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THE AVERAGED POTENTIAL GRADIENT APPROACH TO MODEL THE REJECTION OF ELECTROLYTE SOLUTIONS USING NANOFILTRATION: MODEL DEVELOPMENT AND ASSESSMENT FOR HIGHLY CONCENTRATED FEED SOLUTIONS

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Abstract

Some of the recent publications in nanofiltration modelling converge on the importance of dielectric effects and numerous models have been developed in order to take them into account. However several works reported lately in the literature suggest a screening of image

charges effect at high electrolyte concentration and the predominance of the Born effect, due to the change of dielectric constant inside the confined nanopore regarding that of the feed solution. In pursuit of an exhaustive and simple model for nanofiltration, a new approach is developed that account for both dielectric phenomena. Based on the Steric, Electric and Dielectric Exclusion (SEDE), the introduction of an average potential gradient approximation is shown to greatly improve the computational performance of the model without being detrimental to its predictive accuracy. The results obtained with this simplified model (SEDE-APG) are compared to the original SEDE model and an excellent agreement is obtained even in the case of electrolyte mixtures. Ultimately this model is confronted to experimental data of separation obtained for moderately to highly concentrated feed flows and exhibits promising results.

Keywords: nanofiltration; SEDE model; high concentration; average potential approach; dielectric effects

Introduction

Since 1970s, the field of pressure-driven separation techniques has been push forward by the increasing exigencies of efficiency, prevailing as a cheap, sustainable and reliable solution for separation or concentration operations [1]. The growing need for a technology coupling the high retention rate of reverse osmosis (RO) with the moderate pressure difference used in ultrafiltration (UF) led to the development of nanofiltration (NF), a promising technique which already found applications at industrial scales [2].

The majority of the nanofiltration membranes are polyamide thin-film composite (TFC) [3]. The preparation of those membranes is mainly operated through interfacial polymerisation (IP) on an appropriate microporous support, which is fixed on a woven or non- woven reinforcing layer. The IP is usually realised by in-situ polycondensation on the microporous support [4].

Hence, several factors, inherent to the operating conditions, as well as the choice of the microporous support [5–7], are likely to affect the physic-chemical properties of the active layer. Therefore, the issue of characterisation of the polyamide layer has been addressed in several publications [5,8–11] in order to improve the understanding of the selectivity and permeability processes through this layer.

Even though the rejection of ions can be convincingly modelled by a simple Donnan equilibrium approach in the case monovalent ion solution [12] or for sufficiently large pore [13], the high selectivity regarding multivalent ions, typically observed in the pore range of nanofiltration [14], remains poorly explained by this traditional approach which often relies in inconsistent fitting values for charge densities [15,16] or thickness over porosity ratio [17–19]. A convincing way to address these shortcomings could be to introduce the influence of dielectric effects. The impact of dielectric effect in ion exchange membranes has been firstly stressed by Glueckauf [20] before being roughly considered by Fane et al. [21] and further reviewed and analysed by Yaroshchuk [22], who pointed out its potential importance, as well as the difficulty to quantify its actual contribution. Later, the development of the DSPM&DE model by Vezzani and Bandini [14,23], on the basis of the DSPM model introduced by Bowen and co-workers [16,17,24,25], allowed to take into account the dielectric exclusion resulting from the difference between the dielectric constant of the membrane matrix and the one of the solution – considered as unique in the bulk and inside the confined nanopores. More recently, by developing a steric, electric and dielectric exclusion (SEDE) model, Szymczyk and Fievet added a stone to the edifice of dielectric effects modelling in nanofiltration processes [26]. It notably includes, in a coherent framework, exclusion resulting from the difference of dielectric constant between the bulk and the solution confined in the nanopores – the so-called Born effect –, and the one resulting from

the difference between the dielectric constant of the membrane matrix and of the electrolyte solution – the so-called image effect.

If the influence of the latter has already been submitted to specific theoretical investigations [22,27], the former, namely Born effect, has recently drawn more attention owing to the simplicity of its computation and its ability to accurately render specific behaviours observed in nanofiltration, and notably the high selectivity regarding multivalent ions. The works of Oatley et al. and, before, that of Bowen & Welfoot have been introducing a two parameter model assuming Born partition to be the only dielectric phenomenon involved at the pore interfaces [16,28–31]. Their approach, involving the study of rejection at the isoelectric point of the membrane and the assumption of screened image forces at high charge densities, has shown to be successful. However this latter assumption is only backed by qualitative considerations, and is all the more questionable as the charge of the membrane is compensated at the point of zero charge.

As a matter of fact, recent computer experiment confirmed the effect of nanoconfinment on the dielectric constant of water and aqueous solutions [32–35]. At the same time, the extensive studies carried out on the theoretical influence of image charges clearly stress their theoretical significance [22,26,27,36] and some experimental results also point towards the importance of taking the low dielectric constant of the membrane matrix into account [37]. Although the overlapping between dielectric and electrostatic effects makes it difficult to accurately assess the share of each in the rejection process, it is herein acknowledge that, *a priori*, the rejection mechanism is a conjunction of steric, electrostatic and dielectric effects.

Recognizing the need for a tool equally simple and exhaustive for NF modelling, this work explores a simplified approach to assess the actual rejection of electrolyte solutions considering the influence of dielectric effects. First, by considering the rejection of

electric field along the pore, that it is possible to linearly approximate the potential gradient. Consequently, a simplified model is deduced (SEDE-APG for Averaged Potential Gradient) and compared to the original SEDE model. The results obtained with the former show excellent agreement with those provided by the original model. Moreover it proves to be less resource consuming and faster in terms of computation. Ultimately this simplified model is confronted to experimental data from the literature in order to critically discuss the theoretical contribution of dielectric effects in nanofiltration prediction.

1. Theoretical background

NF membrane is assumed to be a matrix of identical pores, characterised by their half-size r_p and their thickness Δz as depicted in Fig. 1. The study of concentration polarisation being beyond the scope of this work, the external solution is assumed to be ideal and perfectly stirred, so that this phenomenon can be disregarded throughout the development of the model. The system considered is isothermal at 298K.

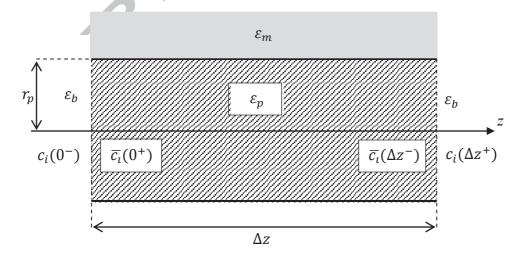


Figure 1. Representation of a pore of radius r_p and length Δz . ε_b denotes the relative permittivity of the bulk, therefore equal in the permeate and retentate, while ε_p is the relative

permittivity inside the pore and ε_m that of the membrane material (equal to 3 for polyamide materials [38]). $c_i(0^-)$ and $c_i(\Delta z^+)$ respectively denote the bulk concentration at the pore inlet and outlet, while $\overline{c_i}(0^+)$ and $\overline{c_i}(\Delta z^-)$ stand for that of the confined solution. The axial coordinate is z.

The pressure-driven transport of each ion i of charge z_i is investigated through the extended Nernst-Planck (ENP) equation. This one accounts for the diffusion of ions under a concentration gradient, their electromigration inside the pore due to the spontaneous formation of an electric field and their convection throughout the flow inside the membrane. By taking into account the hindrance factors for diffusion and convection, the ENP equation can be adapted to the specific case of a NF membrane [17,18,23,26,28,39–45]. At last, giving the negligible radial variation of the potential inside a pore of nanoscale [9,41,42,46–48], the local ion concentrations and electrostatic potential inside the pore can be radially averaged, leading to a one dimensional approximation of the aforementioned model:

$$j_{i} = -K_{i,d}D_{i,\infty}\frac{d\overline{c}_{i}(z)}{dz} - \frac{FK_{i,d}z_{i}D_{i,\infty}\overline{c}_{i}(z)}{RT}\frac{d\overline{\psi}(z)}{dz} + K_{i,c}\overline{c}_{i}(z)\frac{J_{v}}{A_{k}}$$
(1)

Where j_i is the molar flux density of the ion i, $D_{i,\infty}$ its diffusion coefficient at infinite dilution, z_i its charge number, c_i its concentration and $K_{i,d}$ and $K_{i,c}$ are respectively the diffusion and convection hindrance factors related to this ion, calculated using the approximate equations derived by Bungay and Brenner [49]. Besides, F stands for the Faraday constant, R for the ideal gas constant, R for the electric potential inside the pore while J_{ν} represents the permeate volume flux and A_k the membrane porosity.

The Poisson equation being dropped in the uniform approximation, it has to be replaced by the explicit electroneutrality condition inside the pores:

$$\sum_{i} z_{i} \overline{c_{i}}(z) + X(z) = 0 \quad \text{for } 0^{+} \le z \le \Delta z^{-}$$
(2)

where X(z) stands for the local volume fixed-charge density inside the pores.

It is worth mentioning that in Eq. (2) the fixed-charge density is considered to be homogeneous. Even though previous theoretical works have stressed the impact of inhomogeneous charge distributions on membrane rejection [46,50–53], this approximation remain a reliable way to predict the behaviour of a wide range of commercial membranes [54].

Considering the following intrinsic filtration condition:

$$j_i = \frac{J_v c_i(\Delta z^+)}{A_k} \tag{3}$$

The ENP equation (1), can be transformed to express the concentration gradient within the nanopore:

$$\frac{d\overline{c}_{l}(z)}{dz} = \frac{J_{v}}{K_{i,d}D_{i,\infty}A_{k}} \left(K_{i,c}\overline{c}_{l}(z) - c_{l}(\Delta z^{+}) \right) - \frac{z_{l}F\overline{c}_{l}(z)}{RT} \frac{d\overline{\psi}(z)}{dz}$$
(4)

Combining this latter equation (4) with the electronegativity condition (2), the expression of the electric field inside the membrane can be deduced:

$$E(z) = -\frac{d\overline{\psi}(z)}{dz} = -\frac{\sum_{i} \frac{z_{i} J_{v}}{K_{i,d} D_{i,\infty} A_{k}} \left(K_{i,c} \overline{c_{i}}(z) - c_{i}(\Delta z^{+}) \right)}{\frac{F}{RT} \sum_{i} \overline{c_{i}}(z) z_{i}^{2}} - \frac{\frac{dX(z)}{dz}}{\frac{F}{RT} \sum_{i} \overline{c_{i}}(z) z_{i}^{2}}$$
(5)

For the description of the Born effect, the approach used in this work is inspired from the model developed by Born to calculate the electrostatic energy involved in the solvation of a spherical ion characterised by its radius r_i and its valence z_i [55]. Adapting this result to the transfer of an ion from the bulk (dielectric constant ε_b) to the confined solution inside the nanopore (dielectric constant ε_p), the following relation is obtained:

$$\Delta W'_{i,Born} = \frac{(z_i q)^2}{8\pi \varepsilon_0 k_B T r_{i,cav}} \left(\frac{1}{\varepsilon_p} - \frac{1}{\varepsilon_b} \right) \tag{6}$$

where ε_0 is the vacuum permittivity and the prime sign is added to signify that the term is scaled on k_BT , k_B being the Boltzmann constant and T the operating temperature. Another notable difference with the original Born formula, is the use of the cavity radius, defined as the distance from the centre of the ion where the medium begins, instead of ionic radius, as proposed by Rashin and Honig [56]. The best fitting value for it is obtained by increasing respectively the covalent radius of cations and the ionic radius of anions by 7% (this might be explained by the phenomenon of dielectric saturation) [26].

It should be noticed that, for the sake of simplicity in this study, two distinct and uniform dielectric constants inside the bulk and the confined nanopore were considered. Although some attempts to account for the variation of the dielectric constant inside the nanopore already exist [22,28,29,57], the available experimental methods are not able to confirm the validity of those models and the recent computer simulation seem to refute them [32–35]. Moreover the unidimensional nature of the current NF models is hardly able to cope with the supposed variations of the constant inside the pore.

The solvation energy due to image forces (denoted $\Delta W'_{i,lm}$) is accounted for using the model developed by Yaroschuk [22] for slit-like pores:

$$\Delta W'_{i,Im(0^-|0^+)} = -\alpha_i ln \left[1 - \left(\frac{\varepsilon_p - \varepsilon_m}{\varepsilon_p + \varepsilon_m} \right) e^{-2\mu_{(0^-|0^+)}} \right]$$
 (8.1)

$$\Delta W'_{i,lm(\Delta z^-|\Delta z^+)} = -\alpha_i ln \left[1 - \left(\frac{\varepsilon_p - \varepsilon_m}{\varepsilon_p + \varepsilon_m} \right) e^{-2\mu_{(\Delta z^-|\Delta z^+)}} \right]$$
(8.2)

with:

$$\mu_{(0^-|0^+)} = \left(\frac{\varepsilon_0 \varepsilon_b RT}{2F^2 I}\right)^{-1/2} r_p \sqrt{\sum_i \frac{z_i^2 c_i(0^-) \Lambda_{i,(0^-|0^+)}}{2I}}$$
(9.1)

$$\mu_{(\Delta z^{-}|\Delta z^{+})} = \left(\frac{\varepsilon_{0}\varepsilon_{b}RT}{2F^{2}I}\right)^{-1/2} r_{p} \sqrt{\sum_{i} \frac{z_{i}^{2}c_{i}(\Delta z^{+})\Lambda_{i,(\Delta z^{-}|\Delta z^{+})}}{2I}}$$
(9.2)

$$\alpha_i = \frac{(z_i F)^2}{8\pi \varepsilon_0 \varepsilon_p RT N_a r_p} \tag{10}$$

It is worth noticing that the solvation energy model for cylindrical pore could as well be applied. We won't detail it here as it has been extensively described in existing literature [22,26,27]. Here $\Lambda_{i,(\Delta z^-|\Delta z^+)}$ and $\Lambda_{i,(0^-|0^+)}$ are the partitioning coefficient respectively at the pore entrance and outlet defined by the modified Donnan equations:

$$\frac{\overline{c_{i}}(0^{+})}{c_{i}(0^{-})} = \Lambda_{i,(0^{-}|0^{+})} = \phi_{i} \frac{\gamma_{i}(0^{-})}{\gamma_{i}(0^{+})} e^{-z_{i}\Delta\psi_{D,(0^{+}|0^{-})}} e^{-\Delta W'_{i,Born}} e^{-\Delta W'_{i,Im(0^{-}|0^{+})}}$$
(11.1)

$$\frac{\overline{c_i}(\Delta z^-)}{c_i(\Delta z^+)} = \Lambda_{i,(\Delta z^-|\Delta z^+)} = \phi_i \frac{\gamma_i(\Delta z^+)}{\gamma_i(\Delta z^-)} e^{-z_i \Delta \psi_{D,(\Delta z^-|\Delta z^+)}} e^{-\Delta W'_{i,Born}} e^{-\Delta W'_{i,Im(\Delta z^-|\Delta z^+)}}$$
(11.2)

where $\Delta\psi_{D,(0^+|0^-)}$ and $\Delta\psi_{D,(\Delta z^-|\Delta z^+)}$ account for the normalized Donnan potential respectively at the entrance and the outlet of the pore and ϕ_i denotes the steric partitioning, bounded between 0 and 1. The γ_i are the activity coefficients calculated according to the extended Debye-Hückel equation:

$$log(\gamma_i) = -\frac{Az_i^2\sqrt{I}}{1 + (Br_i\sqrt{I})}$$

$$q^2F$$
(12)

with

$$A = \frac{q^2 F}{\ln(10) \times 4\pi\sqrt{2} \left(\varepsilon_0 \varepsilon_r RT\right)^{3/2}} \tag{13}$$

$$B = F \sqrt{-\frac{2}{\varepsilon_0 \varepsilon_r RT}} \tag{14}$$

Where R is the ideal gas constant, q the elementary charge, ε_r the dielectric constant of the medium under consideration and I its ionic strength.

As this work focuses on NF of highly concentrated electrolyte solutions, the image charge effect has been neglected in the partitioning equations, which is justified by the screening of this dielectric effect at high concentration [22,26].

Over a first phase, the separation properties of the membrane are assessed through the intrinsic rejection rate:

$$R_i = 1 - \frac{c_i(\Delta z^+)}{c_i(0^-)} \tag{15}$$

As the concentration polarisation is neglected, for all the part concerning the model development it is also equal to the apparent rejection:

$$R_{app} = 1 - \frac{C_f}{c_i(0^-)} \tag{16}$$

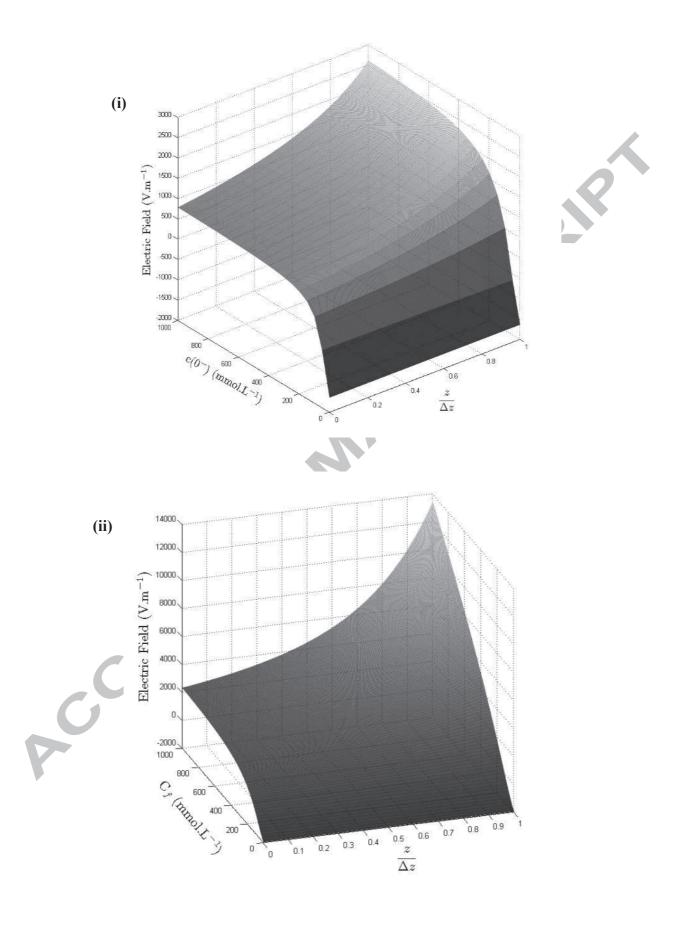
Where C_f is the feed concentration.

2. Model simplification

2.1. Preliminary studies on SEDE model

As mentioned in introduction, most of the traditional nanofiltration model consider an homogeneous charge density along the pore. Even though this assumption remains questionable in the general case, it proved to be a reliable assumption in numerous situations including, for example, the studies of ceramic membrane [39,58–60] or TFC membranes[28–30]. Moreover, the obvious difficulty to determine the fashion of the charge distribution inside pores measuring no more than a few nanometre, makes it the most convenient hypothesis to adopt. Homogeneous charge density models are therefore interesting for a relatively large category of membranes many commercially available models [61].

In order to simplify this model the evolution of the electric field along the pore has been compared for different electrolytes. Considering a uniform fixed charge of -10 mmol.L⁻¹, a dielectric constant of 40 for the confined solution, a pore radius of 0.43 nm and a thickness to porosity ratio of 5µm, the results obtained for simple salt solutions are shown in Fig. 2 and those for electrolyte mixture in Fig. 3. (the results for larger pores and lower fixed charge densities are presented in the Supporting Information, section 1)



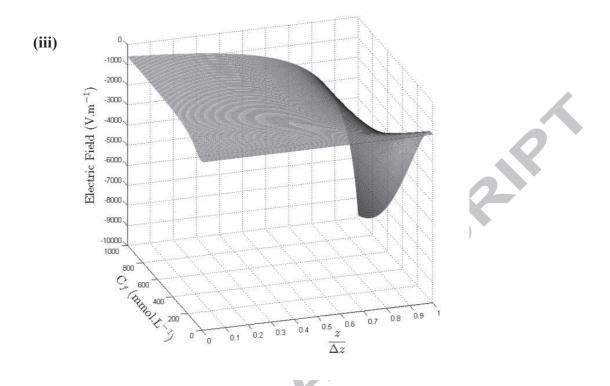
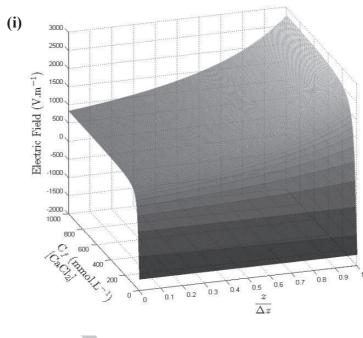


Figure 2. Representation of the electric field along the pore as a function of the concentration for different simple salt solutions. Figures (i), (ii) and (iii) respectively represents the electric field for NaCl, CaCl₂ and Na₂SO₄. The parameters chosen for the membrane are a pore radius of 0.43nm, a thickness over porosity ratio of 5 μ m and a dielectric constant inside the pore of 40. The volumetric flux is $J_{\nu} = 3.9 \times 10^{-5}$ m.s⁻¹.

The electric fields observed for different simple salt solutions exhibit remarkable differences. While all of them seems to present a relatively constant negative electric field at low concentration, their behaviour strongly diverge at high concentration, depending on the nature of the ions in solution. This is convincingly explained by the fact that, at higher concentration the diffusion potential is imposed by the fastest ion inside the pore. Indeed, at low concentration the negative electric field arises as to maintain the electroneutrality inside the pore, taking the sign of the homogeneous charge of the membrane into account. Therefore, in the case of a negatively charge pore cations are attracted inside the membrane, which causes a negative electric field to arise in order to drive the anions on the permeate side. However at

high concentration, the pore charge is quickly neutralized by the positive charges and a new regime is established in which the fastest ion is accumulated at the outlet of the pore. Therefore an electric field opposed to the sign of the fastest ion naturally arises in order to reverse this tendency. Following this reasoning the figure above are corroborated by the sequence of ions mobility $Cl > Na^+ > SO_4^2 > Ca^{2+}$.



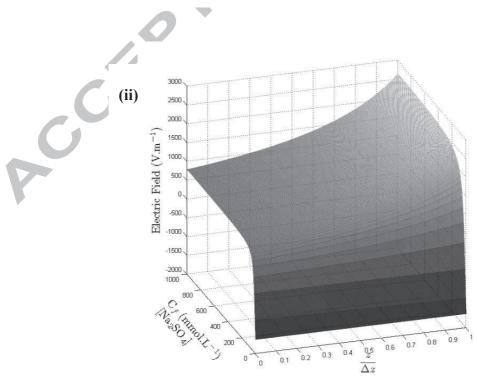


Figure 3. Representation of the electric field along the pore as a function of the concentration for different simple salt solutions. Figure (i) and (ii) respectively represents the electric field for an electrolyte mixture composed of NaCl and CaCl₂ and one of NaCl and Na₂SO₄. The parameters chosen for the membrane are a pore radius of 0.43nm, a thickness over porosity ratio of 5 μ m and a dielectric constant inside the pore of 40. The volume flux is $J_{\nu} = 3.9 \times 10^{-5}$ m.s⁻¹

The electric fields profiles along the pore for the electrolyte mixture considered are similar to each other. Besides, it is interesting to note the similarity with the electric field plotted in the case of NaCl. We can therefore deduce that the mechanism at stake in the formation of the electric field is similar with those described in the case of simple salt solutions. It is relevant to note that these observations on the evolution of the electric field are corroborated, at least partly, by the results of Vezzani et al. [23],

2.2. Model simplification

This preliminary study of the electric field for an homogeneous charge density along the pore exhibit a relatively constant negative electric field at small concentration. Based on those observations a simplification of the SEDE model is thereafter derived.

The idea is to average the electric potential gradient along the pore, in order to simplify the resolution of the concentration gradient (4):

$$\langle \frac{d\bar{\psi}}{dz} \rangle_z = \frac{1}{\Delta z} \int_0^{\Delta z} \frac{d\bar{\psi}(z)}{dz} dz = \frac{1}{\Delta z} \int_0^{\Delta z} d\bar{\psi}(z) = \frac{\Delta \bar{\psi}}{\Delta z}$$
(17)

Subsequently, the expression of the electric field in the transportation equation (5) has been replaced by its average value, leading to a simple first order linear differential equation for the concentration gradient inside the pore:

$$\frac{d\overline{c_i}(z)}{dz} = \left(\frac{Pe_i}{\Delta z} - z_i \frac{F}{RT} \frac{\Delta \overline{\psi}}{\Delta z}\right) \overline{c_i}(z) - \frac{1}{K_{i,c}} \frac{Pe_i}{\Delta z} c_i(\Delta z^+)$$
(18)

The latter equation, considering the normalised potential difference $\Delta \overline{\psi}_N = \frac{F}{RT} \Delta \overline{\psi}$ and given the boundary conditions (11.1) and (11.2) respectively applicable to the pore inlet and outlet, leads to the following solution (see the Appendix for the details):

$$\frac{c_i(\Delta z^+)}{c_i(0^-)} = \frac{\Lambda_{i,(0^-|0^+)} K_{i,c} (Pe_i - z_i \Delta \overline{\psi_N}) e^{(Pe_i - z_i \Delta \overline{\psi_N})}}{\Lambda_{i,(\Delta z^-|\Delta z^+)} K_{i,c} (Pe_i - z_i \Delta \overline{\psi_N}) - Pe_i (1 - e^{(Pe_i - z_i \Delta \overline{\psi_N})})}$$
(19)

And therefore, the rejection rate can be estimated as:

$$R_{i} = 1 - \frac{\Lambda_{i,(0^{-}|0^{+})} K_{i,c} (Pe_{i} - z_{i} \Delta \overline{\psi_{N}}) e^{(Pe_{i} - z_{i} \Delta \overline{\psi_{N}})}}{\Lambda_{i,(\Delta z^{-}|\Delta z^{+})} K_{i,c} (Pe_{i} - z_{i} \Delta \overline{\psi_{N}}) - Pe_{i} \left(1 - e^{(Pe_{i} - z_{i} \Delta \overline{\psi_{N}})}\right)}$$

$$(20)$$

Where Pe_i is the Peclet number for the ion i, equal to $(J_vK_{i,c}z_A)/K_{i,d}D_{i,\infty}$, the quantity z_A corresponding to the ratio of the membrane thickness over its porosity.

In the most general case of multi-ionic solutions, this model can be solved using the following process:

1. Determine the parameters of the model and calculate $\Delta W'_{i,Born}$ according to equation (6).

Calculate $\Delta \psi_{D,(0^+|0^-)}$, $\Delta W'_{i,Im(0^-|0^+)}$ and $\frac{\gamma_i(0^+)}{\gamma_i(0^-)}$. This can be achieved by solving the system formed by equations (8.1), (12) and (21). The latter is deduced as a combination of the electroneutrality equation (2) inside the pore and the boundary condition (11.1):

$$\sum_{i} z_{i} \Lambda_{i,(0^{-}|0^{+})} c_{i}(0^{-}) + X = 0$$
(21)

Calculate $\Delta \psi_{D,(\Delta z^-|\Delta z^+)}$, $\Delta W'_{i,Im(\Delta z^-|\Delta z^+)}$, $\frac{\gamma_i(0^+)}{\gamma_i(0^-)}$ and $\Delta \overline{\psi_N}$. This can be achieved by solving the system formed by (8.2), (12), (22). The latter is deduced by injecting the expression of $c_i(\Delta z^+)$ given by (19) in the electroneutrality conditions on the permeate side (22.1) and at the pore outlet (22.2):

$$\begin{cases}
\sum_{i} z_{i} \frac{\Lambda_{i,(0^{-}|0^{+})} K_{i,c} (Pe_{i} - z_{i} \Delta \overline{\psi_{N}}) e^{(Pe_{i} - z_{i} \Delta \overline{\psi_{N}})} c_{i} (0^{-})}{\Lambda_{i,(\Delta z^{-}|\Delta z^{+})} K_{i,c} (Pe_{i} - z_{i} \Delta \overline{\psi_{N}}) - Pe_{i} (1 - e^{(Pe_{i} - z_{i} \Delta \overline{\psi_{N}})}) = 0 \\
\sum_{i} z_{i} \frac{\Lambda_{i,(0^{-}|0^{+})} \Lambda_{i,(\Delta z^{-}|\Delta z^{+})} K_{i,c} (Pe_{i} - z_{i} \Delta \overline{\psi_{N}}) e^{(Pe_{i} - z_{i} \Delta \overline{\psi_{N}})} c_{i} (0^{-})}{\Lambda_{i,(\Delta z^{-}|\Delta z^{+})} K_{i,c} (Pe_{i} - z_{i} \Delta \overline{\psi_{N}}) - Pe_{i} (1 - e^{(Pe_{i} - z_{i} \Delta \overline{\psi_{N}})}) + X = 0
\end{cases} (22.2)$$

$$\sum_{i} z_{i} \frac{\Lambda_{i,(0^{-}|0^{+})} \Lambda_{i,(\Delta z^{-}|\Delta z^{+})} K_{i,c} (Pe_{i} - z_{i} \Delta \overline{\psi_{N}}) e^{(Pe_{i} - z_{i} \Delta \overline{\psi_{N}})} c_{i}(0^{-})}{\Lambda_{i,(\Delta z^{-}|\Delta z^{+})} K_{i,c} (Pe_{i} - z_{i} \Delta \overline{\psi_{N}}) - Pe_{i} (1 - e^{(Pe_{i} - z_{i} \Delta \overline{\psi_{N}})})} + X = 0$$
(22.2)

Calculate R_i using equation (20).

This simplified model using the averaged potential approximation is abbreviated as SEDE-APG. Its algorithm, presented in Fig. 4, is to be compared with that of the original model: as the nonlinear differential equation for the concentration gradient is dropped, the resourceconsuming iterative process on the RK4 algorithm is not needed anymore and a lot of computational resource is saved.

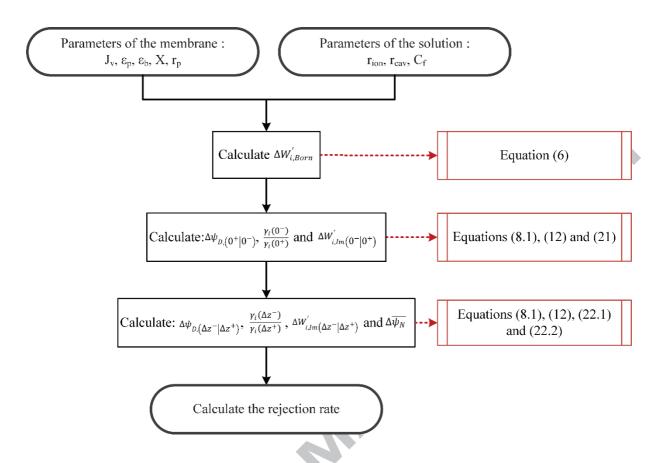


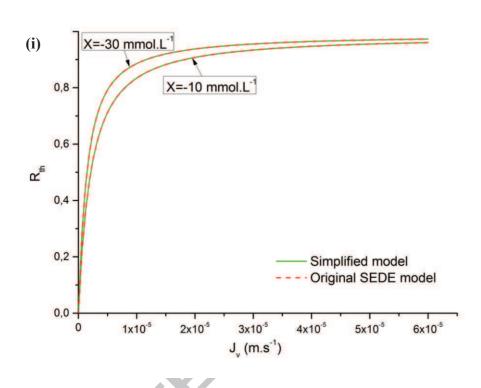
Figure 4. Algorithm of the SEDE-APG model

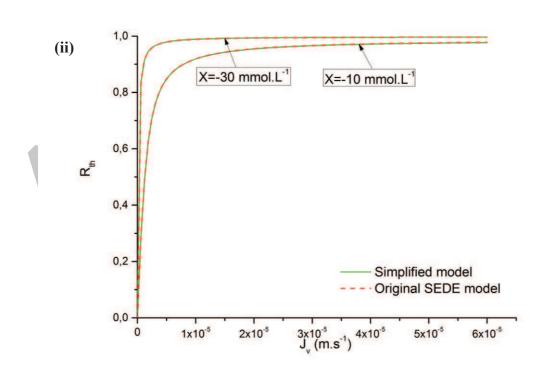
2.3. Model assessment

Using the SEDE-APG the rejections predicted for different moderately concentrated (0.1M to 0.2M) salt solutions were compared with the original SEDE model. Moreover, in order to stress the accuracy of the model at different charge densities, the rejection rate has been simulated for charges of -10 mmol.L⁻¹ and -30mmol.L⁻¹. The other parameters of the membrane chosen for simulations are a pore radius of 0.43 nm and a thickness over porosity ratio of 5 μm. The former corresponding to the characteristic of a NF-270 membrane [29], a typical commercial membrane, while the latter is an average value determined by Bowen and Mohammed from twenty-nine commercial NF membranes [62]. The dielectric constant of 40 for the inside of the nanopore, roughly correspond to that obtained by Oatley et al. [29]. The results are presented in Fig. 5 and Fig. 6. At this stage it is also important to stress that for

higher concentrations, the simplified model remain coherent with the original one in spite of the electric field variations arising along the pore (see Supporting Information). Later on

2.3.1. Single electrolytes solutions





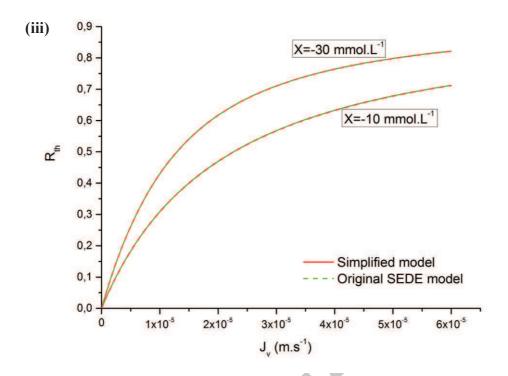


Figure 5. Comparison of the rejection rate against the volume flux using SEDE-APG and the original SEDE model. Figures (i), (ii) and (iii) respectively correspond to the rejections of CaCl₂, Na₂SO₄ and NaCl. Each of the solution is concentrated at 100 mmol.L-1. The membrane parameters are as described in the paragraph above.

Fig. 5 shows an excellent agreement between the two models. Therefore this new model establishes itself as a performant alternative to the current mechanistic models in the case of homogeneous charged pores.

Moreover, the simplicity of the SEDE-APG allows a better understanding and analysis of the mechanisms at stake in the rejection process. Indeed the direct expression of the rejection rate given by equation (20) makes this model an interesting tool to quantify the share of each phenomenon in the rejection process. This expression is however not accessible in the original SEDE model.

2.3.2. Electrolytes mixtures

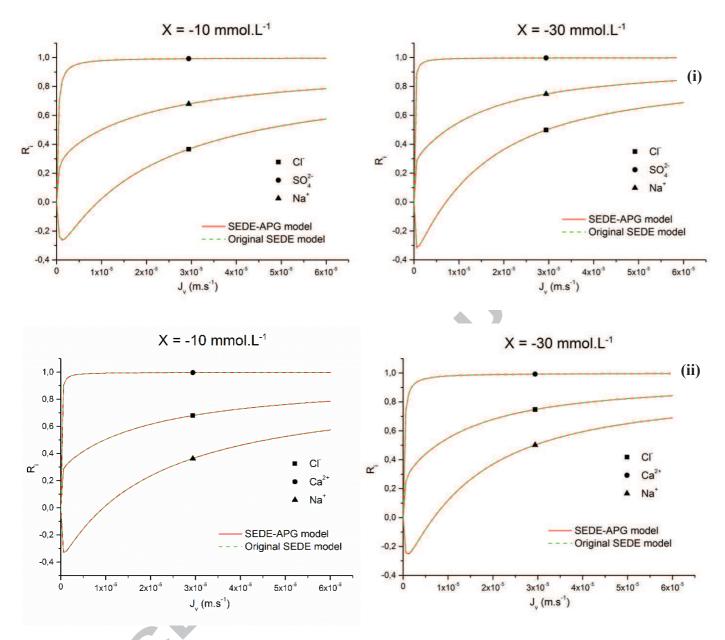


Figure 6. Comparison of the rejection rate against the volume flux using SEDE-APG and the original SEDE model. Figure (i) correspond to an electrolyte solution of 100 mol.L⁻¹ Na₂SO₄ and 200 mol.L-1 NaCl. Figure (ii) correspond to an electrolyte solution of 100 mol.L⁻¹ CaCl2 and 200mol.L⁻¹ NaCl. In each figure, the results are represented for charge densities of -10 mmol.L⁻¹ and -30 mmol.L⁻¹.

Fig. 6 confirm the good results obtained for single salt solution in the case of electrolyte mixtures. Here again the results show a quasi-perfect with the original model. It is worth

mentioning that the new model successfully predicts the phenomenon of negative rejection commonly observed in nanofiltration.

2.3.3. Computational performance

Besides from its simplicity and easier implementation, the computation speed is greatly reduced. Fig. 7 shows a diminution in computation time greater than 1 order of magnitude. Moreover, in the case of the simplified model, the computation time is less dependent of the complexity of the system considered.

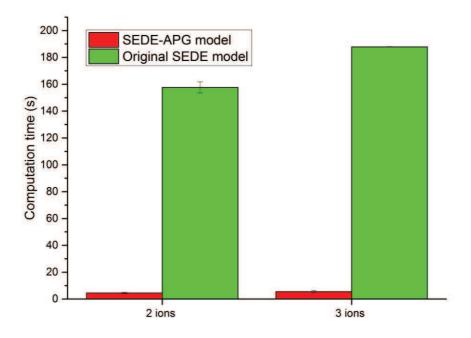


Figure 7. Computation speed of the different models, considering 2 ions and 3 ions mixtures.

3. Application

3.1. Data and methods

In order to prove the predictive potential of this simplified model, the work of Pérez-Gonzalez *et al.* [63] on the nanofiltration separation of SO_4^{2-} and Cl anions in desalination brines has been investigated using the SEDE-APG approach. For this purpose, the predictions of the simplified model were confronted to the experimental results proposed in the aforementioned study which considered model brines with a constant concentration of sodium sulphate of approximately 1M and a varying concentration of sodium chloride between 0.14M and 1.13M [63]. To compare the predictions with the experimental results, a least square objective function S_V has been used. It is defined as follow for n solutes corresponding to j data points:

$$S_{y} = \sqrt{\frac{\sum_{1}^{n} \sum_{1}^{j} (R_{obs} - R_{app})^{2}}{jn - 1}}$$
 (23)

Where R_{app} is the calculated apparent rejection from equation (16).

The characteristics of the membrane were taken from the literature. Several sources agree on an average pore size of 0.43nm [29,64,65] and a pure water permeability of $L_p = 3.75 \times 10^{-11}$ [64] for the NF270 membrane considered in this study, while the thickness to porosity ratio z_A has been determined by adopting the classical Hagen-Poiseuille flow approach [66]:

$$z_A = \frac{r_p^2}{8\eta L_p} = 0.69\mu\text{m}$$
 (24)

Where η is the dynamic viscosity of water at T.

It should be noted that the thickness to porosity ratio thus obtained is a dependent parameter, and is ten-fold smaller than the one obtained using SEM data in the original work of Perez-Gonzales et al. [63]. The approach chose in this paper aims at increasing the internal coherence of the model. Indeed, the original DSPM model, is known to suffer from

inconsistencies in the values of z_A which are found to change with the nature of the electrolyte solution.

The volumetric flux is related to the effective gradient by the following equation:

$$J_v = L_p(\Delta P - \Delta \pi) \tag{25}$$

Where ΔP is the applied pressure gradient and $\Delta \pi$ the osmotic pressure gradient. The osmotic pressure gradient is determined by the difference between the osmotic pressures in the retentate and the permeate estimated through the Van't Hoff law.

For this application the concentration polarisation has been taken into account, as the concentrations considered being relatively high. For this purpose, the mass transfer coefficient for each ion was assessed using the same correlation with the one proposed by the original paper:

$$k_m = \frac{D_{\infty}}{d_h} 0.3125 Re^{0.57} Sc^{1/3}$$
 (26)

Where d_h is the hydraulic diameter of the SEPA-CF membrane cell [67], Re the Reynolds number and Sc the Schmidt number.

The concentration polarisation has been calculated using the classical Spiegler-Kedem approach:

$$\frac{c_i(0^-) - c_i(\Delta z^+)}{Cf - c_i(\Delta z^+)} = e^{J_v/k_m}$$
 (27)

The values of charge densities used here correspond to those calculated by Pérez-Gonzalez *et al.* from the streaming potential measurements [63]. They are reminded in the table below:

| $\alpha = \frac{[Cl^-]}{[SO_4^{2-}]}$ | NaCl (M) | $X (mol.m^{-3})$ | | |
|---------------------------------------|----------|------------------|--|--|
| 1.7 | 0.14 | -265 | | |
| 5.1 | 0.42 | -459 | | |
| 10.2 | 0.85 | -649 | | |
| 13.6 | 1.13 | -750 | | |

Table 1. Charge densities deduced from streaming potential measurements for each model brines. Values taken from [63].

3.2. Results and discussion

Using the theoretical framework described above, the SEDE-APG model has been confronted to experimental results [63] by using three different approaches:

- (a) A full model approach (Donnan, steric, Born and image effects)
- (b) A Donnan, steric and Born effects approach (neglecting image effects)
- (c) A Donnan and steric effects only approach (neglecting both dielectric effects). This approach is similar to that of the original research paper. Here it aims at confirming the influence of the thickness to porosity ratio dependency on water permeability.

The results are presented in Fig. 8 below:

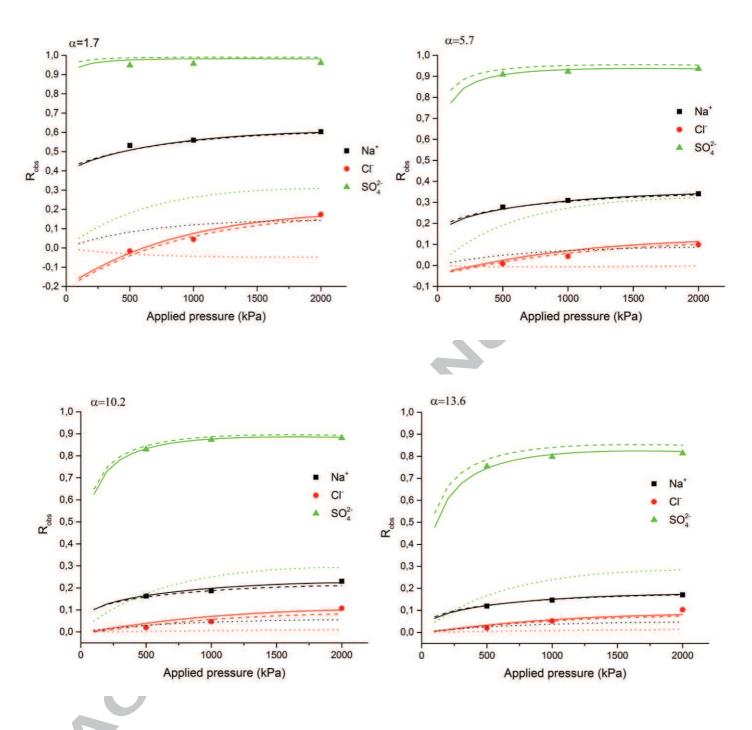


Figure 8. Experimental (symbols) and predicted ions rejections. The predicted ions rejections corresponding either to the approach (a) (dash lines ---), (b) (solid lines ---) or (c) (dot lines ---) described earlier.

The results and parameter used for the different approaches are consigned in Table 2.

| | Model | | | Parameters | | | | Results |
|-----|------------------------------------|---------------------------------------|-----------------|--|--------------------------|---------------|-----------------|----------------|
| | Donnan and steric effects | Born effect | Image effect | $\alpha = \frac{[Cl^-]}{[SO_4^{2^-}]}$ | X (mol.m ⁻³) | $arepsilon_p$ | \mathcal{E}_m | S _y |
| | | | | 1.7 | -265 | 53 | 3 | 0.026 |
| (a) | X | X | V | 5.1 | -459 | 56 | _3 | 0.016 |
| | | | X | 10.2 | -649 | 56 | 3 | 0.015 |
| | | | | 13.6 | -750 | 56 | 3 | 0.025 |
| (b) | | | | 1.7 | -265 | 43 | N/A | 0.021 |
| | | \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ | | 5.1 | -459 | 47 | N/A | 0.013 |
| | X | X | | 10.2 | -649 | 48 | N/A | 0.012 |
| | | | | 13.6 | -750 | 50 | N/A | 0.011 |
| (c) | | | | 1.7 | -265 | N/A | N/A | 0.52 |
| | | | | 5.1 | -459 | N/A | N/A | 0.43 |
| | X | | | 10.2 | -649 | N/A | N/A | 0.39 |
| | | | | 13.6 | -750 | N/A | N/A | 0.36 |

Table 2. Parameters used and results obtained for each approach (a), (b) and (c) described above.

It is worth mentioning that the dielectric constant of the polyamide matrix can hardly be considered as a fitting parameter as it is fixed to $\varepsilon_m=3$ corresponding to an established experimental data widely available in the literature [38]. However the shift in the dielectric constant of the confined medium is still relatively poorly understood. Recent computer experiments confirmed the phenomenon [32–35], but the no reliable method exists to quantitatively assess it or model it in the general case. Interestingly enough a recent computational study on a charged silica nanotube by Renou et al. [34] confirms that, at negative surface charges, the dielectric constant of a confined water solution could be smaller than that of the bulk solution.

From Fig. 8 it is clear enough that the Donnan/steric approach is not enough to predict the ions rejection when z_A is related to the water permeability. However fitting procedures of this parameter have proven to yield inconsistencies in its value [17–19], hence the need to take dielectric phenomena into account. The Table 2 confirms the good results from Fig. 8 for the model (a) and (b) which respectively deviate by no more than 2.6% and 2.1% from the experimental results. An interesting feature of the full model (a) is that the fitted dielectric constant of the confined medium remains relatively constant, while for the model (b) it is increasing along with the concentration. As far as NF modeling goes, a shift in concentration is often assumed to have no effect on the dielectric constant inside the pore, nevertheless it is probable that the presence of ions influence the orientation of water molecules inside the nanopore. To our knowledge this work is the first to clearly compare these two approaches together against the same experimental data. While they both seem relatively accurate, additional data on the confined solution would be necessary to conclude on one or the other approach.

Conclusion

By stressing that the electric field along the pore can confidently be averaged in the case of homogeneous charge distribution, the SEDE-APG model was developed and assessed. This simple model, based on a first order differential equation for the concentration gradient inside the pore, is thus compared to the original SEDE model in terms of accuracy and computational speed.

It exhibits an excellent agreement with the existing theory while reducing the computing speed by more than one order of magnitude. Moreover the resource needed by this new model hardly depends on the complexity of the system. It is likely to be useful for those looking for a fast and accurate tool when trying to predict the performance of a membrane. It is moreover

easy to implement while giving a good grasp on the role of each phenomenon at stake in the nanofiltration process, as it provides an insightful expression for the rejection rate.

Ultimately this model is confronted with experimental data taken from the literature [63]. Using three different approaches we show how this model is able to predict accurately the separation of polyvalent and monovalent anions using a coherent framework that notably dispenses with the useless fitting on the thickness to porosity ratio present in the original DSPM model. The influence of Born and image effect are also discussed. While taking image forces into account results into a more stable fitting for the dielectric constant inside the pore, the lack of scientific knowledge and data on the matter doesn't allow us to draw a definitive conclusion on which approach is more representative of the reality.

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Notations

 A_k = membrane porosity

 $c_i(0^-)$ = charge of the ion *i* on the permeate side (mmol.L⁻¹)

 $\overline{c_l}(z)$ = concentration profile along the pore (mmol.L⁻¹)

 $c_i(\Delta z^+)$ = charge of the ion *i* on the retentate side (mmol.L⁻¹)

 C_f = feed concentration (mmol.L⁻¹)

 d_h = hydraulic diameter (m)

 $D_{i,\infty}$ = bulk diffusion coefficient for the ion i (m².s⁻¹)

q = elementary charge (C°)

E(z) = electric potential inside the pore (V.m⁻¹)

F = Faraday constant (C.mol⁻¹)

 j_i = molar flux density of ion i (mol.m⁻².s⁻¹)

 J_v = permeate volumetric flux (m.s⁻¹)

 k_B = Boltzmann constant (J.K⁻¹)

 k_m = mass transfer coefficient

 $K_{i,c}$ = convection hindrance factor for the ion i

 $K_{i,d}$ = diffusion hindrance factor for the ion i

 L_p = pure water permeability

 Pe_i = Peclet number for the ion i

 $r_{i,cav}$ = cavity radius of ion i (m)

 $R = \text{universal gas constant } (J.K^{-1}.\text{mol}^{-1})$

Re = Reynolds number

 R_{app} = apparent rejection

 R_i = intrinsic rejection

Sc = Schmidt number

 S_v = least square objective function

T = temperature(K)

X(z) = charge distribution along the pore (mmol.L⁻¹)

 X_{avg} = average charge along the pore (mmol.L⁻¹)

z =axial position along the pore (m)

 z_A = thickness over porosity ratio (m)

 z_i = charge of the ion i

Greek letters

 α = ratio between chloride concentration and sulfate concentration

 α_i = ratio between the Bjerrum length and the pore size

 γ_i = activity coefficient for the ion i

 η = dynamic viscosity of water

 $\Lambda_{i,(0^-|0^+)}$ = Partition coefficient at the pore inlet for the ion i

 $\Lambda_{i,(\Delta z^{-}|\Delta z^{+})}$ = Partition coefficient at the pore outlet for the ion i

 ΔP = applied pressure gradient (Pa)

 $\Delta W'_{i,Born}$ = Born solvation energy barrier for the ion i (scaled on $k_B T$)

 $\Delta W'_{i,lm(0^-|0^+)}$ = Solvation energy barrier due to image forces for the ion *i* at the pore inlet (scaled on k_BT)

 $\Delta W'_{i,Im(\Delta z^-|\Delta z^+)}$ = Solvation energy barrier due to image forces for the ion i at the pore outlet (scaled on k_BT)

 Δz = pore length (m)

 $\Delta \pi$ = osmotic pressure difference (Pa)

 $\Delta \bar{\psi}$ = potential variation inside the pore (V)

 $\Delta \psi_{D,(\Delta z^-|\Delta z^+)}$ = normalised Donnan potential at the pore outlet

 $\Delta \psi_{D,(0^+|0^-)}$ = normalised Donnan potential at the pore outlet

 $\Delta \overline{\psi_N}$ = normalised average potential variation inside the pore

 ε_0 = vacuum permittivity (J⁻¹.C².m⁻¹)

 ε_h = dielectric constant of the bulk

 ε_m = dielectric constant of the membrane matrix

 ε_n = dielectric constant inside the pore

 μ = effective reciprocal dimensionless screening length

 ϕ_i = steric partition coefficient

 $\bar{\psi}(z)$ = electric potential along the pore (V)

Appendix A: Derivation of the transmission equation

Let us remind the differential equation describing the evolution of concentration inside the pore:

$$\frac{d\overline{c_i}(z)}{dz} = \left(\frac{Pe_i}{\Delta z} - z_i \frac{\Delta \overline{\psi_N}}{\Delta z}\right) \overline{c_i}(z) - \frac{1}{K_{i,c}} \frac{Pe_i}{\Delta z} c_i(\Delta z^+)$$
(A.1)

At z = 0 inside the membrane, $\overline{c_i}(z) = \overline{c_i}(0^+)$. Solving the equation (A.1) considering this boundary condition gives:

$$\overline{c}_{l}(z) = \overline{c}_{l}(0^{+})e^{\left(\frac{Pe_{i}}{\Delta z} - z_{i}\frac{\Delta\overline{\psi_{N}}}{\Delta z}\right)z} - \frac{Pe_{i}}{K_{l,c}(Pe_{i} - z_{i}\Delta\overline{\psi_{N}})}c_{i}(\Delta z^{+})\left(e^{\left(\frac{Pe_{i}}{\Delta z} - z_{i}\frac{\Delta\overline{\psi_{N}}}{\Delta z}\right)z} - 1\right)$$
(A.2)

At $z = \Delta z$, the concentration inside the pore is $\overline{c_l}(\Delta z^-)$:

$$\overline{c}_{i}(\Delta z^{-}) = \overline{c}_{i}(0^{+})e^{\left(Pe_{i}-z_{i}\Delta\overline{\psi_{N}}\right)} - \frac{Pe_{i}}{K_{i,c}(Pe_{i}-z_{i}\Delta\overline{\psi_{N}})}c_{i}(\Delta z^{+})\left(e^{\left(Pe_{i}-z_{i}\Delta\overline{\psi_{N}}\right)}-1\right) \tag{A.3}$$

Considering the partition equations (7.1) and (7.2), we can express equation (A.3) usig only permeate and retentate concentrations:

$$c_i(\Delta z^+)\Lambda_{i,(\Delta z^-|\Delta z^+)} = c_i(0^-)\Lambda_{i,(0^-|0^+)}e^{\left(Pe_i-z_i\Delta\overline{\psi_N}\right)} - \frac{Pe_ic_i(\Delta z^+)}{K_{i,c}(Pe_i-z_i\Delta\overline{\psi_N})}\left(e^{\left(Pe_i-z_i\Delta\overline{\psi_N}\right)}-1\right) \tag{A.4}$$

Finally, algebraic manipulation of equation (A.4) yields:

$$\frac{c_i(\Delta z^+)}{c_i(0^-)} = \frac{\Lambda_{i,(0^-|0^+)} K_{i,c} (Pe_i - z_i \Delta \overline{\psi_N}) e^{(Pe_i - z_i \Delta \overline{\psi_N})}}{\Lambda_{i,(\Delta z^-|\Delta z^+)} K_{i,c} (Pe_i - z_i \Delta \overline{\psi_N}) - Pe_i (1 - e^{(Pe_i - z_i \Delta \overline{\psi_N})})}$$
(A.5)

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Highlights

- -We show that the evolution of the transmembrane potential with the concentration
- -Using pore averaged potential gradient, the SEDE model is simplified
- -Good agreement is obtained between the simplified and the original model
- -Computation time is greatly reduced

-Good agreement with experimental data for moderate to high concentrations