	Natural convectio
Hearness Cook wall	Horizontal cylinder	Cubic cavity
Al ₂ O ₃ /water	Al ₂ O ₃ /water	Au/ carboxy methyl cellulose
-Single phase, homogenous model, Temperature independent properties	phas, homog nous mode, Both Temperature dependent and independent properties	-Single phase, homogenous model, Temperature independent properties
FVM	Ope. TO'M	FVM
Kolsi et al. [106]	Meng and Li [107]	Ternik and Rudolf [108]

			ACCLI ILD	IUIAUA						
Nusselt number increases with increases in Rayleigh	numoet and nanofluid concentration	With increasing nanoparticle volume fraction heat transfer	increases and entropy generation reduces.		Maximum average	achieved in	inclination angles of 30 and 150 degrees	whereas the average	minimized at 90°.	
Higher thermal conductivity		-Higher thermal conductivity	and inclination angle		Higher	conductivity				
Natural convectio	Lamina	Natural convectio n-	Laminar		Natural	convectio	Laminar			
	Xr. Plan Xr. Plan Cubic cavity with twin adiabatic blocks	Cold wall (Above)	data. (Frost)	Ti , dr ctan, dr enclosure						Cubic cavity with incorporated Ahmed body
Al ₂ O ₃ /water		MWCNTs/water	XV		CNT/water					
-Single phase, homogenous	Temperature independent properties	phas.,	model, Temperature independent properties,		-Single	pnase, homogenous	model, Temperature	independent properties		
FVM	6	FVM			FVM					
Kolsi et al. [109]		Salari et al. [110]			Al-Rashed et al.	[111]				

	ACCEL LED MAIN	
Entropy generation increases with increases in volume fraction of nanoparticles	By adding nanoparticles both Nu and entropy generation increases.	- Nusselt number increases with increases in Marangoni number Entropy generation rises with particle loading.
Higher thermal conductivity	Higher thermal conductivity	Higher thermal conductivity
Natural convectio n- Laminar	Natural convectio n- Laminar	Natural convectio
Cubic cavity with incorporated Ahmed body	Adiabatic Adiabatic Adiabatic Cubic ' pt 1 car'. with diamond obstacle	Her Makes and Ma
CNT/water	Al ₂ O ₃ /water	Al ₂ O ₃ /water
-Single phase, homogenous model, Temperature independent properties	phase, homoge, homodel, Temperature independent properties	-Single phase, homogenous model, Temperature independent properties
FVM	FVM	FVM
Al-Rashed et al. [112]	Kolsi et al. [113]	Kolsi et al. [114]

- Adding nanoparticles increases the heat transfer rate - Heat transfer reduced with extension of active zone and Hartmann number.	Adding nanoparticles increases heat transfer and decreases entropy generation.	- A combined experimental and numerical study was done for six concentrations of 0.01, 0.02, 0.05, 0.1, (.2, ~4 0.4% Her transfer coe ficient is maximized at φ = 0.05%.
Higher thermal conductivity	Higher thermal conductivity Brownian motion	Higher thermal conductivity
Natural convectio n- Laminar	Natural convectio n- Laminar	Natural Convection n. I aminar
3D cubic Cavity with magnetic field	Cubic cavity with different jos dic is o' herting	Circulating water bath Cubic cavity
CNT/water	Cut, water	DWCNTs/ water
-Single phase, homogenous model, Temperature independent properties	-Sir le phase, homogenous model, Temperature dependent properties	-Single phase, homogenous model, Temperature dependent properties
FVM	LBM (based on Dual-MRT model)	FVM
Al-Rashed et al. [115]	Rahimi et al. [116]	Rahimi et al. [117]

3.2. Forced convection of nanofluid flow

The study of forced convection flow is significant for heat exchangers. As s and researchers have simulated nanofluids in applications ranging from micro to conventional s composed and for straight and helical tubes. The hope for replacing conventional base fluids with conofluids is that the heat transfer rate increases. However, this must be balanced with the fact that the pressure drop (pumping power) also increases due to the increase of viscosity. The latio of heat transfer enhancement to pressure drop increment due to adding nanoparticle, to base fluid is called thermal performance index (or the performance evaluation criteria) Different definitions of thermal performance index (shown by η_t) has been presented in the literature. For example, Bizhaem and Abbassi [119] used the following relationship as the thermal performance index (TPI) for the analysis of forced convection in helical tubes:

$$\eta_t = \frac{\left(\frac{h_{nf}}{h_f}\right)}{\left(\frac{\Delta p_{nf}}{\Delta p_f}\right)^{0.166}} \tag{1}$$

Hashemi and Akhavan-Behabadi [120] v the following equation as the TPI in the study of nanofluid flow in horizontal coiled tube:

$$v_{t_{t}} = \frac{\left(\frac{h_{j}}{n_{f}}\right)}{\left(\frac{\Delta p_{nf}}{\Delta p_{f}}\right)} \tag{2}$$

Yang et al.[121] invest gated the nanofluid flow in a parallel channel by assuming the same pumping power for all conditions. They used the following equation as the TPI:

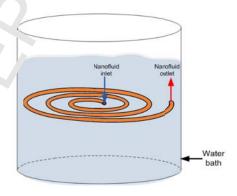
$$\eta_t = \frac{\left(\frac{Nu_{nf}}{Nu_f}\right)}{\left(\frac{f_{nf}}{f_f}\right)^{1/3}} \tag{3}$$

A greater TPI implies that nanofluid efficacy increases.

Next, the studies conducted on forced convection of nanofluids are reviewed in two main sections (i.e. single-phase and two-phase studies).

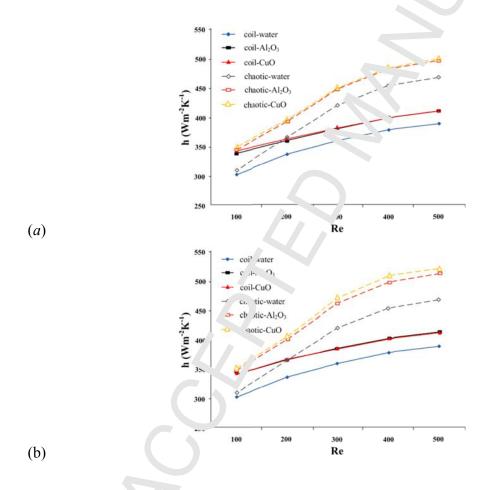
6.2.1. Studies using the single-phase approach

Doshmanziari et al. [122] simulated the forced convection undulent flow and heat transfer of Al₂O₃/water nanofluids with volume fractions up to 1.5 mm a norizontal spiral-coil tube which was kept in a water bath with a constant temperature of 60 °C. Figure 22 shows a schematic of the problem. Nanofluid enters the coil with a constant temp rature of 34 °C and after heating in the bath exits. The 3D numerical results were compared against experimental data and showed a maximum 17% deviation. They concluded that using nanofluid with a volume fraction of 1.5% instead of water can enhance the heat transfer rate up to 47% for Reynolds numbers between 9,000 and 21,200. The authors assumed that there is no slip between nar oparticles and base fluid (single-phase homogenous approach was used). Moreover, the F³ M vas used to discretize the governing equations while RNG k-ɛ model was employed to model the well-allent flow. For thermal conductivity and viscosity, the Corcione correlations were used.



Figur 22. A schematic of the problem considered by Doshmanziari et al. [122]

Tohidi et al. [123] applied two passive approaches for heat transfer enhancement inside a heat exchanger with helical tubes. The two techniques included the use of nanofluids instead of water as well as changing the simple structure of helical tubes to chaotic configuration. The results were presented for Al₂O₃/water and CuO/water nanofluids, nanoparticle concentration up to 3%, and Reynolds numbers between 100 and 500. The single-phase governing equation, were solved using FEM through the commercial software of ANSYS FLUENT. They concended that a water-based heat exchanger with chaotic configuration provides higher heat transfer rates in comparison with a nanofluid-based heat exchanger having simple coils. It should be noted in chaotic tubes the flow turbulence is more than simple tubes that it provides higher heat transfer rate. In addition, they found that CuO/water nanofluids are more advantageous than Al₂O₃/vater canofluids. Figure 23 compares the heat transfer rate for different structures and nanofluids.



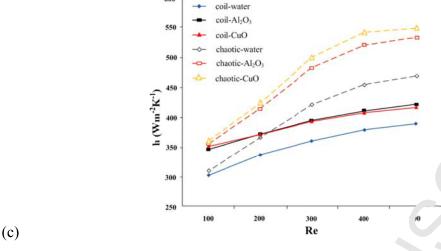


Figure 23. Variations of heat transfer coefficient with Reynolds number for volume concentrations of (a) 1%, (b) 2%, and (c) 3% and different configurations [123](figure is replinted, with permission from publisher).

Togun et al. [124] solved the turbulent flow of Al₂O₃/water nanofluid with Reynolds numbers between 20000 and 50000 and volume fractions up to 2% in at a with sudden expansion by employing the FVM. The effects of Reynolds number, nanofluid conventration, and expansion ratio on flow and heat transfer characteristics have been investigated in the study. The authors concluded that with increasing the working fluid velocity and nanoparticly volume fraction along with a larger expansion ratio the surface heat transfer coefficient callocation. The simulation, k-\varepsilon model was used to capture the turbulence flow while the nanon vide was assumed as single-phase. Maxwell and Brinkman models were used to estimate the therral conductivity and viscosity.

Shalchi-Tabrizi and Seyf [125] in stigated numerically heat transfer and entropy generation of alumina/water nanofluids in ε ingential microtube heat sink using single-phase homogenous approach(temperature dependent properties). The geometry has shown in Fig. 24. The flow was assumed laminar with fo ced convection mode with Reynolds numbers between 50 and 200. Nanoparticles with two different izes (i.e. 29 and 47 nm) and concentrations from 0% up to 4% were employed in the simulations. The results of this study suggested using nanoparticles with a smaller size, and higher concentration to have a higher heat transfer rate and lower entropy generation. In another work with similar geometry used in [125], Seyf et al. [126] simulated heat transfer, pressure drop and entropy generation in the microtube heat sink where nanofluids having a nano-encapsulated phase change material (NEPCM) enters the ducts of heat sink from the top. The results revealed that particle loading can enhance the heat transfer rate in the system. Moreover, increasing the Reynolds

number and the melting point of nanoparticles reduces the thermal resistance, and, consequently, the heat transfer rate ameliorates. It was shown that increasing the two main independent variables (mass concentration and Reynolds number) both have a major effect on the total entry generation rate which means that irreversibilities in the system reduce.

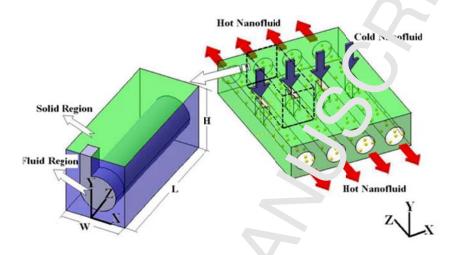


Figure 24. Schematic of microtube microchannel heart ink with tangential impingement [125] (figure is reprinted with permission from publisher)...

Yavuz and Tokgoz [127] studied single-phase flow of water, argon, Al₂O₃/water nanofluid (with a concentration of 8%) in a tube with rectail rular cross section where 8 square ribs were designed in the bottom side and 8 square ribs in the t/ρ side for disrupting the boundary layer. They concluded that using argon is more reasonable than using we are and nanofluid.

Gunnasegaran et al. [128] conside ed i. a cooling of a compact heat exchanger as shown in Fig. 25. A nanofluid (coolant) with a volur ie i action of 2% and under turbulent regime enters the channel with temperature of 82.5 °C while the i. let temperature of air is 37.5 °C. The base liquid of nanofluids was ethylene glycol and three c' ffer ent ranoparticles were considered in the analysis including Cu, diamond, and SiO₂. It was found that to achieve highest heat transfer coefficient diamond nanoparticles should be used. Juigher heat transfer coefficients were reported in the case of SiO₂ nanoparticles compared to Cu particles.

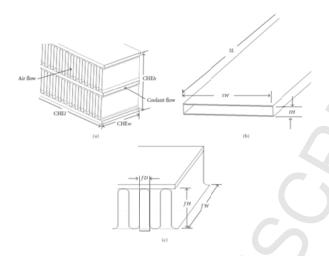


Figure 25. Schematic of the problem considered by Gunnasegaran et al. [128] (figure is reprinted with permission from publisher).

Seyf and Feizbakhshi [129] simulated nanofluid flow of micro-pin-fin heat sinks using FVM and single-phase homogenous approach. They used the corps of nanoparticles including CuO (in diameters of 28.6 and 29 nm) and Al₂O₃ (in diameters of 38.4 and 47nm) and water as the base fluid. The results were presented for volume fractions of 1 and 4%, and Reynolds numbers between 25 and 75. The authors reported that with increasing the column fraction of nanoparticles and Re, the heat transfer enhances for both types of nanoparticles and the main reasons may be the Brownian motion of nanoparticles that enhances the micro-convector in the system. It was also concluded that pressure drop increase induced by particle logating is not much significant. The article also investigated the effect of nanoparticle size. It was oncluded that with increasing the particle size, the heat transfer enhanced in the case of CuO/water nanofluids while for CuO/water nanofluid an opposite trend was obtained. The reason for this way attributed to thermal conductivity changes that for CuO/water nanofluid with increasing the particle size the thermal conductivity increases, but for Al₂O₃/water the trend was reversed.

Dugaria et al. [130] investigated turbulent forced convection of single wall carbon nanohorns (SWCNHs)/water nanon ids in a direct absorption solar receiver. Single-phase homogenous approach was employed in the modeling. Because of low concentrations of nanoparticles, thermophysical properties of nanoflucia were assumed to be equal to water and just a function of temperature. Instead, optical properties of nanofluids were involved in the governing equations. It was found that

among nanoparticle concentrations of 0.006, 0.01, 0.02, and 0.05 gr/lit the optima' concentration is 0.02gr/lit in which the receiver thermal efficiency is maximized.

Tiwari et al. [131] experimentally studied turbulent flow of Al₂O₃/water (with a lon entration of 1%) and CeO₂/water (with a concentration of 0.75%) nanofluids in a plate heat exchanger. Next, CFD simulation was done using single-phase homogenous approach with temperature accendent properties and ANSYS/Fluent software. It was found that CeO₂/water as the working fluid illustrates better performance.

Mukherjee et al. [132] investigated alumina/water nanofluid turbulent Now v th Reynolds numbers between 6,000 and 20,000 in a duct with trapezoidal ribs. Nusselt number enhances by 42.5 and 40.1% for volume fractions of 5 and 3%, respectively. Entropy generally were increased by adding nanoparticles to base fluid.

Hussein et al.[133] simulated forced turbulent convection of the convection of the convections approach (temperature-independent properties). The results were presented for Reynolds numbers between 10000 and 100000 and inlet temperatures of 60-90 °C. It was found that by using nanofluid with a concentration of 4%, the heat transfer rate can be presented by 18% although friction factor rises by 12%. As expected Nu increases with increases in inlet temperature and Reynolds number. Sheikholeslami et al. [134] employed the LBN to study the forced convection of alumina/water nanofluid(volume fractions up to 4% in a cavity where the bottom wall moves with a constant velocity. The authors investigated the context force intensity (due to magnetic field), wall velocity, and volume fraction of nanoparticles on heat transfer and fluid flow in the cavity. They indicated that with increasing the porentz force the velocity and temperature gradients reduce. It was also found that Nusselt number to reased with increases in nanoparticle volume fraction, and velocity of wall but it decreased with raising the Lorentz force. The authors used the KKL model for properties.

Hawwash et al. [135] stated the performance of a flat plate solar collector using alumina/water nanofluids (volume fractio is 0.1-3%) both experimentally and numerically. Single-phase homogenous approach with temperature dependent properties and ANSYS/FLUENT was used for simulation. It was found that the nermal efficiency of solar collector was optimized at a concentration of 0.5%. The

authors stated that adding nanoparticles with volume fractions higher than 0.5% cannot enhance the solar collector's efficiency because of agglomeration of nanoparticles.

Seyf and Nikaaein [136] employed a single-phase homogenous approach (tom₁ erature dependent properties) to model the forced convection of nanofluid flow in microcham, heat sinks. Three different types of nanoparticles including CuO, ZnO, and Al₂O₃ suspender in a mixture of water and EG (40:60 by mass) and two sizes of 29 and 77 nm were examined. The archors indicated that CuO nanoparticles provide the highest thermal performance followed by InO and Al₂O₃ nanoparticles. It was found that heat transfer ameliorates by increasing the volume fraction of nanoparticles and decreasing the size of nanoparticles. Brownian motion and micro-councillose introduced as the main phenomena for heat transfer enhancement.

Najafabadi and Moraveji [137] solved forced laminar convection flow and entropy generation of Al₂O₃/water nanofluid in a microchannel with converging channels under imposed pressure difference and considering partial slip boundary condition. The problem was solved with OpenFOAM and a single-phase homogenous approach with temperatur accordant properties. It was found that if a partial slip boundary condition is considered for the problem, even single-phase approach can predict well the experimental data. It was also noted that with increasing the nanoparticles to base fluid, heat transfer enhances and entropy generation diminishes.

Chen and Cheng [138] studied numericall, the votential of TiO₂/water nanofluids (volume fractions up to 3%) for cooling of stave of blast furnate. Single-phase homogenous model was used to predict the turbulent flow (56,800 to 75,700) of ranofluids in the heat exchanger by considering aggregation of nanoparticles. It was found that neat transfer coefficient increases with an increase in the volume fraction of nanoparticles. Also, heat transfer coefficient increases linearly with Re. It was elucidated that with aggregation of nanoparticles heat transfer coefficient reduces while pressure drop increases.

Hybrid nanofluids are a sind or nanofluids which are composed of two different types of nanoparticles. In hybrid nanofluids, usually a kind of nanoparticles with high thermal conductivity (such as CNTs) is acided to another kind of nanoparticles with lower thermal conductivity for enhancing the effective decimal conductivity of mixture. Nanoparticles such as CNTs with high thermal conductivity have high price so this mixing them with cheaper nanoparticles is reasonable.

Huminic and Francia [139] analyzed heat transfer and entropy generation of two different hybrid nanofluids including multi-walled carbon nanotubes + Fe₃O₄/water (with volume fractions of 0.1 and 0.3%) and nanodiamond + Fe₃O₄/water (with volume fractions of 0.1 and 0.2%) in a flattened

tube with application in car radiator. For properties, experimental data available in the literature were used for calculating thermal conductivity and viscosity which were as a function of nanoparticle concentration and temperature. Single-phase homogenous model and ANSY's/CTX software were applied to solve the laminar forced convection problem. It was found that using hybrid nanofluids enhances the heat transfer rate in the system. Moreover, the results revolved unit to minimize the entropy generation the use of multi-walled carbon nanotubes $+ Fe_3O_4$ 'vva'er is more advantageous than nanodiamond $+ Fe_3O_4$ /water.

Recently, Alfaryjat et al. [140] studied numerically the effects of differant twoes of nanoparticles including Al₂O₃, CuO, SiO₂ and ZnO in four sizes i.e. 25, 40, 55 and 75 and suspended in water on flow and heat characteristics of nanofluid forced convection in a heat characteristics of nanofluid forced convection in a heat characteristics and it was followed by Al₂O₃ nan aparticles and it was followed by CuO, ZnO, and SiO₂ nanoparticles. Indeed, using nanoparticles with a higher thermal conductivity guaranteed a higher heat transfer coefficient. The heat transfer coefficient augments with increasing the volume fraction of nanoparticles and decreasing the size of nanoparticles. On the other hand, pressure drop increases with reducing the nanopart. It size since the effective viscosity of nanofluids having smaller nanoparticles is higher. For solving the Navier-Stokes equations, ANSYS/FLEUNT was used by assuming a single-phase homogenous medel for nanofluids.

Ghasemi and Ranjbar [141] modeled turbulent forced convection in a receiver tube of a parabolic trough collector using CuO/water and Al₂C₂/w ter nanofluids with volume fractions up to 3% with very high Reynolds numbers i.e. about 7.54000. To solve the equations, single-phase homogenous model along with temperature-dependent properties were used. For modeling the turbulent flow k-\varepsilon model was utilized. The results indicated that using Al₂O₃/water and CuO/water nanofluids at a volume fraction of 3% can entance the heat transfer coefficient by 28% and 35%, respectively. Since this work dealt with modeling of a parabolic trough collector; it is useful that in future works some results on outlet temperature and enficiency of solar collector are presented.

Karimi and Afrand [142] invertigated the influences of hybrid nanofluid, tube arrangement, and tube cross section(circular and all ptical) on the thermal efficiency of an air-cooled heat exchanger. They concluded that the heat e changer with circular tubes has about 25% smaller pressure drop, while elliptical pipes have 10% larger heat transfer rate. Moreover, they concluded that the Nusselt number and pressure drop increase by nanoparticle loading.

Hosseinzadeh et al. [143] simulated numerically a nanofluid based photovoltaic thermal device. They reported that the thermal energy performance of the ZnO/water nanofluid with a structure of 0.03 is about 12.78% higher compared to water.

Toghraie et al. [144] investigated the combined impacts of nanofluid and porous los on the efficiency of microchannels. It was concluded that by using the porous ribs, the nanoguid los not a significant effect on heat transfer augmentation.

3.2.2. Studies using the two-phase approach

Khoshvaght-Aliabadi et al. [145] simulated laminar flow of Al_C₃/water nanofluid in twisted minichannels having different shapes of cross section including elliptic, half circular, square, rectangular, and triangular. The results were presented for volume concentrations up to 4%, Reynolds numbers less than 1500, and three different ratios of twist pitch to channel length i.e. 0.25, 0.5, and 1. The modeling was done based on two-phase mixture from and FVM. They concluded that by using a nanofluid with a volume fraction of 1% the perfort. The first maximized.

Zhu et al. [146] numerically studied laminar flow of Al₂O₃ nanoparticles suspended in a binary mixture of ethylene glycol and water inside two microchannel heat sinks with different arrangements of channels. The first microchannel heat sinks have different arrangements of channels. The study was done for verific concentrations up to 4% and Reynolds numbers up to 1,200. It was found that using ranofaid with volume concentrations higher than 1% is not beneficial based on performance index criterion. Although with increasing the nanoparticle concentration, the heat transfer enhances but on the other hand, pressure drop rises, therefore, volume fraction of 4% is not the optimal concentration. A two-phase mixture model was used in the numerical study.

Bizhaem and Abbasi [147] i. 'estigated forced convection and entropy generation of alumina/water nanofluid(volume fractions up to 3%) in a helical tube using two-phase mixture model for Reynolds numbers between 200 and 2000. It was found that nanofluid effect on heat transfer enhancement is not visible at entrance egion that in fully developed region the heat transfer enhancement is significant. Their results indicated that at $\phi = 3\%$ for Re = 200 the heat transfer enhancement (ratio of heat transfer coefficient of nanofluid to water) reaches about 22% while for Re=2000 the heat transfer enhancement approaches 15.7%. By adding nanoparticles, heat conduction in the system improves therefore

temperature gradients diminish and consequently entropy generation reduces especially at low Reynolds numbers. As expected, using helical tubes ameliorates heat transfer rate since centrifugal force applies to working fluid.

Delavari and Hashemabadi [148] simulated the cooling of a car radiator using alu. ma nanoparticles where water and ethylene glycol were considered as base fluids. The numerical study presents a comparison between single-phase and two-phase approaches for both lan. mar and turbulent regimes. Nusselt number obtained by two-phase model was greater than that of obtained by single-phase approach (between 10-45%). Experimental data confirms that two-phase model results are more reliable and closer to tests. Figure 26 compares experimental data with the rults of single-phase and two-phase approaches.

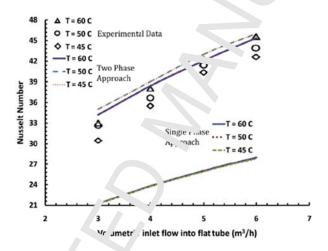


Figure 26. Comparison Letwee. experimental data [149] with CFD results obtained by

Delavari and Hashemabadi [1.9] for 0.7% Al₂O₃/ethylene glycol (figure is reprinted with permission from publisher)..

Ahmed et al. [150] ir restigated turbulent forced convection of Al₂O₃ and CuO nanoparticles suspended in water floving in a triangular duct with vortex generators. Two-phase mixture model was considered to solve the nanofluid flow by using ANSYS/FLUENT software. The results were presented for volunty firections up to 3% and Reynolds numbers between 4000 and 24000. It was found that adding nonoparticles even at a low concentration of 0.5% is more effective than equipping the plain duct to voltex generator. The authors showed that alumina/water nanofluid with a volume

fraction of 3% provides the maximum heat transfer rate even more than CuO/water ranofluid with the same concentration. This was attributed to higher Prandtl number of alumina based na. Aluids.

Ghale et al. [151] studied laminar forced convection flow of alumina/vate nanofluid (with concentrations up to 2%) in a ribbed microchannel heat sink using both sing. phase(homogenous independent-temperature) and two-phase (mixture model) approaches. It ver fould that single-phase approach underestimates the heat transfer rate with a high error content the deviation from experimental data becomes 32.6% and 37.4% for 1% and 2% nanofold, respectively. However, the two-phase mixture model gives very good prediction of heat transfer rate especially for a volume concentration of 2%. For the case of the mixture model, the deviation in experimental data reduces to 11.39% and 2% for 1% and 2% nanofluids, respectively. We also indicated that using ribs increases both heat transfer and friction factor. The simulation was done by ANSYS/FLUENT for Reynolds numbers less than 900.

Kumar and Sarkar [152] employed single-phase and two-phase mixture models to study the laminar forced convection flow of Al₂O₃/water and Al₂O₃+M₁ very water nanofluids in a minichannel heat sink. The numerical results for heat transfer coefficient were compared to experimental results for the case of Al₂O₃+MWCNTs(9:1)/water nanofluid at Revi olds numbers of 307, 368, and 430 as shown in Fig.27. As seen, in the case of nanofluids, two-phase mixture model overestimates the experimental data while single-phase underestimates the experimental data. Based on the figure, it cannot be stated that two-phase mixture model gives certainty be are results since as shown at Re = 368 the results of experimental data and single-phase at preach are closer to each other compared to experimental data and two-phase mixture model results. In general, it was also found that by using nanofluid instead of water, heat transfer coefficient increases. The maximum enhancement in the heat transfer coefficient in the case of Al₂O₃/water nareafted with a concentration of 0.01 vol.% was about 4% while for the same concentration of hybrid panoliuid (Al₂O₃+MWCNT) it reached 9%, 12% and 15.6% for the nanoparticle volume ratio of (1) (8:2), and (7:3) respectively.

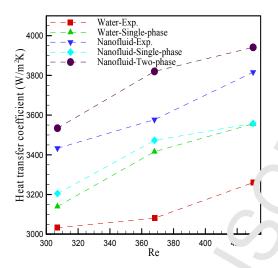


Figure 27. Comparison of single-phase and two-phase approaches with experimental data[152] (figure is reprinted with permission from publicar)..

Yang et al. [153] investigated the turbulent flow of A' C, water nanofluids (concentration up to 4 vol.%) in a channel with square cross section where the bottom of channel was equipped to step-shaped turbulators. To solve the governing equations, is turbulence model was implemented while the equations were discretized through finite volum, approach. The simulations were conducted for single-phase and mixture models and the results were compared. Both response surface method (RSM) and genetic algorithm (GA) were utilized to optimize the performance factor (the ratio of Nusselt number enhancement to pressure drop inchase caused by using nanofluid instead of base liquid) in the channel for Reynolds numbers between 5.600 and 2,0000. The results of this study show that single-phase approach estimates the Nussel number and performance factor lower than that of mixture model (see Fig. 28). The authors stated that single in the mixture model the interactions between nanoparticles as well as the drift velocity tetwoen base fluid and solid particles have been considered in the governing equations, so the mixture model provides higher values of Nusselt number. An interesting point that is observed in Fig. 7.7 is that the same trend of graphs was obtained from both the single-phase and the mixture approaches.

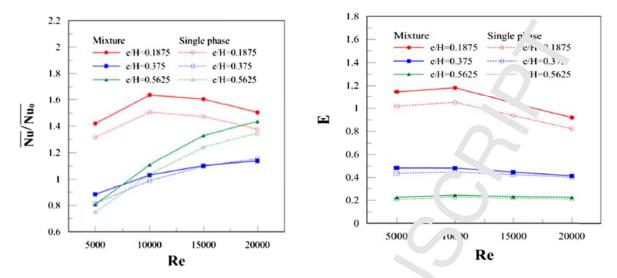


Figure 28. Comparison between single-phase and mixture mo.'als (a) 1 usselt number enhancement (b) Performance factor (for volume fraction of 4%) [153] (figure 1s. aprinted by permission from publisher).

Later, in a similar work to [153], Yang et al. [154] solved the canofluid flow in channels with wavy walls where the flow was turbulent and both single and pixture models were applied to obtain the velocity and temperature fields. In this work, they considered different values of amplitude and wavelength for the walls. Similarly, they found in value model gives higher values for heat transfer.

Bahiraei et al. [155] modeled alumina/wate^{*} nan. fluid flow in a shell and tube heat exchanger with helical baffles applied using both CFD (two phase mixture approach) and a neural network. The authors concluded that although partice loading leads to increases in pressure drop, but heat transfer enhancement is high enough to neglect the pressure drop penalty. For reaching high heat transfer and low pressure drop simultaneously, the neck angle selected should be small.

Ghasemi et al. [156] investigat d la ninar forced convection of CuO/water nanofluid(for volume fractions up to 0.75%) in her c sinks having channels with two different cross sections i.e. circular and square. Eulerian-Eulerian was phase approach and single-phase homogenous model with temperature-independent thermophy scal relations were used for the simulation. In the Eulerian-Eulerian two-phase approach lift force was in alected and just drag force was involved in the equations. They compared the results obtained from single-phase and two-phase approaches by experimental data available in the literature for 400 < Re 1000. The comparison showed both approaches overestimated Nusselt number. The maximum deviation between single-phase approach and experimental data was 8% while it reached 6% by using two-phase approach. The results revealed that adding nanoparticles and

nanoparticle volume fraction and reduction of Re. It should be noted that the value of the was higher for heat sink with rectangular channels. The authors concluded that using minich and electronic devices since the base temperature is lower.

Mashayekhi et al. [157] studied the laminar forced convection flow of A₂ 'we er nanofluids through tubes with staggered and non-staggered inserts as shown in Fig. 29. They solved the governing equation by ANSYS FLUENT and two-phase approach (Eulerian–Lag. angia i method) which considers drag, Saffman lift, thermophoretic, and Brownian force of Them sults were presented for Reynolds number between 100 and 1500, nanoparticle volume in retional up to 5%, and three types of tube i.e. plain tube(without insert), tube with staggered insert, and to be with non-staggered inserts. The results indicated that adding nanoparticles enhances both that transfer rate and friction factor. On the other hand, it was revealed that although non-staggered fructure illustrates higher heat transfer rates but staggered structure provides higher Figure on View (FoM) because of lower friction factor. With increasing Re the parameter of FoM increase.

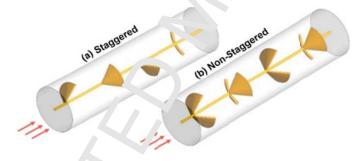


Figure 29. A mixing insert studie . by Mashayekhi et al. [157]: (a) staggered alignment and (b) non-staggered alignment \(\) 'qure is reprinted by permission from publisher).

Naphon and Nakharintr [1^e8] experimentally studied the forced convection flow of TiO₂/water nanofluid with a volume concent ation of 0.4% through a minichannel heat sink. Next, they made a 3D model of the system, with both single-phase (homogenous) and two-phase (mixture and VOF) approaches. They found that two-phase approaches are more suitable for modeling the experimental system. The authors used to capture the Brownian motion of nanoparticles while the investigated regularly numbers were less than 200.

Rostami and Abbass [159] simulated laminar forced convection in a wavy microchannel using alumina/water nanofluid(with volume concentrations up to 2%) by both single-phase homogenous and

two-phase Eulerian–Lagrangian approaches. The results were compared with experimental data available in the literature. It was found that the results of two-phase Eulerian–Lagrangian approach is close to experimental data while single-phase approach underestimates the heat final fer rate. Adding 2% nanoparticles to the base fluid led to about 12% heat transfer enhancement and 3.4% increment in pressure drop. It was also concluded that it is more effective to use nanofluid in way microchannels instead of microchannels with straight tubes.

Shi et al. [160] modelled laminar forced convection flow in a microch annel using Eulerian-Lagrangian approach and by considering the effects of drag force, the grav. v. the Brownian motion, the thermophoretic force, Saffman lift force, and pressure gradien force. It was found that by using nanofluids with a concentration of 2%, the heat transfer coefficient endances about 8.5% whereas this enhancement for volume fraction of 1% is about 5.9%.

Bhattad et al. [161] experimentally investigated turbulent force 1 convection flow in a plate heat exchanger using Al₂O₃/water and Al₂O₃+MWCNTs/water anofluids. Next, the experimental data were compared to simulation results of single-phase at 1 to 2 phase approaches. The main results of this study can be summarized as:

- The comparison between numerical models and experimental data in the case of Al₂O₃/water nanofluid showed that both single-phase and the o-phase approaches underestimate the cold outlet temperature from the heat explanation, and single phase results are closer to experimental data compared to two-phase approach.
- The comparison between num, rice a me dels and experimental data in the case of hybrid nanofluid i.e. Al₂O₃+MWC 'Ts/water showed that two-phase approach provides better predictions of cold outlet temperature compared to single-phase approach.
- Hybrid nanofluid show 1 better performance compared to Al₂O₃/water nanofluid since adding MWCNTs with high the mal conductivity improves the effective thermal conductivity of mixture.
- By using hybric nanofi id instead of water, the heat transfer coefficient increases up to 39% while pumping power increases just about 1.2%.

Sheikhalipc and Abbassi [162] used the Buongiorno's two-component non-homogeneous and Eulerian-Lagra. gian two-phase models to simulate a nanofluid flowing in a trapezoidal microchannel. Their findings indicated that the Eulerian-Lagrangian approach predicts the heat

transfer coefficient of microchannel with higher precision. It was found that wher the size of nanoparticle reaches 100 nm, the magnitude of thermophoretic force is greater 'nan. 'hat of Brownian force at the entrance region of the tube.

Moraveji et al. [163] employed different methods including single phase, mixture, VOF, and Eulerian methods to simulate dilute heat-dissipating nanofluid flow in the microphannel. They found that there is an acceptable agreement between all methods with the experimental data. Moreover, they reported that using single-phase method to model the narothuid flow through the microchannel is more accurate than two-phase methods.

Table 3 provides a summary of studies on 3D simulation of force corve tion of nanofluids.

Table 3. Summary of studies on 3D simulation of forced convection of nanofluids (figures are reprinted by permission from publishers).

	ACCEPTE	J MANUSCRIF I
Concluding remarks	-Using nanofluid with a volume fraction of 1.5% instead of water can enhance the heat transfer rate up to 47% for Reynolds numbers between 9000 and 21200.	-CuO nanoparticles gives higher heat transfer enhancement than that of Al ₂ O ₃ . - A water-based heat exchanger with chaotic configuration provides higher heat 'ransfer rates than a anc.' viid-based heat exch. nger having sir ple coils
Factors of heat transfer enhancement	Higher thermal conductivity	Brownian motion and higher thermal conductivity
Flow	Forced convectio n- Turbulent	Forced convection n- Laminar
Geometry	Spiral-coil Tube	het Heat exchanger with chaotic coils
Nanofluid type	Al ₂ O ₃ /water	CuO/water and Al ₂ O ₃ / water
Physical Model	Single phase, homogenous un, 4el, Ten, 5er 'ure demen ent pror arties	Single phase, homogenous model, Temperature dependent properties
CFD technique(s) /Software	FVM	FEM/ ANSYS FLUENT
Authors	Doshmanziari et al. [122]	Tohidi et al. [123]

With increasing the nanoparticle volume fraction along with a larger expansion ratio the surface heat transfer coefficient can be enhanced	Adding nanoparticles with a smaller size enhances heat transfer rate and decreases the entropy generation rate.	With increasing the mass concentration of nanoparticles the heat transfer enhances and entropy generation reduces.
Higher thermal conductivity	Higher thermal conductivity due to Brownian motion	Higher thermal conduction of nanofluids
Forced convectio n- Turbulent	Forced convection n- Laminar	Forced convection n- Laminar
Concentric annular pipe	Hot Nanofluid Cold Nanofluid Hot Nanofluid Z T, igential micro heat sink	Microchannel heat sinks
Al ₂ O ₃ /water	Al ₂ O ₃ /water	Octadecane / polyalphaolefi (Octadecane used as nanoencapsulate d phase change material)
Single phase, homogenous model, Temperature independent properties	Single phase, ". "nogenous moc ;l, Tempe aturc uepe .den. propc. 'ies	Single phase, homogenous model, Temperature dependent properties
FVM / ANSYS FLUENT	M/	FVM
Togun et al. [124]	Shalchi-Tabrizi and Seyf [125]	Seyf et al. [126]

Argon is the best option.	-Diamond gives higher heat transfer enhancement - SiO ₂ provides higher heat transfer rate than that of Cu	-Al ₂ O ₃ gives higher heat transfer enhancement Increasing the size of Al ₂ O ₃ nanoparticles leads to heat transfer enhancement of system but opposite erd was reported ior C.
1	Higher thermal conductivity	Higher thermal conductivity due to Brownian motion
Forced convectio n- Turbulent	Forced convectio n- Turbulent	Forced convection n-Laminar
Channel with ribs	Air flow CHE CHE COolant flow CHE CHE COOLANT d c heat Exchanger	Flow Out Flow In Micro-pin-fin heat sinks
Al ₂ O ₃ /water(with concentration of 8%), argon, and water	Cu, diamond, د. م SiO ₂ / EG	CuO/water(nano particles with two different sizes i.e. 28.6 and 29 nm) and Al ₂ O ₃ /water(nan oparticles with two different sizes i.e. 38.4 and 47 nm)
Single phase, homogenous model, Temperature independent properties	Single hasom, ¿c ats mou,¹ Temperatur independent properties	Single phase, homogenous model, Temperature dependent properties
FVM / ANSYS FLUENT	FVM	FVM
Yavuz and Tokgöz [127]	Gunnasegaran et al. [128]	Seyf and Feizbakhshi [129]

Using nanofluids enhance the thermal efficiency of solar receiver.	-CeO ₂ /water provides better performance The difference between experimental data and simulation does not exceed 4%.	-Nu increases 42.5% for volume fraction of 5% Entropy generation increases with creasing volume tractir
Better optical properties	-Higher thermal conductivity	-Higher thermal
Forced convectio n- Turbulent	Forced convectio n- Turbulent	orced cr.vect.
upper stainless steel frame steel frame steel frame steel frame steel frame precision solar receiver	Lower Distribution Area Lower Distribution Area Plate heat exchang	Rectangular duct with protrusions
SWCNHs/Water	Cef 2/w. ter and Al2O3/V atc.	Al2O3/water
-Single phase, homogenous model(due to low concentration of nanofluids, properties of wer assum 1thc	-Sing. phase, homogenous model, Temperature dependent properties,	-Single phase, homogenous model, Temperature independent properties,
FVM/ ANSYS FLUENT	FVM/ ANSYS FLUENT	FVM/ ANSYS FLUENT
Dugaria et al. [130]	Tiwari et al. [131]	Mukherjee et al. [132]

Heat transfer rate can be ameliorated by 18% although friction factor rises by 12%	Nusselt number increased with increases in nanoparticle volume fraction, and velocity of wall but it decreased with raising the Lorentz force.	For nanoparticle volume fractions in the range of 0.1 and 3%, the optimum volume fraction was of independent of independent of independent of independent independ
Higher thermal conductivity	Higher thermal conductivity, Brownian motion, Moving the bottom wall	-Higher thermal solutions and agglomeration of normal agglomeration of the standardicle streduces the efficiency.
Forced convectio n- Turbulent	Forced convectio n- Laminar	orced c avecti
d d d d d d d d d d d d d d d d d d d	Nanof A San	Absorber Absorber Heusing Coppertubes Flat Plate Solar Collector
TiO ₂ / water	A1203/W. L.	Al ₂ O ₃ /water
-Single phase, homogenous model, Temperature independent properties	-Single phase, homogenous model, Temperature dependent properties	-Single phase, homogenous model, Temperature dependent properties,
FVM/ ANSYS FLUENT	LBM	FEM/ ANSYS FLUENT
Hussein et al. [133]	Sheikholeslami et al. [134]	Hawwash et al. [135]

-CuO and Al ₂ O ₃ nanoparticles provide highest and lowest thermal performance, respectively With increasing size the thermal performance decreases.	- With decreasing size of nanoparticles the thermal performance enhances Entropy generation reduces with increasing volume fraction and decreasing nanoparticle size.	By considering partial slip boundary condition, even single-phase homogenous pproach can predict well to exp. Imental data
-Higher thermal conductivity -Brownian motion and micro-convection	Higher thermal conductivity Brownian motion	
Forced convection-	Forced convectio n- Laminar	orced correction in aminar
L _{ch} Microchannel heat sink	Nanoffd Microchannel I ea Ex har ger	Hen Hen Converging microchannel
ZnO, CuO and Al ₂ O ₃ nanoparticles suspended in EG-water(60:40 by mass) and two sizes of 29 and 77 nm.	(three di'.ent sizes ir cludin) 29, 34, an 47 nm)	Al ₂ O ₃ /water
-Single phase, homogenous model, Temperature dependent properties	-Sing: phase, homogenous model, Temperature dependent properties	-Single phase, homogenous model, Temperature dependent properties,
FVM	FVM	FVM/ OpenFOAM
Seyf and Nikaaein [136]	Mohammadian et al. [13]	Najafabadi and Moraveji [137]

Heat transfer coefficient increases linearly with increasing Re.	MWCNT + Fe3O4 /water hybrid nanofluids exhibited higher enhancement and lower entropy generation.	-Al ₂ O ₃ gives higher heat transfer enhancementWith decreasing the size of nanoparticles the heat transfer rate enhances but pressure drop tereases.
Aggregation of nanoparticle s reduces heat transfer rate.	-Higher thermal conductivity	Higher thermal conductivity Brownian motion
Forced convectio n- Turbulent	Forced convectio n- Laminar	Forced convectio n- ,aminar
Stave of blast furnace	Flat tube Figure Figur	Indet Total of the Part Sink Hexagonal microchannel heat sink
TiO ₂ /water	M., CNT + \(\times_{\alpha} \) J4 /water \(\text{s.d} \) nanod \(\text{amond} \) + Fe3O4/wat \(\text{r.d} \)	Al ₂ O ₃ CuO, SiO ₂ and ZnO nanoparticles suspended in water (nanoparticles with four different sizes i.e. 25, 40, 55 and 70 nm
-Single phase, homogenous model, Temperature independent properties,	-Sir le phase, homogenous model, Temperature dependent properties,	-Single phase, homogenous model, Temperature dependent properties
FVM/ ANSYS FLUENT	CVFEM/ ANSYS CFX	FVM/ ANSYS FLUENT
Chen and Cheng [138]	Huminic [139]	Alfaryjat et al. [140]

The increase of thermal performance of solar parabolic trough collector was higher for the CuOwater nanofluid	Solid volume fraction of nanoparticle is the dominant factor for increasing both temperature elevation and friction.
-Higher thermal conductivity -Brownian force	-Higher thermal conductivity
Forced convection n- Turbulent	Forced convectio n- Laminar
Receiver of a parabolic solar collector	Tube heat exchanger
CuO/water and Al ₂ O ₃ /water	MgO- MWC ATs/F · Water
-Single phase, homogenous model, Temperature dependent properties,	-Single phase, homogenous model, Temperature dependent properties
FVM/ ANSYS FLUENT	FVM
Ghasemi and Ranjbar [141]	Karimi and Afrand [142]

The thermal energy performance of the ZnO/water nanofluid with a solid volume fraction of 0.03 is 12.78% higher than water.	In the presence of porous ribs, the nanofluid has not a considerable influence on heat transfer enhancement.
Higher thermal conductivity	Higher thermal conductivity
Forced convection n- Laminar	Forced convectio n- Laminar
Total Parish Company of the Company	Microchannel
ZnO/water	CuC Water
-Single phase, homogenous model, Temperature dependent properties	-Single phase, homogenous model, Temperature independent properties
FVM, ANSYS Fluent software	FVM
Hosseinzadeh et al. [143]	Toghraie et al. [144]

Nanofluids with concentrations up to 4% investigated but it was found the performance index is maximized at a volume fraction of 1%.	Nanofluids with concentrations up to 4% investigated but it was found the performance index is maximized at a volume fraction of 1%.
Higher thermal conductivity	Higher thermal conductivity and Brownian motion
Forced convection n- Laminar	Forced convectio n- Laminar
Pymof TWC with climic cross section Report of the control of the	$\frac{(a)}{L} \int_{a_{p}} \frac{(a)}{L} \int_{a_{p}} (a$
Al ₂ O ₃ /water	Jajer vater
Two-phase, mixture model	Two-p. 3se mixture model
FVM /ANSYS FLUENT	FVM
Khoshvaght- Aliabadi [145]	Zhu et al. [146]

- Heat transfer enhances by adding nanoparticles especially at low Reynolds numbers Entropy generation reduces with particle loading due to the increase of heat conduction in the system.	-Nusselt number obtained by two-phase model was greater than that of obtained by single-phase approach (between 10-45%) Experimental data confirms that two-phase model results are more reliable and closer to tests	-Al ₂ O ₃ gives higher heat transfer enhancement than that of CuO because of higher Pr number. Using nanofluids ven, a low con intration of 0.76 is more effective than equipping the tube with vortex generator.
Brownian of nanoparticle s and centrifugal force due to curvature of pipe.	Higher thermal conductivity Brownian motion	Higher Prandtl 'umber
Forced convectio n- Laminar	Forced convectio n- Both Turbulent and Laminar	orced corresponding to the cor
Helical tube	Heat Exchange (c? r. diatr.)	Triangular duct with vortex tube
Al ₂ O ₃ /water	Als 3/29	CuO/water and Al ₂ O ₃ /water
Two-phase mixture model	-sin' e phase, homogenou. model, Temperature dependent properties and -Two-phase, mixture model	Two-phase mixture model
FVM/ ANSYS FLUENT	FVM	FVM/ ANSYS FLUENT
Bizhaem and Abbassi [147]	Delavari and Hashemabadi [148]	Ahmed et al. [150]

Average relative error between experimental data and single-phase model is 32.6% and 37.4% for 1% and 2% nanofluid, while based on two-phase mixture model the deviation reduces to 11.39% and 2% for 1% and 2% nanofluids, respectively.	- By using Al ₂ O ₃ /water at = 0.01%, the heat transfer coefficient enhances 4% while the enhancement reached 15.6% for hybrid nanofluid (with volume ratio of 7:3)Two-phase mixture model overestimates experimental data while single-phase uderestimates the Lata.
Brownian motion of nanoparticle s	Higher thermal conductivity
Forced convectio n- Laminar	Forced convection n-Laminar
No-slip wall Velocity inlet Welsom Web.lmm Web.lmm Rib Ribbed microchannel heat sink	Minichannel heat sink
Al ₂ O ₃ /water	-Al ₂ O ₃ /watr , Al ₂ O ₃ +MW ~NT /water(hybrid nanofluid) -For hybrid nanofluids, three volume ratio of nanoparticles were investigated investigated including (9:1), (8:2), and (7:3).
-Single phase, homogenous model, Temperature independent properties Two-phase, mix ire	-Single phase, homogenous model, Temperature independent properties, - Two-phase mixture model
FVM/ ANSYS FLUENT	FVM/ ANSYS FLUENT
Ghale et al. [151]	[152]

Single-phase model gives lower estimations of the Nusselt number compared to mixture model	Single-phase model gives lower estimations of the Nusselt number compared to mixture model	Heat transfer enhancement is high enough to neglect the pressure drop penalty.
Higher thermal conductivity and Brownian motion of particles	Higher thermal conductivity and Brownian motion of particles	Brownian motion of nanoparticle s
Forced convection n-Turbulent	Forced convectio n- Turbulent	Forced convectio
Rib-grooved channel	The state of the s	Helix Angle Overlap Heat Exchanger with baffles
Al ₂ O ₃ /water	A. O ₃ /water	Al ₂ O ₃ /water
-Single phase, homogenous model, Temperature independent properties and Two-phase, mix are model	phase, homogenou, model, Temperature independent properties and -Two-phase, mixture model	Two-phase, mixture model
FDM	FDM	FVM
Yang et al. [153]	Yang et al. [154]	Bahiraei et al. [155]

-Single-phase and two-phase approaches overestimated the experimental Nu numberTwo-phase model is more accurate Heat sink with rectangular channel is better.	-Staggered structure provides higher FoMAdding nanoparticles enhances the heat transfer enhancement.	Two phase models (mixture two phase and VOF) are more appropriate than homogeneous model (single phase)
-Higher thermal conductivity , -drag force -Brownian motion	Higher thermal conductivity , drag force, thermophore tic force, Brownian force, lift force	Higher thermal conductivity
Forced convection-	Forced convectio n- Laminar	Forced convection the although the second associate with laminar flow)
Phul outlet Phul outlet	Tu' e v . c c nica' rip	No heat loss No heat loss Minichamet Mi
CuO/water	Ag/wat í	TiO ₂ / water
-Single phase, homogenous model, Temperature independent properties, Two-phase moc 3, Euleri 1- cule an	Two-phase, Eulerian– Lagrangian	-Single phase, homogenous model, Temperature independent properties -Two-phase, mixture -Two-phase,
FVM/ ANSYS FLUENT	FVM/ ANSYS FLUENT	FVM/ ANSYS FLUENT
Ghasemi et al. [156]	Mashayekhi et al. [157]	Nakharintr [158]

-Two-phase Eulerian-Lagrangian approach is closer to experimental data -Adding 2% nanoparticles to the base fluid led to about 12% heat transfer enhancement and 2.4% increment in pressure drop	By using nanofluids with a concentration of 2%, the heat transfer coefficient enhances about 8.5% whereas this enhancement for volume fraction of 1% is about 5.9%.
Higher thermal conductivity Brownian force drag force	The following forces were included: drag, the gravity, the Brownian motion, the thermophore tic, Saffman lift, pressure gradient
Forced convection n- Laminar	Forced convectio n- Laminar
Wavy microchannel	Ha Ha Microc.nar.nel Microc.nar.nel
Al ₂ O ₃ /water	Aly 3/, nter
Single-phase homogenous temperature dependent and Two-phase Eulerian—Lagrangian	Tow-r-ase, Eulerian- Lagrangian
FVM	FVM/ ANSYS FLUENT
Rostami and Abbassi [159]	Shi et al. [160]

- Eulerian- Lagrangian model gives more accurate solution in the case of hybrid nanofluid while in the case of Al ₂ O ₃ /water single phase shows better predictions.	-Eulerian- Lagrangian is more accuratewhen the size of nanoparticle reaches 100 nm, the magnitude of thermophoretic force is greater than that of Brownian force at the entrance region of the tube.	Single-phase method is the best.
Higher thermal conductivity	The following forces were included: drag, the Brownian motion, the thermophore tic, Saffman lift	ther al
Forced convectio n- Turbulent	Forced convectio n- Laminar	orced co. tie n- Laminar
Plate heat exchanger	Pyr A Glass Co W Silicon Substrate Trapezoidal microchannel	6 mm ← → → 119 μm Microchannel
Al ₂ O ₃ /water, Al ₂ O ₃ +MWCNT /water	Al ₂ O_Water	CuO/Water
-Single phase, homogenous model, Temperature independent properties, - Two-phaselerian- Lag angian model	Buongiorno's two-component non-homogeneous and Eulerian-Lagrangian two-phase models	Single phase, mixture, VOF, and Eulerian
FVM/ ANSYS FLUENT	FVM	FVM
Bhattad et al. [161]	Sheikhalipour and Abbassi [162]	Keshavarz Moraveji et al. [163]

3.3. Mixed convection of nanofluid flow

Although they are not as common, some studies have been done to simulate nar ofly ds in the mixed convection mode. As before, these studies can be roughly classified into two nain groups – (i) single-phase and (ii) two-phase approaches.

3.3.1. Studies using the single-phase approach

One major applications of nanofluids is in nuclear reactor. Can fluids with higher thermal conductivity compared to base fluids can be good coolants as nuclear reactors. In this regard, Mousavizadeh et al. [164] investigated the effect of using 1.02/w ater nanofluid on cooling rate of VVER-1000 nuclear reactor with a height about 3.8 m by mour eling the mixed turbulent nanofluid flow as a single-phase and homogenous working fluid. It was found that adding nanoparticles with a volume concentration of 1.5% can reduce the clad are perature about 1 °C. Maybe testing other working fluids such as CNTs based nanofluids could show better cooling performance since the effective thermal conductivity of TiO2/water is another high. It was also found that with decreasing the size of nanoparticles and the increase of nanoparticle concentration, the heat transfer coefficient increases.

Dawood et al. [165] studied laminar mi ted contection of different nanofluids containing Al₂O₃, CuO, SiO₂ and ZnO nanoparticles in an elimetric article type, nanoparticle size (from 20 to 80 nm), volume concentration (up to 4%), Revalids number (between 200 and 1000), and different base fluids including water, glycerin, engine bil, and ethylene glycol have been investigated in the study. They concluded that although SiO₂ canoparticles have the lowest thermal conductivity among the above mentioned particles but using SiO₂ based nanofluids provides the highest Nusselt number (followed by Al₂O₃, ZnO, and CuO nanopa ticles). It was found glycerin was the best base fluid for heat transfer enhancement. In addition, neat transfer rate was maximized at Reynolds number of 1000, nanoparticle size of 20 nm and volume raction of 4%.

Kherbeet et al. ['00] 2 ved laminar mixed convection flow(at Re= 35) of four different ethylene glycol based nanotivids containing SiO₂, Al₂O₃, CuO, and ZnO nanoparticles over a micro forward-facing step through single-phase approach. The results were presented for nanoparticle sizes ranging

from 25 to 70 nm and volume fraction up to 4%. They found that using SiO₂ nanoparticles provides highest Nusselt number. Moreover, an increase in volume fraction ameliorates the 'substall number while using nanoparticles with a smaller size is more advantageous from the heat transfer enhancement viewpoint.

Al-Rashed et al. [167] simulated mixed convection of CNTs/water nanofly ids a cavity equipped with adiabatic-driven baffle for Rayleigh numbers between 10³ and 10⁵ using TVM and single phase approach. They investigated the effect of baffle motion in different di ections on heat transfer and entropy generation inside the partially heated cavity.

Al-Rashed et al. [168] later applied the FVM to model the single phase mixed convection flow and entropy generation of Al₂O₃/water nanofluid inside a cavity where all ot block was installed in its center. Maxwell and Brinkman models were used for thermal conductivity and viscosity estimation. It was found that Nusselt number and entropy generation includes with increasing the nanoparticle volume fraction. The results also revealed that with increasing the block size, Nu number and entropy generation increase.

Zhou et al.[60] analyzed mixed convection in a correy filed with alumina/water nanofluid using LBM (D3Q19 model) and employing Maxwell and Brinkman models for thermal conductivity and viscosity. The cavity was under an external magnetic field a d the cold side wall moved with a constant velocity towards up. The effects of nanoparticle volume fractions up to 6%, orientation of magnetic field (angles between 0 to 180°), Richardson and ers between 0.1 and 10, and Rayleigh numbers of 10⁴-10⁶ on flow and heat characteristics in ride the cavity. The results of this study show that the average Nusselt number decreases with increasing the Ri number, and the average Nusselt number increases with an increase in volume fraction of nanoparticles at Ra numbers of 10⁴ and 10⁵, however, for Ra = 10⁶ in which the convection mode is dominant an optimal value for volume fraction can be found in which Nusselt number is maximized. It was also found that with increasing the magnetic field intensity the average Nusselt number hand Nu is minimized when the magnetic field is applied to the cavity perpendicularly. This study suggests that for increasing the average Nusselt number, nanopartical scar of added to the base fluid, especially at low Ra numbers, also the direction that magnetic force of publics to the cavity should be parallel to the cavity as much as possible.

Karbasifar et al. [169] studied the effect of adding alumina/water nanoparticles to water on flow and heat transfer patterns in an inclined cavity where a hot cylinder was installed in it, conter and the top wall could move with a constant velocity. The results were presented for Richaus in numbers of 0.1, 1, 10, 100, nanoparticle volume fractions of up to 0.2%, inclination angles of 0 , 15°, and 45°, and a temperature difference of 50°C between hot cylinder and cold side walls. Their results show that at a given Ri number, the Nu number increases with nanoparticle volume fraction linearly, the authors attributed this increase to Brownian motion and clustering phenome for. However, the authors used the Maxwell and Brinkman models to calculate the thermal conductivity and viscosity, and on the other hand, single phase approach was used to solve the problem, therefore the heat transfer enhancement due to particle adding is not because of Brownian models. The only factor that can be considered in governing equations and thermothysical models. The only factor that can be considered in this problem as responsible to for heat transfer enchantment is enhancement in thermal conductivity.

Mohammed et al. [170] simulated the laminar mixed co. rection of Ag, Au, CuO, diamond, and SiO₂ nanoparticles suspended in water in a vertical channel with square cross section by considering radiation effect. The simulation was done for volume concentrations up to 3%, Reynolds numbers between 200 and 1000, and Rayleigh numbers between 2×10⁶ and 2×10⁷. It was concluded that despite the lowest effective thermal conductivity of SiO₂/rater nanofluids, they give highest values of Nusselt number. On the other hand, Au nanoparticles provide lowest Nusselt numbers.

Selimefendigil and Oztop [171] co sidered mixed convection in a cavity where two cylinders rotate with a constant angular velocity inside the cavity. Three different water based nanofluids containing Al₂O₃, TiO₂, and Cu nanoparticles have been selected as the working fluid. The results were provided for Ra numbers between 10⁴ and 10⁵ and volume fractions up to 4%. Single phase approach and FEM were used to solve the proof of value Maxwell and Brinkman models were selected to estimate the thermal conductivity and viscosity. Figure 30 shows the variation of Nu number versus different values of dimensionless and constant velocity of cylinders for volume fraction of 2% and Rayleigh number of 10⁵. As seen, at ding Conanoparticles with highest thermal conductivity to the base fluid leads to highest heat transfer enhancement. Indeed, the heat transfer enhancement has direct relationship with thermal conductivity of nanoparticles. Also, the maximum heat transfer happens when the cylinders rotate with maximum speed and in counter-clockwise direction.

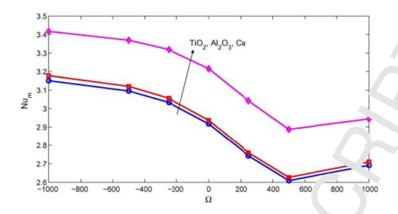


Figure 30. Variations of Nusselt number versus relative angular velocy of y. nders [171] (figure is reprinted by permission from publishe.)

Akbari and Behzadmehr [172] employed finite volume approach to solve the laminar mixed convection developing flow of Al₂O₃/water nanofluid (with volume fractions up to 4%) in a horizontal tube under constant heat flux. It was concluded that adding in poparticles has no a significant effect on the velocity field. However, the temperature field is after a clearly by particle loading because of heat diffusion induced by solid nanoparticles. It was reproced that local heat transfer coefficient ameliorates by adding nanoparticles.

3.3.2. Studies using the two-phase approach

Safikhani et al. [173] first simulated la nin it mixed convection flow of Al₂O₃/water nanofluid in ducts with circular and flatted cross sections wing two-phase mixture model, next using CFD results, optimization was done to reach the natimum heat transfer coefficient and the least pressure drop. Multi-objective optimization v as carried out by employing artificial neural networks (ANN) and genetic algorithms (GA) by involving different parameters including heat flux, size of nanoparticles, volume flow rate, nanoparatile contentration and geometry specifications.

Mohammed et al. [174] investigated laminar and turbulent mixed convection of ZnBr₂/acetone nanofluid by emploring two-phase mixture model. It was found that adding 1.5% nanoparticles enhanced heat transfer coefficient up to 180% mainly due to Brownian motion of nanoparticles.

Shariat et al.[175] s'udied laminar mixed convection flow of alumina/water nanofluids in ducts with elliptical cross section under constant heat flux using two-phase mixture model. They used

temperature-dependent models to estimate the thermal conductivity and viscosity. The authors indicated that adding nanoparticles boosts the secondary flows, and, consequently, the deat transfer rate enhances. In addition, the authors showed that a duct with elliptical cross section can be more advantageous than a circular tube by considering both maximum heat transfer rate and minimum friction factor.

Zonouzi et al.[176] simulated 3D dimensional mixed convection flow of . \\ \frac{1}{2}C_3/\text{water nanofluid} \\
(laminar and developing flow) in helical tubes using mixture model ar \(\text{LVM}. \) remperature dependent models for properties were employed in the simulation where the max. \(\text{num} \) oncentration of nanofluids was 3%. Effects of different forces including centrifug all ar \(\text{L} \) avitational as well as nanofluid concentration and structure of tubes on heat transfer \(\text{L} \) as system were investigated. The authors concluded that although adding nanoparticles co. \(\text{inuous} \) y increases the heat transfer rate but for concentrations higher than 2% the heat transfer enhancement is not significant and is not economic.

Sivasankaran and Narrein [177] numerically investigate. Caminar flow of alumina/water nanofluid(with volume fraction of 1%) in a helical and prous microchannel using two-phase mixture model. Modified models for thermal conductivity and viscosity were used. In the study, there is no discussion on the effect of working fluid type and concentration; instead the focus was on the inlet velocity profile to microchannel.

Kareem and Gao [178] studied turbilient mixed convection in a double lid-driven cavity using ANSYS/FLUENT(based on FVM) and Co-r lase mixture model. The results were presented for three different nanoparticles including S.O₂, 7nO and CuO suspended in water as well as Reynolds numbers between 5000 and 30000, nan particle diameters between 25 and 85 nm, and nanoparticle volume fractions up to 8%. For modeling the turbulence flow, Unsteady Reynolds-Averaged Navier-Stokes (URANS) and Large Eddy Sir ulation (LES) techniques were employed. The results of this study can be summarized as follows.

- The maximum leat transfer enhancement was obtained by using SiO₂ nanoparticles because of their lowest density and hence the maximum velocity. Following SiO₂, ZnO and CuO are in the next rank.
- Large Early Simulation method gives more details of velocity and temperature fields compared to URANS. Although their prediction of Nusselt number is not much different.

- With increasing volume fraction of nanoparticles and Reynolds number and on the other hand decreasing the size of nanoparticles, Nusselt number enhances.
- It can be observed from Fig. 31 that the effect of adding nanoparticle to ¹ ase fluid on Nu is not much visible at low volume fractions (i.e. 2%), however, with increasing u. `nanoparticle loading the heat transfer enhancement highlighted (for volume fraction) from 2 to 8%).

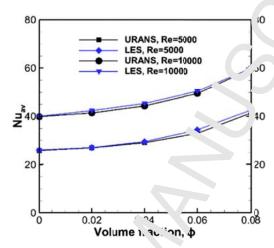


Figure 31. Comparison of average Nusselt number. A siftee ent Reynolds numbers and volume fractions [178] (figure is reprinted by permission from publisher).

Aminfar et al. [179] investigated the potential of passive and active techniques for heat transfer enhancement in a straight tube where water flows inside it with a laminar regime and mixed convection mode. Using a curved tublinstead of straight tube (passive), loading Fe₃O₄ nanoparticles to water with a volume fraction of 4% (passive), and applying a non-uniform magnetic field (active) were the three used techniques. Figure 32 shows the effect of applying different techniques on the value of local heat transfer confining and for Reynolds numbers of 50 and 100. As seen, using the three techniques can enhance the heat transfer significantly (especially nanoparticles loading and applying magnetic field). The authors used two-phase mixture approach to model the problem.

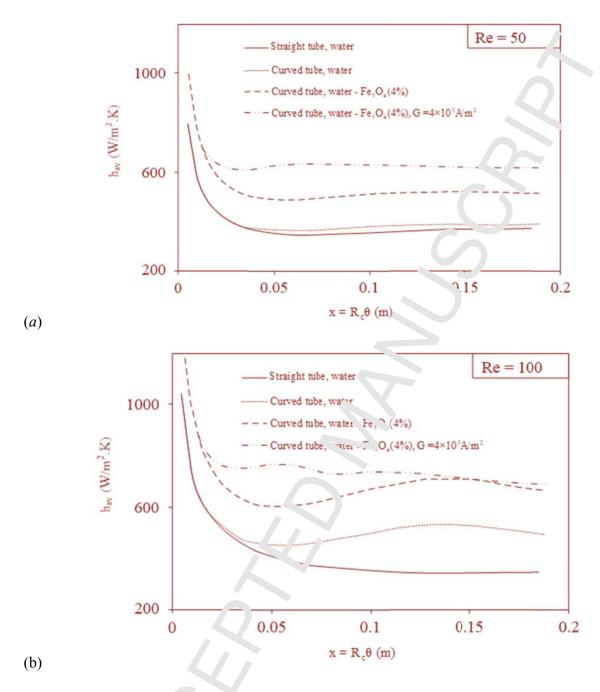


Figure 32. Effects of the geome vic curvature, magnetic nanoparticles and magnetic field on the heat transfer coefficient behavior as the tube (a) Re = 50 (b) Re = 100 [179] (figure is reprinted and modified by permission from publisher).

Shahmohamma I and Jafari [180] studied mixed convection of alumina/water nanofluids in a horizontal tube uncer constant heat flux and equipped to baffles. The simulations were carried for both laminar and turbulent flow regimes (Reynolds numbers up to 3000) and two volume concentrations of

1 and 1.6%. The authors employed homogenous single-phase approach (temperature-independent properties) and three two-phase approaches including Eulerian, mixture, and VO.4. The results were compared with experimental data and it was found that single-phase approach results are relatively far from experimental data, so a two-phase approach should be used to capture un experimental data. Among the three two-phase approaches, mixture model was proposed as the most cuitable because of easiness of application. It was also found that effects of adding nanoparticles to base fluid is more visible at Re < 1000, while equipping the tube to baffle is more advantageous at Re > 2000. Yousofvand et al. [181] studied the first and second laws of thermogenamics for an electromagnetic pump using nanofluids by employing LBM.

Table 4 gives a summary of studies on 3D simulation of mixed convection of nanofluids.

Table 4. Summary of studies on 3D simulation of mixed convection of nanofluids (figures are reprinted by permission from publishers).

Adding nanoparticles has considerable effect on heat transfer coefficient while there is no significant effect on temperatures like clad temperature.	- SiO ₂ provides highest heat transfer enhancement because of its lowest density and consequently highest velocity Nanoparticles with minimum size and maximum volume fraction give maximum heat transfer rateGlycerin is the best oing fluid.
-Higher thermal conductivity -Brownian Motion	Higher velocity of nanofluid
Mixed convectio n- Turbulent	Mixed convectio n- Laminar
Wall heat transfer (1 m) Nuclear reactor	Elliptic annulus
TiO ₂ /water (nanoparticles in two different sizes of 10 and 20nm were tested)	SiO ₂ , Al ₂ C ² , ZnO, and CuC nanoparticles, and four base fluids i.e. water, glycerin, engine oil, and EG.
-Single phase, homogenous model, Temperature dependent preperties,	Single phase, homogenous model, Temperature dependent properties
FVM/ ANSYS FLUENT	FVM / ANSYS FLUENT
Mousavizadeh et al. [164]	Dawood et al. [165]

-SiO ₂ gives higher heat transfer enhancement - Smallest size and highest volume fraction of nanoparticles provide highest heat transfer rate.	Effect of baffle motion in different directions on heat transfer and entropy generation inside the cavity was investigated.	With increasing the block size and concentration of nanofluids both Nu number and entropy generation increase.
Lower density and higher velocity	Higher thermal conductivity and using the baffle at high Ra numbers.	Higher thermal conductivity
Mixed convectio n- Laminar	Mixed convectio n- Laminar	Mixed convectio n- Laminar
Horizontal microscale forward-facing step	The Adiabatic Adiabatic CNT-nanofluid z=0.5 Adiabatic (b) C. oi cav., with moving baffle	Cubic Open Cavity with a Central Isothermal Block
SiO ₂ , Al ₂ O ₃ , CuO, and ZnO nanoparticles suspended in EG.	CNT/water	CNT/water
Single phase, homogenous model, Temperature dependent properties	-Sin Je phase. nom gen. ''s mode., Temperatur independent properties	-Single phase, homogenous model, Temperature independent properties
FVM	FVM	FVM
Kherbeet et al. [166]	Al-Rashed et al [167]	Al-Rashed et al [168]

• Nu increases with an increase in volume fraction of nanoparticles at Ra numbers of 10^5 , however, at Ra = 10^6 an optimal value for volume fraction can be found in which Nusselt number is maximized.	Nu number increases with nanoparticle volume fraction linearly	SiO ₂ gives higher heat transfer enhancement
Higher thermal conductivity, decreasing the intensity of magnetic field increases the Nu number	-Higher thermal conductivity	Lower density and higherlocity
Mixed convectio n- Laminar	Mixed convectio n- Laminar	Mixed onvectio n-
The second secon	coldwall bot cylinder, The adiabatic Tre adiabatic Inclined lid-driven control of the cylinder colliptical centric cylinder	Outlet Rectangular Duct
Al ₂ O ₃ /water	Abs 3/2.rter	Ag, Au, CuO, diamond, and SiO ₂ /water
-Single phase, homogenous model, Temperature independent properties	-Sing, phase, homogenous model, Temperature independent properties,	Single phase, homogenous model, Temperature dependent properties
LBM	FVM	FVM
Zhou et al. [60]	Karbasifar et al. [169]	Mohammed et al. [170]

-When the cylinders rotate counter-clockwise the heat transfer rate is maximized Using nanoparticles with highest thermal conductivity provides the highest heat transfer enhancement.	Adding particles has no significant effect on velocity field but considerably affect the temperature field.	CFD results were used to carry out rulti-objective ptu. 'zation by empl ying ANN and GA'.
-Higher thermal conductivity	Heat diffusion induced by nanoparticle s.	
Mixed convectio n- Laminar	Mixed convectio n- Laminar	fixed cotic n- Laminar
$T = T_h$ $(x_{c_1, c_{c_1}})$ $(x_{c_2, c_{c_2}})$ $(x_{c_3, c_{c_3}})$ (x_{c_3, c_3}) $($	top R Bottom bottom S ann ry Plane Horizontal tube	Flatted tubes with the same perimeter
Cu, Al2O3 and TiO2/water	Al ₂ C ₃ /wate	Al ₂ O ₃ /water
-Single phase, homogenous model, Temperature independent properties	Single-phase, homogenous model, Temperature independent properties	Two-phase mixture model
FEM	FVM	FVM
Selimefendigil and Öztop [171]	Akbari and Behzadmehr [172]	Safikhani et al. [173]

Adding 1.5% nanoparticles enhanced heat transfer coefficient up to 180%.	Adding nanoparticles boosts the secondary flows, and, consequently, the heat transfer rate enhances	Heat transfer enhancement rate decreases with increasing nanoparticle volume fraction.	Effect of inlet elocity profile on leat to masfer rate was lavestigated.
-Higher thermal conductivity , Brownian Motion	Higher thermal conductivity and Brownian motion	Brownian motion of nanoparticle s and centrifugal force due to tube structure.	
Mixed convectio n- Laminar and turbulent	Mixed convectio n- Laminar	Mixed convectio n- Laminar	Mixed convectio n- Laminar
R1.5 Flow direction Flow Flat tube	b y z x y z Elliptic ducts	Powerbear Helical Tube	Helical microchannel
ZnBr/acetone	Al ₂ O ₃ /water	Al ₂ O ₃ /water	Al ₂ O ₃ /water
Two-phase, mixture model	Two-r .ase, mixt .re mode.	Two-phase, mixture model	Two-phase, mixture model
FVM/ ANSYS FLUENT	FVM	FVM	FVM/ ANSYS FLUENT
Mohammed et al. [174]	Shariat et al. [175]	Zonouzi et al. [176]	Sivasankaran and Narrein [177]

-SiO ₂ gives higher heat transfer enhancement With increasing concentration and Re, and decreasing size of nanoparticles the heat transfer enhancesLarge eddy simulation approach is suggested to use instead of Unsteady Reynolds-Averaged Navier-Stokes approach.	Two-phase models are more precise than single-phase model. Among the three two-phase models, the mixture model is suggested to use because it is simplest to apply.
Higher velocity(low er density) and thermal conductivity	Brownian motion of nanoparticle s and heat diffusion of nanoparticle s. Using baffle to increase turbulency
Mixed convection n- Turbulent	Mixed convectio n- Laminar and Turbulent
H L Treatment of the control of the	Tube with baffles
CuO, ZnO, SiO ₂ nanoparticles suspended in water	Al ₂ O ₃ /wate.
Two-phase, mixture model	-Single phase, homogenous model, Temperature independent properties -Two-phase Eulerian- Eulerian- Mixture,
FVM/ ANSYS FLUENT	FVM/ ANSYS FLUENT
Kareem and Gao [178]	Shahmohammadi and Jafari [180]

												1
Optimal value for	volume fraction of	nanoparticles can be	found at high	Rayleigh numbers so	that the cooling rate	is highest.	0					
ı	0											
Mixed	convectio	n-	Laminar									
	Electrods	Hot element	Connecting	wires			Magnets	Descense	rower supply	Electromagnetic Pump		
Cu/water												<u>/</u>
Single-phase, Cu/water	homogenous	model,	Temperature	dependent	properties						/	/
LBM							7					
Yousofvand et	al [181]	[,,,]										

4. Conclusions

Nanofluids are attracting increasing attention due both to their highly attraction the mail properties and to the fact that the nanofluid properties can, to some extent, be tailor do specific applications. Nanofluids are used in wide-ranging applications, from automobiles to solve thermal collectors—any applications which require efficient heat and mass transfer. This comprehens we review built upon Part I [1], which dealt with fundamental and theoretical physics of nanofluidary, including various models presented to describe nanofluid flow on different scales. As such, the present review, Part II, discussed the primary CFD approaches for solving the transport equations given in part I [1]. These approaches were categorized into three general groups i.e. macroscale-based, mesoscale-based, and microscale-based techniques. To examine the state-of-the-art in this field recent three-dimensional studies on modeling nanofluid flow were reviewed, indicating the large of flow regimes, geometries, the nanofluid types, solution methods, and the physical physical physical physical physical physical in each model. Although underlying phenomena can be applied to many approactions, it was found that these three-dimensional studies have most frequently been used to an expectation. For menal systems such as solar collectors and microchannels. The main points that have been revealed in Part II of this review can be summarized as:

- FVM and ANSYS/FLUENT are the most used numerical method and software package, respectively, for solving problems in nanofluid flow. However, as with all fluid mechanics problems, the choice of numerical method depends critically on the specifics of the problem.
- Several studies look at the natural convection of nanofluids in cavities, and the difference between 2D and 3D models Giverge with increasing Rayleigh number and nanoparticle volume fraction (see, for example, 'sef. [87])
- The aspect ratio of a c. vity may cause differences between predictions of 2D and 3D models.
- For a specific probem, the single-phase approach may results which match experimental better data compared to a two-phase approach, but by changing the nanofluid this trend may reverse (as mentioned in Ref. [161].

- Brownian motion of nanoparticles has often been cited as the most important phenomenon responsible for heat transfer enhancement of nanofluids, especially in strictles that employed the single-phase homogenous approach with temperature-dependent properties.
- Using nanoparticles with a higher thermal conductivity (for example A. O₃ with a thermal conductivity of about 40) does not always provide a higher heat transfer rate. Sometimes using nanoparticles with a lower density (such as SiO₂ with a thermal conductivity of 1.4 W/mK) yields a higher heat transfer rates because a lower density nano fluid can have a higher velocity. In other words, the velocity of nanofluid is also an important—but often overlooked—parameter in the determination of the heat transfer rate.
- Entropy generation in thermal systems where irreversiblity due to heat transfer is dominant usually decreases by adding nanoparticles, since nanoparticles enhance heat conduction in the system and consequently reduce temperature gradients.
- Considering a partial slip boundary condition in ni rochannels increases the accuracy of the single-phase homogenous approach in compa. so with experimental data (see for example [137]).
- The effects of adding nanoparticles or is ansfer coefficient is not high at the entrance region of tube in cases of forced and mixed convection, but when the flow becomes fully developed the effect of nanoparticly loading on heat transfer coefficient is more pronounced.

5- Gaps and future work

The present review revealed that there are still many unsolved questions in the field of nanofluid flow simulation, particularly when three-dimensions must be considered. The literature still needs comprehensive studies that the all involved physical phenomena in nanofluid flow and heat transfer problems without excessive simplifications. Figure 33 shows the most common keywords in studies on three-dimensional nodeling of nanofluids, and may help to better identify the gaps in this area. The following points can be found from the figure:

• As seen, mr ng nanoparticles, Al₂O₃ nanoparticles are the most used. Other nanoparticles such as CuO, TiC₂, SiO₂ and CNTs are other materials that used frequently. Moreover, almost all nanoparticles used in the studies are spherical and cylindrical in shape. Therefore, one

suggestion may be developing experimental and theoretical models for prediction the properties of nanofluids having novel nanoparticles and shapes, and ther evaluation of their potential for heat transfer enhancement in different systems.

- Most studies use homogenous models (either temperature-dependent) or the mixture model. More studies, both numerical archivenental, are needed to determine the optimum approach for modeling and the condition under which the single-phase homogenous approach (the easiest technique for modeling of nanofluid flow) gives acceptable results.
- Besides laminar and turbulent regimes, nanofluids flow if the transition regime is an area that requires more investigation.
- The FVM was the most used numerical approach for simulation of nanofluid flow. Comprehensive studies are still lacking that compare the capabilities of different numerical approaches.



Figure 33. Word cloud of most used terms in three-dimensional modeling of nanofluids

In the following some other cugge cons have been given for future work:

- Three dimensional modeling of nanofluids in thermal systems having vibration may be interesting since in practice vibration might keep the particles suspended better and create mixing at the same time.
- More attem, to show ld be done on three dimensional modeling of thermal systems by considering, acticle sedimentation during the computational time interval.
- Erosion and corrosion due to nanofluid flow may be another topic of interest.

- Using experimental-based correlations or more advanced models for thermophysical properties may reduce the difference between heat transfer rate predicted by the single pince homogenous approach and experimental data.
- Using two-phase approaches for hybrid nanofluids, where the non-uniforn. v in shape and size of nanoparticles are included simultaneously, could be a challenge.
- Studies can be done on the determination of the exact contribution of afferent forces, including common forces such as Brownian and thermophoretic in one hand, and on the other hand interparticle forces such as double layer and van der Waa.
- Solidification and melting phenomena may be considered for 2 \(\infty \) nodeling using two-phase approaches.
- Three dimensional analysis of solar desalination systems [182] could be of interest due to the present crisis of fresh water in the world.
- Determination of dominant forces in nano-refrigerant flows and modeling of this type of flow in various configurations and regimes could be 21.1est.
- There are only a few studies on CFD simulation of bubbles dynamics in pool boiling of nanofluids (for example see Ref. [183]) on thread immensional modeling of pool boiling of nanofluids could be of interest going forward.

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