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Lattice and Valence Electronic Structures of Crystalline Octahedral Molybdenum Halide Clusters-based Compounds, Cs$_2$[Mo$_6$X$_{14}$] (X = Cl, Br, I), Studied by Density Functional Theory Calculations

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Abstract

The electronic and crystal structures of $\text{Cs}_2[\text{Mo}_6\text{X}_{14}]$ ($\text{X} = \text{Cl}, \text{Br}, \text{I}$) cluster-based compounds were investigated by density functional theory (DFT) simulations and experimental methods such as powder X-ray diffraction (XRD), ultraviolet-visible (UV-Vis) spectroscopy, and X-ray photoemission spectroscopy (XPS). The experimentally determined lattice parameters were in good agreement with theoretically optimized ones, indicating the usefulness of DFT calculations for the structural investigation of these clusters. The calculated band gaps of these compounds reproduced those experimentally determined by UV-Vis reflectance within an error of a few tenths of an eV. Core-level XPS and effective charge analyses indicated bonding states of the halogens changed according to their sites. The XPS valence spectra were fairly well reproduced by simulations based on the projected electron density of states (PDOS) weighted with cross-sections of Al $K_{\alpha}$, suggesting that DFT calculations can predict the electronic properties of metal-cluster-based crystals with good accuracy.

**Keywords:** octahedral cluster; molybdenum halide; DFT calculation; XPS; electronic structure
Introduction

Octahedral metal cluster complexes, \([M_6L^j_8La^a_6]^{n-}\) (M = Mo, W, or Re; L^j = inner ligand; L^a = apical ligand), have attracted much attention, being regarded as building blocks for the construction of unique solid state inorganic and hybrid organic/inorganic compounds\(^1\,^2\) and nanostructures\(^3\,^4\) exhibiting interesting chemical and physical properties.\(^5\) As the size of these complexes is much larger than that of mononuclear ones, they can crystallize with various large inorganic (e.g., Cs\(^+\)) and molecular organic counter cations.\(^5\) Indeed, the combination of these metal cluster complexes and organic molecules enables the design of numerous functional structures, such as meso-scale structured materials\(^6\) and highly dimensional supramolecular assemblies.\(^7\)

An interesting feature of such metal-cluster-based compounds is the tunability of their properties by choosing an appropriate combination of M, L^j, and L^a\(^8\,^9\,^10\,^11\) or by crystallization with various counter cations.\(^12\) For example, some of these compounds show electric conductivity or superconductivity,\(^13\,^14\) while those with a relatively large band gap energy (\(E_g\)) show useful luminescence,\(^15\,^16\) photocatalytic,\(^17\,^18\,^19\) and redox properties.\(^20\) Numerous studies on nanostructure synthesis have been conducted to enhance the useful functions of these cluster compounds.\(^21\,^22\,^23\,^24\,^25\,^26\) In particular, \([Mo_6X^j_8X^a_6]^{2-}\) (X = Cl, Br, I) complexes have been widely studied because of their broadband red luminescence under UV or blue light illumination.\(^28\) Highly efficient phosphors emitting red light under excitation with blue light-emitting diodes (LEDs) are very important in solid-state lighting devices. Hence, the optimization of chemical compositions and structures of these compounds is promising for their applications as phosphors. In fact Kitamura and his
related group have developed novel metal-cluster-based compounds with high luminescence efficiency through modification of cluster’s chemical composition.\textsuperscript{29,30}

An effective exploration strategy of these complex systems involves the utilization of theoretically predicted composition-structure-property relationships. One of the earlier studies on the molecular orbital (MO) calculation of $[\text{Mo}_6\text{Cl}_{14}]^{2-}$ cluster was reported by Cotton in 1978.\textsuperscript{31} After that electronic properties of the metal cluster complexes such as chemical state and absorption energy have been calculated everywhere since 1990.\textsuperscript{32–36} However, most of those studies were based on MO calculations, where neither the presence of counter cations nor lattice periodicity were considered and electronic structures of spatially isolated and electrically charged metal cluster complexes were calculated, although it is reasonable to expect that exchange of counter cations should cause changes in atomic arrangements and effective charge of the complexes. Hence, in order to investigate electronic structure and structural stability of the metal-cluster-based compounds in crystalline form, it is necessary to perform electronic structure calculations based on crystalline periodicity with charge neutrality. Furthermore, most of those calculations were performed using classical functionals, such as the Hartree-Fock approximation. Thus, the utilization of updated density functional theory (DFT), e.g., the generalized gradient approximation (GGA),\textsuperscript{37} and consideration of lattice periodicity including counter cations is needed for more accurate predictions of composition-structure-property relationships in metal cluster complexes.

In this context, we have recently studied the crystal structure of $\text{Cs}_2[\text{Mo}_6\text{Cl}_{14}]$\textsuperscript{38} using plane-wave-based DFT calculations to examine the applicability of DFT for reproducing the structural and electronic features of metal-cluster-based crystalline compounds. As a result, it was shown
that the accuracy of conventional DFT is sufficient to predict formation energy differences between polymorphs of crystalline Cs₂[Mo₆Cl₁₄], implying that DFT calculations can be a useful tool for exploring metal-cluster-complex-based solid systems. Hence, we have attempted to predict the optical properties of metal-cluster-based compounds using updated DFT calculations.

This study describes DFT calculations on Cs₂[Mo₆X₁₄] (X = Cl, Br, I), aiming to accurately reproduce the effects of halogen substitution using the GGA functional. To examine the consistency between experimental observations and theoretical predictions, the observed lattice parameters were compared with the theoretically optimized ones. Furthermore, the reproducibility of theoretically predicted electronic structures was examined by comparison with experimentally observed X-ray photoemission (XPS) spectra and $E_g$ values.

**Materials and methods**

**Sample preparation**

The metal cluster-based solid state ternary halides Cs₂[Mo₆X₁₄] (X = Cl, Br, I) were synthesized and purified using procedures reported elsewhere.³⁸⁻⁴⁰ After purification, all samples were heated at 150 °C for 1 h in a glove box filled with dry N₂ gas (< 0.1 ppm H₂O). In our previous study,³⁸,³⁹ expansion of lattice parameters of Cs₂[Mo₆Cl₁₄] due to insertion of water molecules from environmental humidity was detected and those inserted water molecules could be removed by heat treatment in dry ambient at 150 °C. Hence, similar dehydration treatment was performed to all the samples prepared in this study to observe intrinsic nature of pure Cs₂[Mo₆X₁₄] without influence of water molecule insertion.

**Characterization and analyses**
The crystal structures of the obtained powders were characterized by XRD using a RINT-Ultima III diffractometer (Rigaku Co. Ltd., Tokyo, Japan) with monochromatic Cu $K_\alpha$ radiation ($\lambda = 0.15418$ nm). The observed diffraction patterns were indexed assuming that the samples crystallized in the trigonal centrosymmetric $P\overline{3}1c$ space group. Finally, the lattice parameters of Cs$_2$[Mo$_6$X$_{14}$] were refined using the method of least squares.

The diffuse reflectance spectra of Cs$_2$[Mo$_6$X$_{14}$] in the near-UV to near-infrared (near-IR) range were measured using a SolidSpec-3700 spectrophotometer (Shimadzu Corp., Tokyo, Japan) equipped with a BaSO$_4$ integrating sphere. Both core-level and valence band range XPS spectra of samples were obtained using a $\Sigma$-probe spectrometer (Thermo Fisher Scientific K.K, Yokohama, Japan) equipped with a monochromated Al $K_\alpha$ X-ray source ($h\nu = 1486.6$ eV). The pass energy was set at 20.0 eV for all spectra, with the instrumental resolution of electron energy being $\sim$0.2 eV. Samples were attached on an adhesive tape containing carbon particles. When obvious charging under X-ray irradiation occurred, a charge neutralizer employing both Ar$^+$ ion and electron emitters was used to eliminate charging. All binding energies were calibrated with respect to the C 1$s$ peak of adventitious carbon at 284.6 eV. After subtraction of the spectral background using Shirley’s method, the observed spectra were fitted by mixed Gaussian-Lorentzian functions using the method of least squares to calculate the integrated peak intensities and relative shifts of peak positions.

**Computational methods**

All DFT calculations were performed for the trigonal form of Cs$_2$[Mo$_6$X$_{14}$] ($X = \text{Cl, Br, I}$), which belongs to the $P\overline{3}1c$ centrosymmetric space group, as shown in Fig. 1(a), with
structural optimizations performed by applying structural constraints to maintain \( \bar{P}_{3}1c \) symmetry. It should be noted that this simplified model was not perfectly compatible with the experimentally refined crystal structure of \( \text{Cs}_2[\text{Mo}_6\text{Br}_{14}] \). Indeed, as shown in Fig. 1(b), the XRD characterization of \( \text{Cs}_2[\text{Mo}_6\text{Br}_{14}] \) indicated splitting of Cs sites along the \( c \)-axis and the presence of interstitial Cs sites at \((0, 0, 0.25)\) with a 12% occupancy. However, the simplified model shown in Fig. 1(a) was adopted for DFT calculations of all \( \text{Cs}_2[\text{Mo}_6\text{X}_{14}] \) complexes (including \( \text{Cs}_2[\text{Mo}_6\text{Br}_{14}] \)) due to limited computational resources. The structural parameters used to construct the initial structural model are listed in Table S1.

All DFT calculations were performed with the CASTEP code utilizing the plane wave pseudo-potential method. The norm-conserving pseudo-potentials (NCPPs) were generated using the OPIUM code. The revised Perdew-Burke-Ernzerhof GGA functional for solid-state compounds (PBEsol) was employed for energy minimization using the Pulay density mixing scheme. The cell parameters and atomic coordinates were relaxed using a quasi-Newton method and the Broyden-Fletcher-Goldfarb-Shanno Hessian update scheme. Electron spin polarization was considered for all DFT calculations. The plane wave cut-off energy was set to 830 eV, a Monkhorst-Pack grid \((4 \times 4 \times 3 \text{ mesh})\) was employed for Brillouin zone sampling, and a \( 96 \times 96 \times 144 \) mesh was adopted for the fast Fourier transformation. The convergence tolerances were set to \( 5 \times 10^{-5} \) nm for atomic displacement, \( 5 \times 10^{-6} \) eV/atom for total energy, 0.1 eV/nm for maximum interatomic force, and 0.02 GPa for pressure. The effective charges of constituent elements were estimated using two methods, i.e., Mulliken and Hirshfeld population analyses.
To compare the observed spectra with calculated results, additional simulations of optical and electronic spectra were performed. Optical absorption spectra were simulated by computing inter-band transition probabilities using the results of DFT calculations. The number of $k$-points involved in the simulation of optical properties was set to 21 per irreducible Brillouin zone. Valence band XPS spectra were also simulated by assuming a previously reported photoionization probability.

**Results and discussion**

**Structural analyses**

The observed XRD patterns shown in Fig. 2 were identified to be the trigonal phase as previously reported in references.\(^38-40\) However, for the sample with $X = \text{Cl}$, some peaks (denoted by arrows in Fig. 2), not assignable to $\text{Cs}_2[\text{Mo}_6\text{Cl}_{14}]$, were found. As previously reported,\(^38\) these extra peaks were from the secondary phase(s) crystallizing during synthesis and/or purification. The secondary phase was assigned to be $\text{Cs}_2[\text{Mo}_6\text{Cl}_{14}]\cdot\text{H}_2\text{O}$ as reported in a separate report.\(^39\) As the fraction of this secondary phase in the currently prepared sample should be negligibly small, we assume that the obtained results represent the characteristics of the trigonal $\text{Cs}_2[\text{Mo}_6\text{Cl}_{14}]$ phase. The refined lattice parameters of each sample, listed in Table 1, were almost identical to those reported in literature,\(^38-40\) being only slightly smaller. This deviation was attributed to the removal of volatile impurities, such as water related molecules. We previously reported that insertion of water molecules from ambient condition into the trigonal lattice of $\text{Cs}_2[\text{Mo}_6\text{Cl}_{14}]$ caused slight expansion of the lattice volume, and the water impurities could be removed by heating in an atmosphere of dry $\text{N}_2$, along with contraction of lattice volume.\(^38\) Hence, the samples prepared in this study are assumed to be very close to their intrinsic states.
The results of structural optimization and energy minimization converged well for all calculations, with the optimized lattice parameters being close to experimental values, as listed in Table 1. The calculated lattice parameters were well-matched with the experimental ones along the $a$-axis, being somewhat longer along the $c$-axis. We note that the overestimation of lattice parameters is due to a general tendency of the GGA functional. The detailed optimized lattice structures and fractional positions of all atoms in the lattice are summarized in Table S2 in the Supporting Information. These parameters are also consistent with the values reported in literature, indicating that the DFT structural optimization was successful, and the lattice structures were consistently reproduced by DFT calculations employing the PBEsol functional.

**Electronic structures**

The valence band structure of Cs$_2$[Mo$_6$X$_{14}$] varied with X, as seen from the PDOS of Cs$_2$[Mo$_6$X$_{14}$] (Fig. 3) obtained using the PBEsol functional after structural optimization. As up-spin and down-spin orbitals were identical, this figure shows the total PDOS profiles, featuring a summation of up- and down-spin orbitals. As can be seen, the Mo 4$d$ states were dominantly found around the valence band maximum (VBM), while the valence $p$-orbitals of X were distributed in the relatively deeper parts of the valence band. In particular, the valence $p$-states of X's were located in deeper parts of the valence band compared to those of X's. Moreover, the $s$-orbitals of X in the semi-core region (> 9 eV) showed similar behavior: the $s$ states of X's were deeper than those of X's. These results indicate that the chemical states of X's and X's are obviously different. In addition, the energy dispersion of valence electrons also varied with X. For instance, the energy dispersion of the valence $p$-orbitals of X's obviously changed with X.
(Fig. 3). Indeed, the population of X p-orbitals within VBM increased with the atomic number of X. Moreover, the dispersion of valence X p-orbitals seemed being broader with the increase of the atomic number of X. These valence band structure changes are reflected in the results of charge analyses shown in Table S3. The charge of X became more positive with increasing atomic number, mirrored by the charge of Mo becoming more negative. These results indicate that Mo–X bonds are highly ionic for X = Cl and less ionic for X = Br and I. Although the results of charge analyses suggest changes in chemical bonds between Mo and X, the calculated charge values seem to be inconsistent from the viewpoint of experimental chemistry. Namely, the positively charged X and negatively charged Mo atoms do not correspond to the intuitively expected results, since Mo and X are usually considered as a cation and anions, respectively. Such inconsistencies between intuitive and calculated results might be due to the charge analysis methodology adopted in this study, implying that the PDOS obtained by projection of the total electron distribution to the assumed atomic orbitals should feature a similar problem. Considering the difficulties in evaluating reasonable effective charges, the characteristics of Mo–X bonds are discussed below in terms of real-space orbital population distribution.

Figure 4 shows the highest occupied molecular orbital (HOMO) of Cs2[Mo6X14]. For X = I, the HOMO was dominated by Mo 4d and I 5p states at Xa sites (1p-5p). On the other hand, for X = Cl and Br, the HOMO featured contributions from the p-states of Xi. In particular, the HOMO of Cs2[Mo6Cl14] was dominated by Mo 4d and Cl 3p states at Xi (Cl3p). Note that the HOMO of Cs2[Mo6Br14] was intermediate between that of Cs2[Mo6Cl14] and Cs2[Mo6I14]. These results indicate that the electronic structure of the valence band (VB) of Cs2[Mo6X14] obviously changes with X despite the structural similarity.
The valence band structures of $\text{Cs}_2[\text{Mo}_6\text{Cl}_{14}]$ and $\text{Cs}_2[\text{Mo}_6\text{I}_{14}]$ are shown in Fig. 5 to investigate the effect of X in $\text{Cs}_2[\text{Mo}_6\text{X}_{14}]$. As seen in this figure, the electronic bands within the VB are classified into bundles. As the electronic states of every cluster are highly localized, every band possesses a small dispersion in $k$-space, which is the reason behind the formation of bundles. Thus, the observed electronic structure resembles the energy levels of isolated molecules. As seen from Fig. 5, the energetic order of the bundles was fairly independent of X; for instance, $\Phi_D$ and $\Phi_E$ of $\text{Cs}_2[\text{Mo}_6\text{I}_{14}]$ resembled $\Phi_4$ and $\Phi_5$ of $\text{Cs}_2[\text{Mo}_6\text{Cl}_{14}]$, respectively. However, the number of bands in the $\Phi_A$–$\Phi_E$ bundles in $\text{Cs}_2[\text{Mo}_6\text{I}_{14}]$ and that of $\Phi_1$–$\Phi_5$ in $\text{Cs}_2[\text{Mo}_6\text{Cl}_{14}]$ equaled 28 and 22, respectively, implying that several bands located above $\Phi_E$ in $\text{Cs}_2[\text{Mo}_6\text{I}_{14}]$ had energies below that of $\Phi_5$ in $\text{Cs}_2[\text{Mo}_6\text{Cl}_{14}]$. Indeed, $\Phi_F$ and $\Phi_6$ show different numbers of bands and dissimilar energy dispersions. Another typical difference between $\text{Cs}_2[\text{Mo}_6\text{Cl}_{14}]$ and $\text{Cs}_2[\text{Mo}_6\text{I}_{14}]$ can be found in bundles located relatively deep in the valence band. Both $\Phi_{14}$ and $\Phi_O$ bundles are close to the bottom of the valence band and consist of 12 electron bands. However, the energy dispersion of $\Phi_{14}$ is obviously narrower than that of $\Phi_O$.

Differences in the electronic band structure of $\text{Cs}_2[\text{Mo}_6\text{Cl}_{14}]$ and $\text{Cs}_2[\text{Mo}_6\text{I}_{14}]$ are likely due to the variable degree of Mo-X hybridization. Since Fig. 5 indicates that the energy dispersion of all bundles was wider for $\text{Cs}_2[\text{Mo}_6\text{I}_{14}]$ than for $\text{Cs}_2[\text{Mo}_6\text{Cl}_{14}]$, the electrons in $\text{Cs}_2[\text{Mo}_6\text{Cl}_{14}]$ are presumably more strongly localized than those in $\text{Cs}_2[\text{Mo}_6\text{I}_{14}]$. This understanding is consistent with the variation of orbital shapes shown in Fig. 6. The wave functions in $\text{Cs}_2[\text{Mo}_6\text{Cl}_{14}]$ are highly localized on all atoms, and the Mo–Cl bonds seem to be highly ionic. In support of this, the valence orbital overlap of Cl and Mo is negligibly small, as shown by the iso-surfaces of
electron orbitals. In contrast, the electron orbitals in $\text{Cs}_2[\text{Mo}_6\text{I}_{14}]$ show covalent bond character. For instance, the electron orbital involved in $\Phi$O is located at the center of the Mo–I bond, and all orbital distributions are not homogeneous, but rather anisotropic, as seen in $\Phi$I, $\Phi$K, and $\Phi$M. Another characteristic feature found in $\text{Cs}_2[\text{Mo}_6\text{I}_{14}]$ is the hybridization of $\text{I}^i$ and $\text{I}^a$, as exemplified by $\Phi$K. The difference between $\Phi$14 and $\Phi$O is also interesting. As mentioned above, $\Phi$14 showed a very narrow energy dispersion compared to that of $\Phi$O. Typical orbital distributions of bands involved in $\Phi$14 and $\Phi$O are compared in Figs. 6(o) and (p). All Cl$i$ atoms contribute nearly equally to every electron orbital in $\Phi$14, while the contribution of I$i$ atoms to electron orbitals of $\Phi$O differ from each other. This is an indication that the electron orbitals of $\text{Cs}_2[\text{Mo}_6\text{I}_{14}]$ possess a strong directionality, which is characteristic of covalent bonds. Indeed, the calculated total electron density in $\text{Cs}_2[\text{Mo}_6\text{Cl}_{14}]$ showed a spherical distribution centered at every Cl, while that in $\text{Cs}_2[\text{Mo}_6\text{I}_{14}]$ was distorted from spherical shape (Fig. S1). Hence, it was concluded that Mo–X bonds become more covalent with increasing halogen atomic number.

Reproducibility of typical electronic spectra

Figure 7 compares calculated and observed optical absorption spectra. Herein, experimental spectra were obtained from the observed diffuse reflectance shown in Fig. S2 using the KM function. The calculated spectra were obtained by applying Gaussian broadening with 0.05 eV in width. The observed and calculated absorption edges agreed within an error of less than 0.2 eV, indicating that the calculated $E_g$ well reproduced the experimental values. It has been suggested that $E_g$ calculated by conventional DFT methods tends to be smaller than the experimentally obtained values. However, for this system, the calculated $E_g$ showed good agreement with experimental observations. It should be also noted that the HOMO-LUMO gaps evaluated in the other study employing a molecular orbital method were much wider than the
experimental values of $E_g$. For instance, the HOMO-LUMO gap for $X=\text{Cl}$ evaluated by the molecular orbital calculation was reported to be 3.3 eV in the reference.\textsuperscript{63} The comparison of present results with experimental results and the other reported calculations indicates that the corresponding energy band structure calculations based on DFT are appropriate for predicting band gap energies in $\text{Cs}_2[\text{Mo}_6X_{14}]$ systems.

It has to be reminded that we have employed energy band structure calculation involving lattice periodicity. The most definite difference between the previous studies\textsuperscript{31–36} using the cluster calculation based on molecular orbital concept and present study is that present one dealt with neutral lattice with crystalline periodicity. As this study is based on crystalline lattice, effective charge of the metal cluster complex and counter cation, i.e., Cs, varied with chemical compositions as described above. Hence the effective charge of the metal cluster complexes could be converged into reasonable values. We suppose that this is the most significant merit of this study where the lattice periodicity has been considered. Indeed the accordance between experimental and calculated absorption spectra is good news for researchers investigating the electric and optical properties of metal-cluster-based compounds, since DFT simulation based on lattice periodicity is useful for material design, e.g., obtaining compounds with the desired $E_g$ by substitution of $X$ by another halogen ($X'$) to form $\text{Cs}_2[\text{Mo}_6(X, X')_{14}]$. Namely, we can expect that prediction of the stable structure and physical properties of metal complex compound with various counter cation is possible with plane wave DFT calculations based on lattice periodicity.

The observed XPS core-level spectra of $\text{Cs}_2[\text{Mo}_6X_{14}]$ are shown in Fig. 8. The core-level spectra of halogens featured two doublets, denoted $P_1$ and $P_2$. Since these doublets originated from spin-orbit coupling, profile fitting was performed assuming the presence of two different halogen species. Indeed, the presence of two halogen ion components in XPS spectra has been
reported,\textsuperscript{64–66} with these two peaks attributed to $X^a$ and $X^i$. The results of peak fitting are summarized in Table 2. The integrated intensity ratio of $P_1$ and $P_2$ ($S_1/S_2$) ranged from 0.74 to 0.77, consistently corresponding to 0.75 ($= 6/8$), which is reasonably attributed to $X^a$ and $X^i$ in the $[\text{Mo}_6X^i_8X^a_6]^2^-$ complex. The energy difference between $P_1$ and $P_2$ ($E_{b2} - E_{b1}$) equaled 2.1 eV for $X = \text{Cl}$ and $\text{Br}$, being equal to 1.6 eV for $X = \text{I}$. As the current DFT study used pseudo-potential and not all-electron calculations, it was not possible to determine the orbital energies of the observed core levels. On the other hand, the above experimentally observed energy difference is comparable to the energy difference of semi-core states calculated by DFT. Based on the calculated DOS shown in Fig. 3, the values of $E_{b2} - E_{b1}$ estimated by DFT simulations equaled 2.1 eV for $X = \text{Cl}$, 2.0 eV for $X = \text{Br}$, and 1.7 eV for $X = \text{I}$. These estimated values were in agreement with the experimental ones within an error of 0.1 eV, providing further evidence that the results of DFT calculations were consistent with experimental observations. The results of the corresponding XPS studies also indicate that the variation of the electronic structure of $\text{Cs}_2[\text{Mo}_6X_{14}]$ with $X$ discussed above was a reasonable consideration. As displayed in Fig. 6(I), electron orbitals with contributions from $p$-orbitals of both $I^i$ and $I^a$ were found in the results of the DFT study on $\text{Cs}_2[\text{Mo}_6I_{14}]$. This indicates that the relatively small energy separation between the levels originating from $I^i$ and $I^a$ resulted in hybridization between $I^i$ and $I^a$.

Here, it should be noted that the variation of ionicity of halogen at $X^a$ and $X^i$ site indicated by DFT calculation enables us to explain observed reactivity of the metal cluster complexes. From the viewpoint of chemical reaction for elimination and exchange of halogens in the metal-cluster-based compounds, halogen at $X^a$ site in the complex with $X^i = \text{Cl}$ or $\text{Br}$ can be replaced by other halogens,\textsuperscript{67,68} but halogen substitution in $[\text{Mo}_6I_{14}]$-complex seems to be difficult. As the complex with $X = \text{Cl}$ and $\text{Br}$ possesses relatively strong ionicity as indicated by DFT calculation,
substitution of X\(^a\) site in [Mo\(_6\)Cl\(_{14}\)]- and [Mo\(_6\)Br\(_{14}\)]-complex should be allowed when the electric charge of X\(^a\) site is maintained. However, replacement of I at X\(^a\) site by other halogen is expected to be limited because relatively high electronegativity of Cl and Br is not compatible to covalent bond formed in [Mo\(_6\)I\(_{14}\)]-complex. Hence, we can conclude that DFT calculation which visualize characteristics of chemical bonds is very useful tool for understanding of the chemical reactivity of the metal cluster complex compounds.

In addition to core-level XPS, the observed valence band XPS spectra and calculated PDOS were also compared, as shown in Fig. 9. Herein, the calculated XPS spectra were obtained by multiplying the reported photoionization probability listed in Table S4 with the PDOS shown in Fig. 3. Details of the simulation method are described in the Supporting Information. The shape of the valence band spectrum of Cs\(_2\)[Mo\(_6\)X\(_{14}\)] showed an obvious dependence on X, indicating corresponding changes in the electronic band structure of Cs\(_2\)[Mo\(_6\)X\(_{14}\)]. Comparison of the observed and calculated spectra indicated that the spectral features in the observed spectra were well reproduced in the calculated ones, although the valence band widths of the former were much wider than those of the latter. Note that the presence of two peaks in the Cs 5\(p\) region of the observed spectra resulted from spin-orbital coupling, not being an indication of the presence of two different electronic states of Cs. In the observed spectra, the semi-core levels of X\(^i\) and X\(^a\) were not well resolved for X = Br and I due to the overlap of doublets resulting from spin-orbit coupling. However, it is evident that the energy separation between the semi-core states of Cl observed in the XPS spectrum was well reproduced in the calculated spectrum. Hence, we can safely conclude that the band structure of Cs\(_2\)[Mo\(_6\)X\(_{14}\)] was well reproduced by DFT. Accordingly, the above discussion on valence band electron orbitals obtained by DFT

15
calculations was meaningful, since the calculation results well reproduced the XPS and optical absorption spectra.

Conclusions

In this study, both experimental and theoretical characterizations were carried out to reveal the electronic structure of cluster-based \( \text{Cs}_2[\text{Mo}_6\text{X}_{14}] \) ternary solid state compounds. The calculated structural features (lattice parameters) and optical properties \( (E_g) \), as well as the calculated DOS of these compounds were consistent with the experimental results, indicating that DFT simulations are appropriate for reproducing and predicting the above properties. The results of DFT calculations indicated that the electronic structure of \( \text{Cs}_2[\text{Mo}_6\text{X}_{14}] \) solids depend on the nature of \( \text{X} \), although their crystal structures were fairly independent of the nature of \( \text{X} \). The most significant electronic structure change due to the variation of \( \text{X} \) was found to be the difference in the degree of hybridization of Mo–X bonds.

As the calculated results were in good agreement with experimental observations, the DFT technique is considered appropriate for the prediction of electronic and optical properties of \( \text{Cs}_2[\text{Mo}_6\text{X}_{14}] \) systems with various compositions. Hence, DFT can be a useful tool to explore the useful properties exhibited by \( \text{Cs}_2[\text{Mo}_6\text{X}_i^i\text{X}^a_6] \) with various elemental combinations, such as \( \text{Cs}_2[\text{Mo}_6\text{Cl}^i_8\text{I}^a_6] \), \( \text{Cs}_2[\text{Mo}_6\text{Br}^i_8\text{Cl}^a_6] \), etc., where \( \text{X}^i \) and \( \text{X}^a \) sites are occupied by different elements.
Figure 1. Schematic representation of the crystal structures of trigonal Cs$_2$[Mo$_6$X$_{14}$] belonging to the centrosymmetric $\bar{P}\overline{3}1c$ space group: (a) X = Cl, I; (b) X = Br. In (b), the additional Cs atom at position 2a occupies 12% of the site instead of partially occupying another Cs site at position 2c. Furthermore, the other Cs site close to the origin is split into two equivalent sites.
Figure 2. XRD patterns of Cs$_2$[Mo$_6$X$_{14}$]: (a) X = Cl, (b) X = Br, and (c) X = I. Arrows denote Cs$_2$[Mo$_6$Cl$_{14}$].H$_2$O.
Figure 3. PDOS of Cs$_2$[Mo$_6$X$_{14}$]: (a) X = Cl, (b) X = Br, and (c) X = I.
Figure 4. Electron orbital distribution of the highest occupied orbital in Cs$_2$[Mo$_6$X$_{14}$] for (a) X = Cl, (b) X = Br, and (c) X = I. The yellow clouds indicate iso-surfaces normalized at 0.08 e/Å$^3$, and the red and blue arrows indicate the clouds representing the contributions of X$^i$ and X$^a$, respectively.
Figure 5. Electron energy band structure of Cs$_2$[Mo$_6$X$_{14}$] in the valence band range for (a) X = Cl, (b) X = I. Every band was classified into bundles, e.g., $\Phi_1$, $\Phi_2$, $\Phi_3$, ..., $\Phi_n$ for X = Cl and $\Phi_A$, $\Phi_B$, $\Phi_C$, etc. for X = I. The numbers in parentheses show the number of bands involved in every bundle.
Figure 6. Iso-surface plot of typical electron orbitals in Cs₂[Mo₆X₁₄] for X = Cl and I. The figures (a), (c), (e)...(s) depict representative electronic orbitals of bundles Φ₄, Φ₅, Φ₆,...Φ₁₆ defined in Fig. 5(a) and the figures (b), (d), (f),...(t) exhibit representative electronic orbitals of bundles ΦD, ΦE, ΦF,...ΦQ defined in Fig. 5(b). Arrows indicate characteristic orbital shapes reflecting the chemical states of Mo–X bonds.
Figure 7. Calculated and observed absorption spectra of Cs₂[Mo₆X₁₄] (X = Cl, Br, I).
Figure 8. Core-level XPS spectra of Cs₂[Mo₆X₁₄]: (a) Cl 2p region for X = Cl, (b) Br 3p region for X = Br, and (c) I 3d region for X = I. P₁ and P₂ indicate the presence of two doublets.
Figure 9. Comparison between the observed and calculated XPS valence spectra of Cs$_2$[Mo$_6$X$_{14}$] for (a) X = Cl, (b) X = Br, and (c) X = I. Arrows denote matching spectral features in the observed and calculated profiles.
Table 1. Refined lattice parameters of trigonal Cs$_2$[Mo$_6$X$_{14}$] (X = Cl, Br, I) in hexagonal expression.

<table>
<thead>
<tr>
<th></th>
<th>Lattice parameter</th>
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<tr>
<td></td>
<td>$a$ / nm</td>
<td>$c$ / nm</td>
<td>$V$ / nm$^3$</td>
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<tr>
<td>Experimentally determined in this study</td>
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<tr>
<td>Cs$_2$[Mo$<em>6$Cl$</em>{14}$]</td>
<td>0.9789(1)</td>
<td>1.4195(3)</td>
<td>1.1779(1)</td>
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<td>Cs$_2$[Mo$<em>6$Br$</em>{14}$]</td>
<td>1.0156(2)</td>
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<tr>
<td>Cs$_2$[Mo$<em>6$I$</em>{14}$]</td>
<td>1.0794(2)</td>
<td>1.6249(5)</td>
<td>1.6394(3)</td>
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<tr>
<td>Calculated in this study</td>
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<tr>
<td>Cs$_2$[Mo$<em>6$Cl$</em>{14}$]</td>
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<td>1.475</td>
<td>1.227</td>
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<td>Cs$_2$[Mo$<em>6$Br$</em>{14}$]</td>
<td>1.014</td>
<td>1.550</td>
<td>1.380</td>
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<td>1.084</td>
<td>1.636</td>
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<td>Indicated in literature [38,40]</td>
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<td>1.6258(5)</td>
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Table 2. Spectral parameters ($E_b$ for peak position and $S$ for relative integrated peak intensity) of halogens in Cs$_2$[Mo$_6$X$_{14}$] (X = Cl, Br, I) obtained by profile fitting under the assumption that all core level profiles comprised two components (P$_1$ and P$_2$).

<table>
<thead>
<tr>
<th>X</th>
<th>Core level</th>
<th>P$_1$</th>
<th>P$_2$</th>
<th>$(E_{b2} - E_{b1}) / \text{eV}$</th>
<th>$S_1/S_2$</th>
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<tr>
<td>Cl</td>
<td>2$p$ 3/2</td>
<td>197.8</td>
<td>1090</td>
<td>199.9</td>
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<tr>
<td>Br</td>
<td>3$p$ 3/2</td>
<td>180.8</td>
<td>1730</td>
<td>182.9</td>
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<tr>
<td>I</td>
<td>3$d$ 5/2</td>
<td>619.0</td>
<td>7790</td>
<td>620.6</td>
<td>10520</td>
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ASSOCIATED CONTENT

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Author Contributions

All authors have given their approval to the final version of the manuscript.

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Notes

Any additional relevant notes should be placed here.

Supporting Information Available: Listings of crystal graphic parameters for theoretical calculation studies, the results for the effective charge analyses, contour map of electron density, experimental UV-Vis diffuse reflection data, and photoionization probability data.

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REFERENCES


Characterization of $\text{Cs}_2[\text{Mo}_6\text{X}_{14}]@\text{SiO}_2$ Phosphor Nanoparticles Based on Transition Metal Clusters ($\text{X} = \text{Cl}, \text{Br}, \text{and I}$). *Adv. Mater.* **2008**, 20, 143–148.


The electronic and crystal structures of Cs₂[Mo₆X₁₄] (X = Cl, Br, I) ternary cluster-based compounds were investigated by density functional theory (DFT) simulations and experimental methods. The experimentally refined lattice parameters were in good agreement with theoretical optimized ones. The calculated band gaps also reproduced those photo-spectroscopically determined within an error of a few eV. The X-ray photoemission valence spectra were fairly reproduced from projected density of state (PDOS) weighted with cross-sections of Al Kα.
Table of Contents graphic

For Table of Contents Only