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# *Article* **Detecting Neolithic Burial Mounds from LiDAR-Derived Elevation Data Using a Multi-Scale Approach and Machine Learning Techniques**

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**Abstract:** Airborne LiDAR technology is widely used in archaeology and over the past decade has emerged as an accurate tool to describe anthropomorphic landforms. Archaeological features are traditionally emphasised on a LiDAR-derived Digital Terrain Model (DTM) using multiple Visualisation Techniques (VTs), and occasionally aided by automated feature detection or classification techniques. Such an approach offers limited results when applied to heterogeneous structures (different sizes, morphologies), which is often the case for archaeological remains that have been altered throughout the ages. This study proposes to overcome these limitations by developing a multi-scale analysis of topographic position combined with supervised machine learning algorithms (Random Forest). Rather than highlighting individual topographic anomalies, the multi-scalar approach allows archaeological features to be examined not only as individual objects, but within their broader spatial context. This innovative and straightforward method provides two levels of results: a composite image of topographic surface structure and a probability map of the presence of archaeological structures. The method was developed to detect and characterise megalithic funeral structures in the region of Carnac, the Bay of Quiberon, and the Gulf of Morbihan (France), which is currently considered for inclusion on the UNESCO World Heritage List. As a result, known archaeological sites have successfully been geo-referenced with a greater accuracy than before (even when located under dense vegetation) and a ground-check confirmed the identification of a previously unknown Neolithic burial mound in the commune of Carnac.

**Keywords:** LiDAR; Digital Terrain Model; Multi-scale Topographic Position; machine learning; Random Forest; visualisation techniques; Neolithic burial mound

### **1. Introduction**

Since the early 2000s, Airborne LiDAR remote-sensing technology has become an important tool for locating and monitoring cultural heritage sites in large or hard-to-access areas. High-density and high-precision LiDAR point clouds are processed to generate terrain models that are then used to detect and characterise archaeological evidence through the analysis of morphological or topographic anomalies [1–3].

To enhance the interpretation of subtle landforms from Digital Terrain Models (DTMs), archaeologists have relied on common visualisation techniques (VTs), including hillshade, slope, or colour-casted models derived from DTMs. More recently, advanced VTs, such as principal component analysis (PCA) of hillshades, sky-view factor, and openness models have been developed and successfully used to improve visual detection of archaeological remains. The main limitation

of these approaches is that they depend on empirical parameters (such as orientation or radius) and thus bias analyses of archaeological structures (or topographic anomalies) of specific sizes or morphologies [4]. The increasing development and complexity of these VTs can make the manipulation of LiDAR-derived models confusing and their interpretation subjective by non-expert users.

Along with the visual interpretation approach, an increasing number of automatic or semi-automatic feature-detection methods have been developed to address the issues involved in using LiDAR datasets to reveal archaeological remains. Object-based image analysis [5] and template matching [6] applied to DTMs or VTs has been used to automatically detect archaeological structures. While effective, this method requires defining a prototypical structure (for template matching) or characteristic spatial attributes (size, shape, orientation, specific VT value, etc.) to classify objects. This information is difficult to define for heterogeneous structures, especially for thousands of years old remains that have been altered throughout the ages.

In this article, we focus on the use of airborne LiDAR data to detect megalithic funeral structures in the region of Carnac, the Bay of Quiberon, and the Gulf of Morbihan (France). We developed an innovative approach that combines multi-scale topographic analysis of the LiDAR-derived model, as a new VT, with a machine learning method to produce a probability map to support archaeological prospections and accompanying field surveys.

### *1.1. Archaeological Context*

The French Atlantic coast, especially the Gulf of Morbihan, maintains traces of some of the most emblematic evidence left by our forebears during the Neolithic period [7,8]. The Neolithic funeral structures in the Carnac region, dating from 4500–7000 years ago, have been particularly affected by time, especially through natural erosion and anthropomorphic modifications. Some features, of multiform nature (burial mounds or tumuli, dolmens, cairns), have been significantly reduced in size or even completely levelled. Although these megalithic structures in Morbihan can be seen as isolated individual elements, they have a complex organisation that structured the Neolithic landscape [9]. Monuments were deliberately erected in precise locations and reflect an organised signature [10]. Situated in specific topographic contexts and usually dominating their environment, the funeral structures were most likely positioned to be visible from long distances [11]. Topographic analysis, especially based on a high-resolution terrain model, thus becomes one way to examine individual monuments and also the potential spatial organisation of a wider archaeological landscape [12].

### *1.2. Terrain Visualisation Techniques*

VTs applied to LiDAR-derived DTMs are widely used for archaeological interpretation [2,13–17]. VTs enhance topographical information by generating illustrative and interpretable representations of the relief through raster-based calculations. Many common VTs can be calculated with the open tool Relief Visualisation Toolbox [15,17] (Figure 1).

Not commonly defined as VTs but as topographic metrics to automate landform classification [18], the topographic position index and deviation from mean elevation (DEV) [19] are also inherently scale-dependent (e.g., a rocky outcrop on a valley bottom is dominating at the local scale but is dominated at a broader scale). The multi-scale approach recently developed by Lindsay et al. [20] combines DEV metrics calculated at multiple scales, which overcomes the scale-dependent disadvantage of the commonly used VTs. Developed for geomorphological applications, this approach seems effective for topographic analysis, and we believed that it could be adapted to interpret high-resolution DTMs for archaeological applications.

### *1.3. Machine Learning and Classification Techniques*

Supervised machine learning algorithms, such as Random Forest (RF), Support Vector Machine (SVM), or Multilayer Perceptron (MLP), are commonly used to solve classification problems [21]. Based on a training data set containing observations of known categories, the model is trained and then used to predict the category in which a new observation belongs.

 $RF$  is especially adapted to solve high-dimensionality problems.  $As$  an ensemble classifier,  $\overline{a}$ RF provides a classification score calculated from classification results of the forest's individual and independent decision trees. Each tree is generated from a random selection of features/variables and observations. This output can be used to generate a probability map, which is preferred to binary classification for computer-aided feature detection in archaeology. In addition to the probability map, RF also identifies the relative importance of features during classification, which can be useful in understanding the classification process [22,23]. RF is robust and effective, even with unbalanced data, and easier to implement than SVM [23]. The progress of an observation as it is being classified is also easier to follow with RF than with MLP, which is often considered a black box.  $\alpha$  is in prediction than  $\beta$  in progress of an observation as it is being classified is



**Figure 1.** Visualisation techniques calculated using the Relief Visualisation Toolbox [24]. **Figure 1.** Visualisation techniques calculated using the Relief Visualisation Toolbox [24].

### **2. Materials and Methods 2. Materials and Methods**

### *2.1. Study Area 2.1. Study Area*

The megalithic landscape of Carnac extends 40 km along the southern coast of Brittany (France), The megalithic landscape of Carnac extends 40 km along the southern coast of Brittany (France), from the Etel River in the west to the Rhuys Peninsula in the east (Figure 2). The area is home to 519 from the Etel River in the west to the Rhuys Peninsula in the east (Figure 2). The area is home to 519 known Neolithic sites currently selected for inclusion on the UNESCO World Heritage List. These sites known Neolithic sites currently selected for inclusion on the UNESCO World Heritage List. These must not be perceived as individual or single monuments, but as an integral part of the landscape with inter-relations based on their topographical positions or co-visibility. The megalithic monuments (i.e., burial mounds, single standing stones, stone circles, alignments of standing stones) follow structural and functional patterns such as "alignment and stone circle" or "alignment and stone circle and burial mound". Thus, even though some are barely perceptible due to their degraded stone circle and burial mound". Thus, even though some are barely perceptible due to their degraded conditions, archaeologists have grouped some of the 519 sites into 26 sub-areas to understand these conditions, archaeologists have grouped some of the 519 sites into 26 sub-areas to understand these patterns. Two of these sub-areas, Kerlescan and Lann Granvillarec, both located in the Carnac region, patterns. Two of these sub-areas, Kerlescan and Lann Granvillarec, both located in the Carnac region, were selected for detailed analysis for two reasons. First, they contain all of the types of Neolithic were selected for detailed analysis for two reasons. First, they contain all of the types of Neolithic remains known in the study area and all of the main structural and functional patterns identified. remains known in the study area and all of the main structural and functional patterns identified. Second, they have contrasting environments: Lann Granvillarec is a densely forested area with both Second, they have contrasting environments: Lann Granvillarec is a densely forested area with both deciduous and coniferous vegetation, while Kerlescan is mainly an open area with little vegetation. deciduous and coniferous vegetation, while Kerlescan is mainly an open area with little vegetation.



Figure 2. Topographic and bathymetric relief of the region of Carnac, Bay of Quiberon, and Gulf Morbihan, as well as the LiDAR coverage used in the study and the locations of Neolithic of Morbihan, as well as the LiDAR coverage used in the study and the locations of Neolithic archaeological sites and the Lann Granvillarec and Kerlescan sub-areas. archaeological sites and the Lann Granvillarec and Kerlescan sub-areas.

## *2.2. LiDAR Data 2.2. LiDAR Data*

The study was based on Airborne LiDAR data acquired with an Optech Titan bispectral LiDAR The study was based on Airborne LiDAR data acquired with an Optech Titan bispectral LiDAR sensor. The survey was performed in March 2016, immediately before the end of the off-leaf season sensor. The survey was performed in March 2016, immediately before the end of the off-leaf season to to ensure maximum signal penetration through the canopy. ensure maximum signal penetration through the canopy.

For the survey, the system was set for multi-echo recording, and specifications were defined For the survey, the system was set for multi-echo recording, and specifications were defined (Table 1) to reach a combined nominal point density of 14 points/m<sup>2</sup> (7 points/m<sup>2</sup> per channel). The nominal point density is estimated for a non-overlapping area, considering only the most recent  $\overline{a}$ echo. Full waveform information was not recorded during the flight. The data were delivered as

an unclassified 3D point cloud in LAS format (v1.2), with files organised by channel and flight line and compressed into LAZ files using LASzip software.



**Table 1.** Specifications of the Airborne LiDAR of the study area.

### *2.3. The Method 2.3. The Method*

The method for processing LiDAR data consisted of several steps (Figure 3). The method for processing LiDAR data consisted of several steps (Figure 3).



**Figure 3.** Workflow of LiDAR data processing. **Figure 3.** Workflow of LiDAR data processing.

## 2.3.1. Pre-Processing of LiDAR Data 2.3.1. Pre-Processing of LiDAR Data

An iterative method was used to pre-process the LiDAR data by filtering ground points and An iterative method was used to pre-process the LiDAR data by filtering ground points and generating a high-resolution DTM to maximise the number of micro-relief features. All pre-generating a high-resolution DTM to maximise the number of micro-relief features. All pre-processing processing tasks (Figure 4) were performed with LASTools software [25]. tasks (Figure 4) were performed with LASTools software [25].



**Figure 4.** Pre-processing workflow of LiDAR data from raw point cloud data to the Digital Terrain **Figure 4.** Pre-processing workflow of LiDAR data from raw point cloud data to the Digital Terrain Model (DTM). Model (DTM).

LAZ files, organised by channel and flight line, were then merged and reprocessed in a tiling LAZ files, organised by channel and flight line, were then merged and reprocessed in a tiling  $(500 - 1.50)$ triangulation. Tiles were then spatially indexed to expedite the workflow. triangulation. Tiles were then spatially indexed to expedite the workflow. Out-of-range values were excluded based on the Z coordinate value of each point: outside the  $(500 \text{ m} \times 500 \text{ m})$  system. A 50 m buffer area was used to avoid boundary effects between tiles during

Out-of-range values were excluded based on the Z coordinate value of each point: outside<br>
Out-of-range values were excluded based on the Z coordinate value of each point: outside the valid range from  $-5$  m to 60 m, the point was labelled as "Noise". Isolated points were detected  $\frac{1}{10}$ Thus, points with 10 or fewer neighbouring points in the surrounding  $27 \text{ m}^3$  were labelled as noise and excluded from further processing. and excluded from further processing. using the lasnoise tool with a 1 m step (step\_xy and step\_z) and a minimum threshold of 10 neighbours.

A first iteration of ground filtering was performed using the lasground tool with the step A first iteration of ground filtering was performed using the lasground tool with the step parameter parameter set to 25 m. This setting provided coarse ground filtering (without micro-relief) and set to 25 m. This setting provided coarse ground filtering (without micro-relief) and excluded  $\frac{1}{2}$  above-ground features (building ground matrix  $\frac{1}{2}$  and  $\frac{1}{2}$  were denoted  $\frac{1}{2}$  were denoted  $\frac{1}{2}$ above-ground features (buildings and vegetation) well. Filtered ground points were labelled "Ground".

The lasclassify tool was used to classify non-ground points (above-ground features) into vegetation and building classes. All points more than 1.5 m from the ground and with a neighbouring vegetation and building classes. All points more than 1.5 m from the ground and with a neighbouring planarity factor of at least 0.15 were labelled as buildings. All points more than 1.5 m from the ground planarity factor of at least 0.15 were labelled as buildings. All points more than 1.5 m from the ground and with a neighbouring ruggedness factor of at least 0.4 were labelled as vegetation. The lasclassify tool was used to classify non-ground points (above-ground features) into and with a neighbouring ruggedness factor of at least 0.4 were labelled as vegetation.

A second iteration of ground filtering was performed using lasground with a smaller step (3 m)  $\frac{1}{10}$ to identify smaller topographic details. This iteration was run on all points, including those already classified as buildings, vegetation, or noise. This approach helped identify additional bare-ground  $\frac{1}{2}$ details (ground points) while ensuring that above-ground features did not interfere. details (ground points) while ensuring that above-ground features did not interfere. to identify smaller topographic details. This iteration was run on all points, including those already

Final ground points were used to generate a surface based on triangulated irregular network interpolation and gridded to a DTM with a 0.25 m ground sampling distance. The optimum resolution in the optimum resolution resolution was defined by calculating the nominal point spacing, equal to *√(1/PointDensity)* [26]. was defined by calculating the nominal point spacing, equal to <sup>√</sup> *(1/PointDensity)* [26]. Final ground points were used to generate a surface based on triangulated irregular network

# 2.3.2. Multi-Scale Topographic Analysis 2.3.2. Multi-Scale Topographic Analysis

by the integral image approach by Lindsay et al. [20]. Integral image transformation was applied to efficiently perform multi-scale analysis of DEV before integrating the results into a composite image  $\begin{bmatrix}\n\text{Ficure 5}\n\text{Ficure 5}\n\end{bmatrix}$ Multi-scale analysis of the LiDAR-derived DTM, the core of the method, was directly inspired (Figure 5).

 $\overrightarrow{F}$  The processing, detailed hereafter, was performed using the open-source Whitebox Geospatial Analysis Tools [27] and the available Maximum Elevation Deviation (multiscale) tool, coupled with a custom *R* script [28] to create the RGB composite image. a custom *R* script [28] to create the RGB composite image.



**Figure 5.** Multi-scale Topographic Position (MSTP) approach based on calculating an integral image **Figure 5.** Multi-scale Topographic Position (MSTP) approach based on calculating an integral image from the Digital Terrain Model and multi-scale statistical analysis of the deviation from mean from the Digital Terrain Model and multi-scale statistical analysis of the deviation from mean elevation.

Integral Image Transformation Integral Image Transformation

calculates the sum of values in a rectangular subset of a grid  $[29]$ . The value at any pixel  $(x, y)$  in calculates the sum of values in a rectangular subset of a grid [29]. The value at any pixel  $(x, y)$  in the integral image (*ii*) is the sum of all the pixels above and to the left of  $(x, y)$ , inclusive, in the original image (*i*). Once the integral image is calculated, summing pixel values in any rectangular window, regardless of its size, requires only four array references, presented in the following Equation (1): regardless of its size, requires only four array references, presented in the following Equation (1): An integral image (or summed-area table) is a data structure and algorithm that efficiently

$$
\sum_{x=x_a}^{x_b} \sum_{y=y_a}^{y_b} i(x, y) = ii(x_b, y_b) - ii(x_{a-1}, y_b) - ii(x_b, y_{a-1}) + ii(x_{a-1}, y_{a-1})
$$
\n(1)

It allows for rapid calculation of the sum (Figure 6) and thus the mean, especially within a large It allows for rapid calculation of the sum (Figure 6) and thus the mean, especially within a large moving window (kernal) approach [20]. moving window (kernal) approach [20].

A single integral image can be used to sum values within an entire range of window sizes. This characteristic enables a multi-scale approach based on integral images to the analysis of topographic metrics.



**Figure 6.** Example of an integral image. Summing the values within any rectangular window in original image requires only four values and three simple mathematical operations (two subtractions the original image requires only four values and three simple mathematical operations (two subtractions and one addition). and one addition).

### Calculating Topographic Deviation at Multiple Scales Calculating Topographic Deviation at Multiple Scales

The topographic DEV equals the difference between the elevation of each grid cell and the mean elevation of the local neighbourhood, divided by the standard deviation [19], as shown in Equation (2): Equation (2):

$$
DEV(D) = \frac{(Z_0 - \overline{Z}_D)}{\sigma_D} \tag{2}
$$

pixel of the window,  $\overline{Z}_D$  is the mean elevation in the window, and  $\sigma_D$  is the standard deviation pixel of the window,  $\mathbb{Z}_D$  is the mean elevation in the window, and  $v_D$  is the standard deviation of elevations in the window. The multi-scale approach was based on calculating multiple *DEV* raster layers from roving windows of different sizes. It was implemented efficiently using integral  $\overline{Z}$  image transformation  $(\overline{Z}$  was calculated from the integral image, while  $\overline{Z}$  was calculated from  $t$  the second-power integral image). image transformation (*Z<sub>D</sub>* was calculated from the integral image, while *σ<sub>D</sub>* was calculated from the second-nower integral image) where  $D$  is the size of the roving window (local neighbourhood),  $Z_0$  is the elevation of the central

Three scales of analysis were defined: micro, meso, and macro. Intra-scale analysis was performed for each scale. The *DEV* raster layer was calculated *n* times with a window size  $D_n$  ranging from  $D_{min}$  to  $D_{max}$  along the mathematical sequence  $D_n = D_{min} + (n-1)k$ , where k equals the incremental  $\epsilon_{min}$  to  $\epsilon_{max}$  along the mathematical sequence  $\epsilon_{in}$   $\epsilon_{min}$  ,  $\epsilon_{min}$  ,  $\epsilon_{min}$  ,  $\epsilon_{min}$  are incrementational step. The resulting raster layer at each scale was calculated using the maximum absolute DEV from the multiple intre-coole analyzer performed within the window size range defined using Equation (3).  $\mathbf{I}$  intra-scale analyses performed with the window size range defined using  $\mathbf{I}$ the multiple intra-scale analyses performed within the window size range defined using Equation (3):

$$
maximum DEV = max\{|DEV(D_{min})|, ..., |DEV(D_{max})|\}\tag{3}
$$

The window size range and incremental step of each scale are input parameters. The window size ranges were defined based on the size of the archaeological structures to be studied. As burial mounds are usually 10–100 m in size, and scale boundaries were defined at those sizes (Table 2):

	Window Size Range $[D_{min}; D_{max}]$		
Scale	In metres	In pixels (0.25 m resolution)	
micro	[1; 10]	$[3 \times 3; 41 \times 41]$	
meso	[10; 100]	$[41 \times 41; 401 \times 401]$	
macro	[100; 1000]	$[401 \times 401; 4001 \times 4001]$	

**Table 2.** The three scales of analysis and their window size ranges (in metres and pixels).

To avoid excessive calculations, the incremental step (*k*) of window size was set to create 11 intra-scale analyses for each scale using Equation (4) with *k* rounded to the nearest integer: intra-scale analyses for each scale using  $E$  rounded to the nearest integer:  $\mathcal{E}$ 

$$
k = \frac{(D_{min} - D_{max})}{10} \tag{4}
$$

For example, the *maximumDEV* raster for the macro scale (100–1000 m) was selected from 11 *DEV* rasters calculated with a 90 m step. The result of each *maximumDEV* was a raster layer with cell values that range from −3 to +3, which correspond to topographical positions that are lower or higher, values that range from −3 to +3, which correspond to topographical positions that are lower or higher, respectively, than those in their neighbourhood (Figure 7). respectively, than those in their neighbourhood (Figure 7).



**Figure 7.** Maximum deviation from mean elevation at the meso scale. **Figure 7.** Maximum deviation from mean elevation at the meso scale.

## MSTP Image, the Multi-Scale Image Composite MSTP Image, the Multi-Scale Image Composite

The three raster layers of maximum topographic deviation (*maximumDEV*<sub>*micro*</sub>, *maximumDEV*<sub>*meso*</sub>, maximumDEV<sub>*macro*</sub>) were converted into absolute values and scaled to the range 0–254. Results were then combined into a single RGB image called a Multi-scale Topographic Position (MSTP) image for visualisation and interpretation (Figure 8). The composite image is composed of the macro-scale, the macro-scale, meso-scale, and micro-scale results (in the red, green, and blue bands, respectively). meso-scale, and micro-scale results (in the red, green, and blue bands, respectively).

### 2.3.3. Implementing the Machine Learning Algorithm 2.3.3. Implementing the Machine Learning Algorithm

While the absolute value of *maximumDEV* was used to create the composite MSTP image, the original value of *maximumDEV* (positive or negative) defined the actual topographic position signature of each pixel. The value indicates whether the position is dominating (positive) or dominated (negative) in the specified neighbourhood. Based on the three scale deviation signature, an RF an RF algorithm was implemented in *R* software using the *Caret* package [30] to fit a model to algorithm was implemented in *R* software using the *Caret* package [30] to fit a model to automatically detect Neolithic burial mounds. The sampling plan, which was defined in a sub-area of Carnac (1 km<sup>2</sup>), included 50 data samples (Figure 9). Each sample was a 100 m<sup>2</sup> square (1600 pixels at 0.25 m resolution) whose location was selected using the Latin hypercube sampling method to ensure adequate representation of variability in the data [31]. The sample size of 100  $\text{m}^2$  was defined empirically based on the burial mound's minimum size. The sampling plan contained two labels ("burial mound", "not burial mound") that were cross-checked with on-site verification and archaeological reference "data from the French Regional Archaeological Service. Of the 50 samples, 12% were "burial mound and 88% were "not burial mound". unal mound") that were cross-checked with on-site verification and archaeological fere equation of variability in the sampling plan contained two faces (300 m2 mo



**Figure 8.** Interpretation of the Multi-scale Topographic Position image to identify topographic **Figure 8.** Interpretation of the Multi-scale Topographic Position image to identify topographic features and their multi-scale position.



Figure 9. Samples of "burial mound" and "not burial mound" selected using the Latin hypercube a to belief signature of 80,000 provided from a state of the state and the state interest. sampling method. For better visibility, samples are overlaid on the hillshaded terrain model. sampling method. For better visibility, samples are overlaid on the hillshaded terrain model.

A total of 80,000 pixel signatures were extracted from a stacked raster layer of three bands (maximumDEV<sub>micro</sub>, maximumDEV<sub>meso</sub>, maximumDEV<sub>macro</sub>). The signatures and associated labels ("burial mound", "not burial mound") were randomly divided into two parts to train and evaluate the model (70% training data, 30% evaluation data). The training data were used to construct a set of the New York of the New York of the New York of the New York of the probability (from 0 to 1) of the presence of the probability (from 0 to 1) of the probability (from 0 to 1) of the probability (from 0 topographic elem  $\pi$  according the burial model from  $\pi$ of 120 decision trees as a model for binary classification, as well as for generating a probability map. This map indicates the probability (from 0 to 1) of the presence of topographic elements with characteristics similar to those of the Neolithic burial mounds (0.5 is the value that separates "burial mound" from "not burial mound").

The model was evaluated using the validation dataset. A confusion matrix including "burial The model was evaluated using the validation dataset. A confusion matrix including "burial mound" and "not burial mound" classes was generated for accuracy assessment and for calculating mound" and "not burial mound" classes was generated for accuracy assessment and for calculating performance metrics such as Cohen's kappa coefficient [32] and precision and recall [33]. performance metrics such as Cohen's kappa coefficient [32] and precision and recall [33].

The model was then generalised to other regions in the study area to identify pixels considered as The model was then generalised to other regions in the study area to identify pixels considered potential Neolithic burial mounds without prior knowledge of the area. as potential Neolithic burial mounds without prior knowledge of the area.

#### **3. Results 3. Results**

### *3.1. Training the Model to the Kerlescan Sub-Area 3.1. Training the Model to the Kerlescan Sub-Area*

The known Neolithic funeral structures in the Kerlescan sub-area are clearly visible on its MSTP The known Neolithic funeral structures in the Kerlescan sub-area are clearly visible on its MSTP image (Figure 10). This is confirmed by statistical analysis of the samples ("burial mound" vs. "not image (Figure 10). This is confirmed by statistical analysis of the samples ("burial mound" vs. "not burial mound") (Figure 11). The signature of burial mounds from the three scales is singular and burial mound") (Figure 11). The signature of burial mounds from the three scales is singular and clearly separated from other terrain positions, particularly at meso and macro scales. clearly separated from other terrain positions, particularly at meso and macro scales.



**Figure 10.** Multi-scale Topographic Position image generated for the Kerlescan training sub-area **Figure 10.** Multi-scale Topographic Position image generated for the Kerlescan training sub-area (Carnac) as a colour composite image from macro-scale (red band), meso-scale (green band), and micro-scale analysis (blue band).

The statistical results (Figure 11) confirm that these monuments have a particularly dominating The statistical results (Figure 11) confirm that these monuments have a particularly dominating The statistical results (The statistical results of the statistical results of the statistical results of the statistical resu position within the neighbouring area at meso and macro-scales (the topographical context<br>
position within the neighbouring area at meso and macro-scales (the topographical context of the structure), but no significant difference in signature at the micro scale (micro-topography  $B_{\text{B}}$  on the ability to separate the two classes, as shown on the confusion matrix (Table 3), the confusion matrix (Table within the structure itself).

Based on the ability to separate the two classes, as shown on the confusion matrix (Table 3), the RF model trained on the Kerlescan sub-area performed well, with a Cohen's kappa coefficient of 0.98 and precision and recall metrics of 0.98 for the "burial mound" class.



**Figure 11.** Boxplots of the maximum topographic deviation of pixels "burial mound" and "not burial **Figure 11.** Boxplots of the maximum topographic deviation of pixels "burial mound" and "not burial mound" sample areas at micro, meso, and macro scales. A total of 80,000 pixel signatures (1600 pixels mound" sample areas at micro, meso, and macro scales. A total of 80,000 pixel signatures (1600 pixels  $\times$  50 samples) are used here. The class balance is 12% ("burial mound"), 88% ("not burial mound").

Table 3. Confusion matrix of the Random Forest classification, with true positive (tp), false negative (fn), and false positive (fp) values for the class "burial mound".



The results for Kerlescan are presented on the probability map (Figure 12) that shows the detected position of know Neolithic burial mounds and reflects the strong separation between the two classes, with only a few pixels (<1%) ranging from 0.3 to 0.7.  $d_{\text{rel}}$  and  $d_{\text{rel}}$  and  $d_{\text{rel}}$  and  $d_{\text{rel}}$  and reflects the strong separation between the two  $\epsilon$ 



**Figure 12.** Probability map of the Random Forest and Carnet of the Random Forest and Carnet of the Random Forest and  $\frac{1}{2}$  $\mathbf{r}$  is overlaid structures labelled. The map is overlaid on the hillshaded. The map is over **Figure 12.** Probability map of burial mounds (Kerlescan, Carnac) as an output of the Random Forest **Figure 12.** Probability map of burial mounds (Kerlescan, Carnac) as an output of the Random Forest classifier, with known New York and New York functional structures labelled. The map is over the hillshaded classifier, with known Neolithic funeral structures labelled. The map is overlaid on the hillshaded

MSTP analysis was applied to the Lann Granvillarec sub-area. As for Kerlescan, the MSTP MSTP analysis was applied to the Lann Granvillarec sub-area. As for Kerlescan, the MSTP (Figure 13) image visually provides topographic information that was not visible or barely visible on (Figure 13) image visually provides topographic information that was not visible or barely visible on the hillshaded DTM. Likewise, the funeral structures of Lann Granvillarec have a strong response at the hillshaded DTM. Likewise, the funeral structures of Lann Granvillarec have a strong response at meso and macro scales (indicated by their bright yellow colour). This is also true for the most levelled meso and macro scales (indicated by their bright yellow colour). This is also true for the most levelled monuments, which have subtle topographic prominence, such as Lann Granvillarec 3. monuments, which have subtle topographic prominence, such as Lann Granvillarec 3.



**Figure 13.** Multi-scale Topographic Position image calculated for Lann Granvillarec. The image is **Figure 13.** Multi-scale Topographic Position image calculated for Lann Granvillarec. The image is overlaid on the hillshaded terrain model with 30% transparency. overlaid on the hillshaded terrain model with 30% transparency.

 $T_{\rm eff}$  model trained on  $K_{\rm eff}$ The RF model trained on Kerlescan was applied to Lann Granvillarec, generating a probability map (Figure 14) without prior knowledge of the latter. Of the six Neolithic funeral structures in Lann Granvillarec known to the French Regional Archaeological Service (Drac/SRA), the model identified five with a probability higher than 0.9. The site that was not detected (Lann Granvillarec 5) was a nearly levelled barrow that was accidentally destroyed by recent house construction. Although it has completely disappeared, it is still recorded in the archaeological reference database of the Drac/SRA.

Other areas in the map show high probability values. Three are false positives, corresponding to recent anthropomorphic modifications of the terrain by construction in the past 30 years. One particular zone of high probability lies in the north-west section of Lann Granvillarec and has a morphology and orientation common to burial mounds (Figure 15). On-site verification by the Drac/SRA confirmed it as a previously unknown Neolithic funeral structure. It is approximately 70 m long, 30 m wide, 2 m high, and covered by deep maritime pine forest. Its centre shows signs of two orthogonal excavations (visible on the LiDAR), which could indicate that it was once partially excavated, either by unauthorised activities (looting) or scientific operations whose archives have been lost to history. Declared as a new archaeological entity by the Drac/SRA, the monument (named "Tumulus of Coët Cougam") is now recorded in the archaeological reference database and thus protected by administrative regulations of the Drac/SRA.



Figure 14. Probability map of burial mounds generated for Lann Granvillarec. The map is overlaid on the hillshaded terrain model with 30% transparency. the hillshaded terrain model with 30% transparency. the hillshaded terrain model with 30% transparency.



Figure 15. The "Tumulus of Coët-Cougam", previously unknown to the French Regional Archaeological Service (Drac/SRA), was detected by the method developed.

## **4. Discussion and Perspectives 4. Discussion and Perspectives**

#### $T_{\text{eff}}$  and  $T_{\text{eff}}$  and  $T_{\text{eff}}$  and  $T_{\text{eff}}$  by via barrain by time and  $T_{\text{eff}}$ *4.1. Comparing MSTP and Other VTs of the Burial Mound of Kerlescan 4.1. Comparing MSTP and Other VTs of the Burial Mound of Kerlescan*

The Tertre of Kerlescan, covered by vegetation, has been levelled mainly by time and anthropomorphic activities (agriculture/ploughing, archaeological excavations). Comparing VTs anthropomorphic activities (agriculture/ploughing, archaeological excavations). Comparing VTs<br>commonly used in archaeological contexts to the MSTP image (Figure 16), the latter highlights the topographical context and provides morphological information that was not visible or barely using standard VTs. visible using standard VTs.

Local Relief Model Slo Hillshading Azimuth : 315<sup>°</sup> Radius : 20 pixels Elevation: 35° **MSTP** image Neg. openness Pos. openness Directions: 16 Directions: 16 Radius : 10 pixels Radius : 10 pixels **FIRM MODER** Orthoimage **PCA** of Hillshading Sky-view factor Directions: 16 Radius : 10 pixels

**Figure 16.** Comparison of commonly used visualisation techniques and the Multi-scale Topographic **Figure 16.** Comparison of commonly used visualisation techniques and the Multi-scale Topographic Position (MSTP) image calculated from the LiDAR-derived Digital Terrain Model of the Tertre Kerlescan (Carnac). The orthoimage shows the vegetation that hides the monument. of Kerlescan (Carnac). The orthoimage shows the vegetation that hides the monument.

## *4.2. Advantages and Limitations of MSTP 4.2. Advantages and Limitations of MSTP*

The study has shown that the MSTP approach performs well for visual interpretation and automatic feature detection. As it focuses on the topographical context of structures rather semi-automatic feature detection. As it focuses on the topographical context of structures rather than the structures themselves, it seems particularly appropriate for the heterogeneous character than the structures themselves, it seems particularly appropriate for the heterogeneous character barrows. of Neolithic barrows.

In addition to semi-automatic detection, the visual interpretation offered by MSTP images In addition to semi-automatic detection, the visual interpretation offered by MSTP images complements the common relief VTs developed for archaeology. The latter are usually based on fixed complements the common relief VTs developed for archaeology. The latter are usually based on fixed scales of analysis (e.g., using a single predefined radius to calculate relief metrics), while MSTP scales of analysis (e.g., using a single predefined radius to calculate relief metrics), while MSTP images states of analysis (e.g., asing a single predefined radials to calculate reflect incrites), while the H images<br>show topographic details from local to broad perspectives due to their integral image transformation transformation (and the first multi-scale approach). Even when the distribution of used and the state of used alone, they have a state of used alone, they h (an effective multi-scale approach). Even when MSTP images are not used alone, they can provide  $\epsilon$ . useful archaeological evidence, as demonstrated in Lann Granvillarec.

Despite their advantages for visualisation and interpretation, MSTP images, like most VTs, do Despite their advantages for visualisation and interpretation, MSTP images, like most VTs, do not not provide topographic measurements. Pixel values in an RGB array are not elevations or slopes. A provide topographic measurements. Pixel values in an RGB array are not elevations or slopes. A DTM provide topographic measurements. I fact values in an ROD analy are not exercise to provide the topographic measurements. I fact is still required to comprehensively explore the topographical context. In addition, DEV values (stored into absolute values of the values as positive and usefully nothing numbers) mast be converted into absorbe whates before they can be scaled to 0–254 and used as red, green, and blue bands. This makes it impossible to distinguish bumps in this makes it impossible to distinguish bumps from holes based only on MSTP colour. Although this limitation can be avoided by blending other<br>discussion of the workflow. This can be avoided by blending other as positive and negative floating numbers) must be converted into absolute values before they can be layers (Figure 17), it adds another processing step to the workflow.



Figure 17. Multi-scale Topographic Position (MSTP) image at 1 m resolution (a), and slope model at 0.25 m resolution (b). The resulting combined image (c) provides the topographical context (the entire monument) and local micro-relief (e.g., the cist). monument) and local micro-relief (e.g., the cist).

#### *4.3. RF Classifier and Futur Perspectives 4.3. RF Classifier and Futur Perspectives*

The RF technique, which has been used in remote sensing since the early 2000s, was chosen as The RF technique, which has been used in remote sensing since the early 2000s, was chosen as the classification algorithm for this study, for its simplicity of implementation, robustness, and its capacity to predict probabilities [23,34,35]. The challenge we faced, which was to detect the features of the Neolithic burial mounds, once performed through the multiscale topographic analysis, appeared to be fairly simple. As shown in the results section, the monuments have a particularly dominating position within the neighbouring area at meso and macro scales (i.e., the topographical context of the structure). The class separability is so high that the RF classifier expectedly performed well with a Cohen's kappa coefficient of 0.98 and a precision and recall metrics of 0.98 for the "burial mound" class.

Recently developed Deep Learning (DL) techniques, such as the convolutional neural network (CNN), have shown to be more effective than other classifiers for solving complex image processing tasks [36,37]. However, they require high-performance computing and expensive hyperparameter searches, tuning, and testing [37]. Our objective was to develop a straightforward, yet efficient methodology combining visualisation techniques and supervised feature detection, easily reproducible by archaeologists. Considering the performance of the RF classifier in this specific study, and therefore the low potential of improvement of the classification accuracy, we did not evaluate the CNN's performance. Nevertheless, in a broader context (different archaeological structures and/or areas with different environmental conditions), the use of CNN could be considered and implemented for evaluation and comparison to RF. For example, future work could focus on the use of a deep convolutional autoencoder (DCAE). Such a strategy, successfully applied for synthetic aperture radar (SAR) image classification [38], could possibly be adapted to automatically extract features that represent morphological or topographic anomalies from LiDAR-based elevation data.

#### **5. Conclusions**   $L<sub>1</sub>$  data are widely used for archaeological prospection; however, the use of  $M<sub>2</sub>$ **5. Conclusions**

LiDAR data are widely used for archaeological prospection; however, the use of MSTP analysis has not been explored for archaeological applications. The preliminary results presented in this article have shown that this approach combined with machine learning techniques can provide useful results  $\mu$  possibilities. and possibilities:

• A pertinent and innovative VT for using a LiDAR-derived DTM in archaeology morphology) of inventoried structures

- The ability to help archaeologists improve descriptions (geographic location and extent, morphology) of inventoried structures
- A support for archaeological prospection (through visualisation/interpretation of MSTP images)
- A step towards semi-automatic detection by incorporating machine learning (RF) algorithms

Although the method was developed on two test areas, the tools and processing workflow are sufficiently operational to study the entire LiDAR dataset covering the Carnac area. Additional terrain surveys are required to completely evaluate the method developed, which may require adjusting the process and refining the model using additional ground-checked samples.

The site-as-points current database offers variable accuracy over the entire "UNESCO area". Most site positions actually correspond to land parcel centroids. The use of LiDAR and the proposed method provides a way to improve the documentation of the sites. Beyond the UNESCO project, this study was carried out within the French Regional Archaeological Service (Drac/SRA), whose objective is to continuously enrich the inventory of archaeological sites to ensure the protection of this heritage.

Although this study focused on archaeological remains in Morbihan, the method developed will be explored in the future to extend the scope of application to a wider range of structures and a variety of archaeological contexts. Additionally, state-of-the-art classification techniques such as Deep Learning (DL), i.e., convolutional neural networks (CNNs), will be evaluated against the Random Forest classifier. Indeed, CNN frameworks like Caffe, Computational Network Toolkit (CNTK), and Torch could be employed at the pixel level via sliding window scanning to produce a confidence map similar to the one we generated for this study.

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**Author Contributions:** All authors conceived and designed the study. Thierry Lorho provided part of the in situ data and description of the archaeological context. Alexandre Guyot and Laurence Hubert-Moy defined the methodology. Alexandre Guyot processed the data. The results were examined by Alexandre Guyot, Thierry Lorho and Laurence Hubert-Moy. All authors contributed to the writing and approved the final manuscript.

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