# Chiroptical properties of carbo[6]helicene derivatives bearing extended $\pi$ conjugated cyano substituents 

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#### Abstract

New carbo[6]helicene derivatives grafted with $\pi$-conjugated cyano-phenyl arms have been synthesized in enantiopure forms and their $\pi$-conjugation examined by UV-vis spectroscopy. The influence of the $\pi$-conjugation on the circular dichroism spectra and molar rotations is discussed based on comparing experimental data with results from quantum chemical calculations. The results highlight the fact that increasing the $\pi$-system in a helicene molecule is an efficient way of increasing its molar rotation.


## INTRODUCTION

Helicenes are ortho-fused nonplanar polyaromatic molecules with a unique helical shape combined with $\pi$-conjugation providing them with huge chiroptical properties (circular dichroism and optical rotation). ${ }^{1-5}$ The development of chiral molecules revealing high chiroptical properties may lead to novel multifunctional molecular materials displaying chirality combined with other properties (circularly
polarized luminescence (CPL), optical or redox switching, gels or fibers formation, chiral recognition, etc...). ${ }^{6}$ Helicene-based molecules may find applications in such domains, and attention has been recently paid on their properties. ${ }^{7}$ Since the first synthesis and optical resolution of carbo[6]helicene in the mid$50 \mathrm{~s},{ }^{8}$ a number of helicene homologues have been prepared using different synthetic methods. ${ }^{1-6,9,10}$ Among the various strategies available, an effective general method to obtain enantiopure helicenes involves $i$ ) the photocyclization of stilbenic systems to produce racemic helicenes, ${ }^{11,12}$ and $\left.i i\right)$ the enantiomeric resolution of racemic helicene samples by preparative HPLC with appropriate chiral stationary phases. ${ }^{13}$ Consequently, this enables to record experimental circular dichroism (CD) spectra and molar rotation values (MR) of enantiomeric helicenes and to compare them to the calculated ones, in order to get more insight into the different factors influencing these chiroptical properties. The impact on the CD spectra and MR values, of such factors as the helical pitch, the number of aromatic rings, the incorporation of heteroatoms or metallic ions, the substitution with conjugated groups, the positive or negative induction effect, the assembly of two helicenes, has been experimentally and theoretically studied. ${ }^{14-24}$

We have recently demonstrated that the chiroptical properties of helicenes can be engineered by introducing lateral organometallic substituents. ${ }^{25}$ This result has highlighted the very important role of substituents grafted on the helicene core but incorporated in the $\pi$-system in determining its chiroptical properties. In this paper, we show that simple organic lateral vinyl or ethynyl $\pi$-substituents can greatly modify the chiroptical properties. We describe the synthesis and the enantiomeric resolution of novel carbo[6]helicene derivatives H2-H4 (Fig. 1) bearing $\pi$-conjugated cyano substituents and examine their chiroptical properties by comparing experimental data with results mainly from density functional theory (DFT) and time-dependent DFT (TDDFT) calculations of structural parameters, optical rotations, and CD spectra.

## RESULTS AND DISCUSSION



P/M-H2



Fig. 1. Carbo[6]helicene derivatives H1-H4

## A. EXPERIMENTAL RESULTS

## A.1. Synthesis and resolution of helicene derivatives

Racemic $\mathbf{H} \mathbf{2}$ was prepared from racemic 2-ethynyl-[6]carbohelicene $\mathbf{H} \mathbf{1}^{25}$ and the commercially available 4-bromobenzonitrile with $70 \%$ yield using classical Sonogashira coupling conditions (Scheme 1). Single crystals of racemic $\mathbf{H 2}$ were grown by slow diffusion of pentane vapors into a $\mathrm{CH}_{2} \mathrm{Cl}_{2}$ solution and the Xray crystallographic structure is depicted on Fig. 2 ( $\mathrm{P} 21 / \mathrm{n}$ space group). The overlapping of the terminal phenyl rings of the helicene moiety is clearly seen, with a helicity (dihedral angle between the terminal rings) of $48.5^{\circ}$, a classic value for a carbo[6]helicene derivative. Moreover, the coplanarity of the 4-cyano-phenyl-ethynyl moiety with the connected terminal phenyl ring of the helicene moiety is illustrated by the angle values of 173.6 and $177.4^{\circ}$ for respectively $\mathrm{C} 2-\mathrm{Ca}-\mathrm{Cb}$ and $\mathrm{Ca}-\mathrm{Cb}-\mathrm{Cc}$ and a dihedral angle of $15.2^{\circ}$ between the benzonitrile and the phenylethynyl rings. This coplanarity ensures an efficient electronic coupling between the helicene core and the $\pi$-ligand and highlights the fact that $\mathbf{H 2}$ is actually an extended $\pi$-conjugated helicene derivative. Enantiopure $P$ - and $M$ - H3 were finally obtained by HPLC over Chiralpak IA (hexane/ethanol/chloroform (90/5/5) as the mobile phase). The experimental details are given in the SI part.


Scheme 1. Synthesis of enantiopure $P$ - and $M-\mathbf{H} 2$ from enantiopure $P$ - and $M-\mathbf{H} 1 .{ }^{25}{ }^{i}$ ) 4bromobenzonitrile, $\mathrm{PdCl}_{2}\left(\mathrm{PPh}_{3}\right)_{2}, \mathrm{CuI}, \mathrm{Et}_{3} \mathrm{~N}, \mathrm{Ar}, 50^{\circ} \mathrm{C}, 1$ night, $70 \%$. ii) HPLC separation over a chiral stationary phase (vide supra).



Fig. 2. X-ray crystallographic views of $\mathbf{H} \mathbf{2}$ and $\mathbf{H 4}$ (only the $P$ stereoisomers shown).
The synthesis of $P$ - and $M$ - enantiomers of 4-cyanophenyl-vinyl substituted carbo[6]helicene $\mathbf{H 3}$ was achieved according to Scheme 2. The first step was a classical Wittig reaction between the previously described benzo[c]phenanthrylphosphonium bromide $\mathbf{1},{ }^{26}$ and commercially available 4-cyanobenzaldehyde, the reaction leading to olefin 2 with $85 \%$ yield as a mixture of the two cis and trans isomers that do not need to be separated for the next photocyclization reaction, a common reaction in the helicene synthesis. ${ }^{11,12}$ Using classical photocyclization conditions (highly diluted toluene solutions in the presence of catalytic iodine and irradiation for one night using a 150 W Hg lamp), 2-cyanocarbo[6]helicene H5 was obtained with $45 \%$ yield after purification over column chromatography. The cyano group was then reduced to an aldehyde using DIBAL-H in toluene at $30^{\circ} \mathrm{C}$, giving
carbo[6]helicene-2-carbaldehyde $\mathbf{H 6}{ }^{28}$ with $85 \%$ yield. The final step was a Horner-Emmons reaction between the produced aldehyde $\mathbf{H 6}$ and an already prepared 4-cyanobenzylphosphonate ${ }^{27}$, yielding the desired product H3 as a 30:70 cis/trans isomeric mixture. HPLC separation over a Chiralpak IB column (hexane/EtOH 8:2 as the mobile phase, see SI) enabled to obtain the final enantiopure $P$ - and $M$ - $\mathbf{H 3}$ in their pure trans form (Fig. S1).


Scheme 2. Synthesis of enantiopure $P$ - and $M$-H3. $i$ ) 4-cyano-benzaldehyde, $n$-BuLi, THF, Ar, r.t., 3 hrs, $85 \%$; ii) hv, cat. $\mathrm{I}_{2}$, toluene, one night, $45 \%$; iii) DIBAL-H, toluene, Ar, r.t., 2 hrs , $80 \%$; iv) 4cyanobenzylphosphonate ${ }^{27}, \mathrm{NaH}, \mathrm{THF}, \mathrm{Ar}, 2 \mathrm{hrs}, 80 \% ; v$ ) HPLC separation over a chiral stationary phase (vide supra).

The synthesis of $P$ - and $M$ - enantiomers of carbo[6]helicene $\mathbf{H 4}$ substituted with a long $\pi$-conjugated arm was achieved according to Scheme 3. Racemic aldehyde H7 was first prepared by a Sonogashira coupling between racemic H1 and 4-iodobenzaldehyde with $92 \%$ yield. Then racemic H4 was obtained by a Horner-Emmons reaction using 4-cyanobenzylphosphonate with $82 \%$ yield. Single crystals of racemic H 4 were grown by slow diffusion of pentane vapors into a $\mathrm{CH}_{2} \mathrm{Cl}_{2}$ solution and the X -ray crystallographic structure is depicted on Fig. 2. The structure was solved in the P-1 space group. The two phenyl rings of the stilbenyl moiety are almost coplanar with a dihedral angle of 6.5-7.6 ${ }^{\circ}$ between them. Moreover, the dihedral angle between the stilbenyl and the linked phenyl of the helicene core is between
28.8-30.6, values that still ensure efficient electronic coupling between the helicene core and the $\pi$-ligand. The carbo[6]helicene core displays a helicity (dihedral angle between the terminal rings) value of 49.6$50.4^{\circ}$, which shows that the pendant $\pi$-system does not destabilize the helicene part. Here again, H4 corresponds to an extended $\pi$-conjugated helical molecule. Finally, pure $P$ - and $M$ - H 4 enantiomers in their pure trans isomeric form were separated by HPLC over Chiralpak IC (Hexane/2-PrOH/chloroform (75/5/20) as the mobile phase, see SI).
H1



Scheme 3. Synthesis of enantiopure $P$ - and $M$-H4. i) 4-iodobenzaldehyde, $\mathrm{PdCl}_{2}\left(\mathrm{PPh}_{3}\right)_{2}, \mathrm{CuI}, \mathrm{Et}_{3} \mathrm{~N}, \mathrm{Ar}$, $50^{\circ} \mathrm{C}, 1$ night, $92 \%$; ii) 4-cyanobenzylphosphonate, ${ }^{27} \mathrm{NaH}$, THF, Ar, 2 hrs, $82 \%$; iii) HPLC separation over a chiral stationary phase (vide supra).

## A.2. Experimental UV-Vis and chiroptical properties

In Fig. 3 are depicted the UV-vis spectra of helicene derivatives H1-H4. Ethynyl substituted $\mathbf{H 1}$ displays several absorption bands below 380 nm (320, 332 and 352 nm ) with moderate absorption coefficients (13000-26000 $\mathrm{M}^{-1} \mathrm{~cm}^{-1}$ ). They are accompanied with two small bands at 390 and 410 nm . Compound 4-cyano-phenyl-vinyl substituted carbo[6]helicene H3 displays broad absorption bands tailing down to 430 nm and more intense than in $\mathbf{H} \mathbf{1}$ above 350 nm . Going from 4-cyano-phenyl-vinyl compound $\mathbf{H 3}$ to 4 -cyano-phenyl-ethynyl substituted H2, the absorption bands become much more intense (absorption coefficients up to twice as high as for H3) with several bands at $306,329,355,395$ and 417 nm , tailing down to $430-450 \mathrm{~nm}$. In other words, phenyl-ethynyl substituted helicene $\mathbf{H} \mathbf{2}$ is more conjugated than phenyl-vinyl substituted helicene $\mathbf{H 3}$, itself more conjugated than ethynyl-helicene $\mathbf{H 1}$, and increasing charge transfer is observed within the series $\mathbf{H 1} \rightarrow \mathbf{H} \mathbf{3} \rightarrow \mathbf{H} \mathbf{2}$ (see also the discussion of the calculated CD spectra below). Finally, helicene H4 substituted with 4-cyano-phenyl-vinyl-phenyl-ethynyle long arm displays an even more intense spectrum tailing down to $\sim 450 \mathrm{~nm}$, with bands at $334,350,359,376,400$ and 417 nm , of intensities within the range $3700-50000 \mathrm{M}^{-1} \mathrm{~cm}^{-1}$. The UV-vis spectra therefore illustrate how the electronic properties of a carbo[6]helicene can be molecularly engineered by simply grafting a $\pi$ conjugated arm of different vinyl or ethynyl substituents and of different lengths. This simple method does therefore directly influence the chiroptical properties of helicenic systems.


Fig. 3. UV-vis spectra of carbo[6]helicene derivatives H1-H4.

Fig. 4 displays the CD spectra of $\mathbf{H 1} \mathbf{- H 4}$. The $P$ and $M$ enantiomers reveal the expected mirror-image relationship. The experimental CD of $P-\mathbf{H 1}$ and $P-\mathbf{H} 3$ shows two intense CD bands at 250 nm (negative, ${ }^{1} \mathrm{~B}_{\mathrm{a}}$ transition according to the Platt nomenclature ${ }^{29}$ ) and around 335 nm (positive, ${ }^{1} \mathrm{~B}_{\mathrm{b}}$ transition) with a vibronic structure appearing. Note that the ${ }^{1} \mathrm{~L}_{\mathrm{b}}$ transition existing in helicene $C D$ spectra is usually of very low intensity and not always seen and can change sign. ${ }^{23,24}$ It is therefore difficult to identify. The CD shape of $\mathbf{H 1}, \mathbf{H} \mathbf{3}$ corresponds to the common fingerprint of $P$-helicene derivatives. In Fig. 6 the CD spectra of the four $P-\mathbf{H 1}-\mathrm{H} 4$ enantiomers are compared. As was already observed in UV-vis, the CD spectrum of $\mathbf{H 3}$ is overall of lower intensity than $\mathbf{H 1}$ with a slight bathochromic shift between 350-430 nm . The CD spectra of compounds $\mathbf{H 2}, \mathbf{H} 4$ are sensibly different from $\mathbf{H 1}, \mathbf{H 3}$ since they display two additional bands between 280 and 380 nm (negative, negative for $P-\mathbf{H} 2$ and positive, negative for $P-\mathbf{H 4}$ ) beside the common intense negative bands at 250 nm and intense structured positive bands that appear highly bathochromically shifted (at 356 and 362 nm respectively). Very interestingly, Fig. 5 reveals that the ${ }^{1} \mathrm{~B}_{\mathrm{a}}$ transitions are of similar intensity in the four helicene derivatives. In contrast, the bands corresponding to the ${ }^{1} \mathrm{~B}_{\mathrm{b}}$ transition significantly change upon functionalization. ${ }^{15,23,24,29}$


Fig. 4. CD spectra of enantiopure carbo[6]helicene derivatives H1-H4.


Fig. 5. CD spectra of H1-H4 $P$-enantiomers.

The specific and molar rotations values are summarized in Table 1 (vide infra). The molar rotations display increasing values within the series $\mathbf{H} \mathbf{3}<\mathbf{H} \mathbf{1}<\mathbf{H} \mathbf{2}<\mathbf{H} 4$. They are clearly affected by the $\pi$ conjugation of the whole derivatives while the helicity of the helicene core is maintained. These results highlight the fact that increasing the $\pi$-system in a helicene molecule is an efficient way of increasing its molar rotation.

## B. CALCULATIONS

## B.1. Computational details

For compatibility with our previous work on helicene derivatives ${ }^{18-22,25}$, DFT geometry optimizations were initially performed with the Turbomole program version 5.7.1 ${ }^{30,31}$, employing the $\mathrm{BP}^{32-34}$ exchangecorrelation functional and a split-valence basis set with one set of polarization functions for non-hydrogen atoms ( $\mathrm{SV}(\mathrm{P}))^{35-37}$. Computations with this functional and basis set combination are referred to as BP in the following. To provide further insight into the relationships between structure and chiroptical properties of the helicenes, subsequent geometry optimizations were performed with inclusion of dispersion (D) interactions. A subset of these calculations was carried out with the semi-empirical DFTD3 ${ }^{38}$ approach as implemented in the Amsterdam Density Functional (ADF) program version 2012.01 ${ }^{\text {39- }}$ ${ }^{41}$. The DFT-D3 calculations employed the BP functional and an all-electron double- $\xi$ (split valence) + polarization (DZP) Slater-type orbital basis for C and N along with a double- $\xi$ (DZ) basis for H atoms. This set of calculations is referred to as BP-D in the following. An old branch of the optimization code in ADF 2012 was used after we found that the default, more recent, implementation of the optimizer produced nonphysical structures in conjunction with the D3 correction. Dispersion forces arise from dynamic fluctuating interactions between distant electrons due to electron correlation. Another subset of calculations employed Hartree-Fock (HF) theory followed by a perturbational treatment of electron correlation at the second-order Møller-Plesset level (MP2). The MP2 calculations were performed with the Gaussian 09 program $^{42}$, utilizing the correlation-consistent polarized double- $\xi$ Dunning basis set cc$\mathrm{pVDZ}{ }^{43}$ for all the atoms. For brevity, we refer to these calculations as MP2 in the following without explicitly indicating the basis set.

Time-dependent DFT (TDDFT) linear response calculations of optical rotation (OR) and circular dichroism (CD) were performed with NWChem $6.1^{44,45}$ utilizing the optical activity module developed by one of the authors ${ }^{46}$. Optical rotation parameters were computed at the sodium $D$-line wavelength $\lambda=$ 589.3 nm . The simulated CD spectra are based on calculations of the 60 lowest singlet vertical excitations and the corresponding electric and magnetic electronic transition dipole moments. The spectra were Gaussian broadened with a root mean square width parameter of $\sigma=0.2 \mathrm{eV}$.

The list of systems that were studied computationally includes the four carbo[6]helicene cyano derivatives H1-H4 (Fig. 1) and, for comparison, the H5 compound along with pristine [6]helicene. The latter is labeled as $\mathbf{H 0}$ in order to indicate its role as the structural parent of $\mathbf{H 1}-\mathbf{H 5}$. For systems $\mathbf{H 3}$ and H4, both s-cis and s-trans isomers as shown in Fig. 6 were considered. All calculations were carried out for the $P-(+)$ isomers without imposing symmetry. The results for $\mathbf{H 5}$ were found to be very similar to those for H1, which is not surprising because the two systems are isoelectronic. Furthermore, no detailed
experimental data are available for H5. Accordingly, $\mathbf{H 5}$ is not discussed in detail. Results from a full set of calculations for $\mathbf{H 5}$ can be found in the SI (Figures S10-S13, Tables S5 and S6).

s-trans

s-cis

s-trans


Fig. 6. Molecular structures of carbo[6]helicene derivatives $\mathbf{H 3}$ and $\mathbf{H 4}$. Relative energies in $\mathrm{kcal} / \mathrm{mol}$ are listed for the optimized $\mathrm{BP} / \mathrm{SV}(\mathrm{P})$ (displayed), BP-D3/DZ(P), and MP2/cc-pVDZ geometries.

## B.2. Benchmarks

In order to determine a computationally efficient, yet reliable, protocol for a description of the chiroptical properties of the samples, test calculations were initially carried out based on the BP geometries. For an overview of various influences that generally affect the computation of optical activity see Ref. 47. The main points addressed by the present calculations are (i) a possible origin dependence of the OR due to basis set incompleteness, (ii) the size of the basis set needed in order to obtain reasonable results for the helicene systems, (iii) the influence of approximations in the density functionals.

Regarding point (i), the standard length (L) representation of the electric transition dipole yields origin dependent isotropic chiroptical properties in calculations with finite AO basis sets. Although the
problem is associated with a gauge freedom for the magnetic dipole operator ${ }^{48}$, the origin-dependence can be eliminated by adopting the velocity representation (V) of the electric dipole operator ${ }^{49}$. For OR, a modified velocity representation suggested in Ref. 50 was used. Alternatively, the origin-dependence is eliminated by adopting a distributed gauge origin for the magnetic vector potential, for instance by using a 'gauge-including' atomic orbital (GIAO) basis ${ }^{46,51,52}$. The three types of calculations (AO-L, AO-V, GIAO) become equivalent in the complete basis limit but they may generate very different results for finite basis sets. Since the AO-V and GIAO formalisms entail some additional computational cost, it was examined whether the computationally least demanding AO-L calculations are suitable for the helicene systems studied in this work (AO-V has additional overhead only for optical rotation, when using the 'modified' form). Regarding point (ii), it was examined whether diffuse basis functions are required for the present study. Results from computations with the aug-cc-pVDZ ${ }^{43,53}$ basis $v s$. $\mathrm{SV}(\mathrm{P})$ were compared. Regarding point (iii), the list of examined functionals included two global hybrids, B3LYP ${ }^{54-56}$ and BHLYP ${ }^{55,57}$, and a hybrid functional with range-separated exchange and correct asymptotic potential, LCPBE $0^{58-60}$ used in our previous benchmarks ${ }^{14,61}$.

In line with helicene data from our recent 45 -molecule OR benchmark (OR45 ${ }^{14}$ ), the ORs show excellent agreement between the AO-L, AO-V, and GIAO calculations (Table S3). The agreement with experiment becomes better as the fraction of HF exchange in the functional increases, going from B3LYP to BHLYP to LC-PBE0 (Table S4 and Figure S2). Further, a substantial reduction in the basis set size when going from aug-cc-pVDZ to $\mathrm{SV}(\mathrm{P})$, does not change the MR values much (Table S4). This finding is in line with the rather good performance of $\mathrm{SV}(\mathrm{P})$ in many other studies on helicenes and helicene derivatives ${ }^{18-22,25}$. The underlying reason is that the OR is strongly dominated by valence excitations of low energy that barely have any contributions from hydrogen-centered AOs (see Section B.4). The CD over the UV-vis spectral range is assigned entirely to such valence transitions. Hence, computations of the OR and of the CD spectra in the UV-vis spectral range without diffuse basis functions and without polarization functions for hydrogen atoms are suitable for the purpose of this work. Accordingly, all subsequent computations employed the LC-PBE0 functional and the $\mathrm{SV}(\mathrm{P})$ basis set with AO-L gauge, using center of nuclear charges coordinates.

## B.3. Geometry dependence of the optical rotations

Calculated molar rotations (MRs) [ $\phi]_{\mathrm{D}}$ for the helicene systems are listed in Table 1 along with available experimental data. Even though the LC-PBE0 functional gives ORs closer to experiment than the global hybrid functionals B3LYP and BHLYP (Table S4, Figure S2), except for $\mathbf{H 0}$ the calculations
substantially overestimate the MRs for the BP optimized geometries ( $\mathrm{X}=\mathrm{BP}$ ). Experimentally, only $\mathbf{H 4}$ has a significantly larger OR than H0. Instead, H1 and H2 have ORs similar to H0, and the OR of H3 is even lower. The overestimation of the calculated ORs with the BP geometries increases for systems with longer vinyl / ethynyl substituents, i.e. when going from $\mathbf{H 1}$ to $\mathbf{H 3}$ / H4. In fact, such a trend is expected. The $\pi$ orbitals of the substituted systems exhibit pronounced $\pi$-conjugation between the helicene and the substituents, meaning that the effective chromophore length increases (compare Fig. 11 vide infra). In agreement with previous studies of substituted helicenes ${ }^{14,18,19,61}$, the increased spatial extension of the helicene chromophore relative to $\mathbf{H 0}$ intensifies the CD and increases the magnitude of the OR even though the substituent is not chiral itself (other than through a chiral induction when it is bound to the helicene). There is also an important influence from charge-transfer (CT) in the substituted helicenes, as shown in Section B.4.

Table 1. Molar rotations ( $\mathrm{deg} \mathrm{cm}{ }^{2} \mathrm{dmol}^{-1}$ ) calculated for $\mathbf{H 0}$ to $\mathbf{H 4}$, and comparison with experiment. ${ }^{a}$ Experimental specific rotations $\left(\operatorname{deg} /\left[\mathrm{dm}\left(\mathrm{g} / \mathrm{cm}^{-3}\right)\right]\right)$.

| System |  | ${ }_{\text {d }}{ }^{\text {calc }}$ |  | $[\phi]_{\mathrm{D}} \mathrm{expt} b^{\text {b }}$ | $[\alpha]_{\mathrm{D}} \mathrm{expt}^{\text {b }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | LC-PBE0/SV(P)//X |  |  |  |  |
| $\mathrm{X}=$ | BP | BP-D | MP2 |  |  |
| H0 | 10448 | 9532.2 | 9583.6 | $11954{ }^{\text {c }}$ | $3640{ }^{\text {c }}$ |
| H1 | 13966 | 12050 | 12508 | 11030 | 3133 |
| H2 | 18833 | 14727 | 11727 | 11900 | 2623 |
| H3 s-cis | 21393 | 13886 | 14302 | --- ${ }^{d}$ | --- ${ }^{\text {d }}$ |
| H3 s-trans | 19640 | 14551 | 11877 | 10650 | 2350 |
| H4 s-cis | 20329 | 17958 | --- | --- ${ }^{d}$ | --- ${ }^{\text {d }}$ |
| H4 s-trans | 20476 | 15000 | --- ${ }^{\text {e }}$ | 15820 | 2846 |

[^0]In our recent studies ${ }^{14}$ a pronounced dependence of the optical rotations of pristine and substituted helicenes on their molecular structure was noted. It was found that inclusion of van der Waals (dispersive)
forces may play a crucial role in geometry optimizations to ensure an accurate description of ORs in such compounds especially for more complex systems with $\pi$-conjugated substituents. One may distinguish two types of effects on the geometry of our samples: first, dispersion decreases the pitch of the helicene moiety through attractive $\pi$-stacking-like interactions. This effect reduces the magnitude of the OR. For H0, the reduction is about $10 \%$, with very similar results from the optimizations with BP-D and MP2. For pristine [ $n$ ]helicenes with not too large $n$ and simple derivatives thereof, the reduction of the OR magnitude is within the accuracy limits of the TDDFT calculations. We have shown previously that the influence of the exact exchange in the range-separated functional, and the system-dependence of the range-separation parameter, may be of higher importance especially for systems with higher $n^{61}$. A second effect from the dispersion forces affects the substituted helicenes, by producing large reductions in the distances between the substituent and the terminal aryl ring at the opposite end of the helicene moiety. Structure overlays for two representative molecules are shown in Fig. 7. The impact of this structural change on the OR may take place, for instance, via coupling of excitations involving orbitals centered in the substituent and the helicene terminus, respectively. Potentially, breaking or reducing the $\pi$ conjugation between the helicene and the substituent due to a bending of the linker moiety, as seen for $\mathbf{H} \mathbf{2}$ in Fig. 7, may also have a strong effect. In the substituted helicenes, the helical pitch is reduced in optimizations with dispersion similar to what is found for $\mathbf{H 0}$. A comparison of X-ray crystal structures of $\mathbf{H 2}$ and H4 s-trans with BP, BP-D, and MP2 optimized geometries can be found in the SI (Figure S9). The effects of dispersion corrections on experimental structural parameters follow the general trends discussed in Ref. 61, in particular as far as the helical pitch is considered.

The ORs listed in Table 1 show a significantly improved agreement with experimental data when going from BP to BP-D and MP2 geometries. The dispersion effect on the geometries uniformly reduces the ORs, in some cases dramatically, meaning that the effects from the pitch reduction and from the reduced distance between ligand and helicene terminus add up. As a result, the ORs of H1 to H3 calculated with the MP2 optimized structures emerge as similar to that of $\mathbf{H 0}$; the effect from the increased effective chromophore length is counterbalanced by the dispersion corrections to the geometry. Visual inspection of the orbitals of $\mathbf{H 1}$ to $\mathbf{H 4}$ that yield dominant contributions to the CD spectrum (vide infra) indicate that the geometry changes due to dispersion interaction alter the extent of $\pi$-conjugation between the helicene moiety and the substituents only slightly. This assessment is further corroborated by the fact that the appearance of the CD spectra (Section B.4) is qualitatively similar for the structures with and without dispersion corrections. The spectra for the MP2 structures are, however, significantly less intense, which goes hand in hand with the reduction of the OR. We tentatively ascribe part of the large effects of the geometry changes on the ORs of $\mathbf{H 2}$ to $\mathbf{H 4}$ to excitonic coupling effects, similar to what has
been found previously for helicene-metal complexes ${ }^{18,19}$. Since the interaction is strongly distancedependent (as indicated by the comparison between BP and BP-D or MP2 structures), there are potentially significant vibrational corrections to the $\mathrm{OR}^{63}$ which may further improve the agreement with experiment and produce the correct trend among H1, H2 , and H3 .


BP/SV(P) vs. MP2/cc-pVDZ


BP-D3/DZ(P) vs. MP2/cc-pVDZ

H2




Fig. 7. Overlays of $\mathrm{BP} / \mathrm{SV}(\mathrm{P})$, BP-D3/DZ(P), and MP2/cc-pVDZ optimized structures of $\mathbf{H 0}$ and $\mathbf{H 2}$. See the SI for a complete set of overlay structures.

For the less complex systems $\mathbf{H 0}$ and $\mathbf{H 1}$, the BP-D and MP2 geometries are very similar. Consequently, very similar ORs are obtained. Likewise, for $\mathbf{H 3} \mathbf{s}$-cis, the geometries are quite similar, and so are the calculated ORs. H3 s-trans and H2 show important differences between the BP-D and MP2 geometries. In the MP2 geometries, the substituent is closer to the helicene terminus, which amplifies the reduction of the OR discussed in the previous paragraph. In both cases, the calculated ORs with the MP2 structures are much closer to experiment than those obtained with the BP-D geometries (which already give a strong reduction relative to BP). The calculations further predict significantly larger ORs for the scis isomers of $\mathbf{H 3}$ and $\mathbf{H 4}$ than for the s-trans isomers, which would be interesting to confirm experimentally. Unfortunately, we were not able to converge MP2 geometry optimizations for H4. Irrespective of whether internal or Cartesian coordinates were optimized, large oscillatory forces on the atoms in the alkynyl linker persisted through many optimization steps. We attempted optimizations with another code and using additional approximations but obtained clearly deficient structures. Due to the rather high computational demand of the MP2 optimizations for H4, the approach was eventually abandoned and we decided to proceed only with the BP-D geometries. Fortunately, the calculated ORs agree well with experiment, which suggests that the optimized structure is reasonable. We speculate that a
structural distortion, similar to what is seen for $\mathbf{H} \mathbf{2}$ when going from BP-D to MP2, would result in a too large energetic penalty from disrupting the pronounced $\pi$-conjugation between the helicene and the substituent which is visible, for instance, in the HOMO isosurfaces of $\mathbf{H 4}$ (vide infra).

## B.4. CD spectra

Fig. 8 displays comparisons of calculated and experimental spectra for each $\mathbf{H 1} \mathbf{- H 4}$ system separately. To facilitate the interpretation of the theoretical results, Figures 9 and 10 compare the TDDFT UV-vis and CD spectra, respectively, for all systems in the same plot. A color scheme corresponding to the experimental data shown in Figures 3-5 is used here. Selected labeled excitations in the low-energy regions of the CD spectra (Fig. 10) have been characterized in detail. A list of pairs of occupiedunoccupied MOs that contribute with $10 \%$ weight or more to the transition density matrix of a selected excitation is provided in Table 2. The electric and magnetic transition dipoles are calculated from the transition density matrix, and therefore a large weight of a given pair of occupied and unoccupied MOs is indicative of their contributions to the intensity and provides an assignment of the excitation. Selected MOs are visualized in Fig. 11 (HOMOs and LUMOs) and Figures S4-S8.

Overall, the CD spectra agree well with experiment. The applied computational protocol typically does not yield intensities better than within a factor of 2 from experiment, and therefore the correct intensity ordering between $\mathbf{H} \mathbf{2}$ and $\mathbf{H} \mathbf{3}$ would be difficult to reproduce quantitatively. The main spectral features, and most importantly the sign patterns of the CD bands, are reproduced. The simulated spectra are based on Gaussian-broadened vertical excitations, and therefore they do not incorporate information on the vibronic structure of each CD band. As pointed out in the previous subsection, the spectra calculated with the MP2 geometries have lower intensity (in particular for $\mathbf{H} 2$ and $\mathbf{H 3}$ ), which goes along with the significantly reduced ORs for these systems compared to the structures optimized without dispersion corrections.

H4 affords an intense positive CD band (from excitation no. 1) at particularly low energy, which is clearly a strong contributor to the large positive OR of this system. The MO analysis identifies this excitation as predominantly HOMO to LUMO. The relevant orbitals (Fig. 11) indicate that this transition affords $\pi$ to $\pi^{*}$ transition character in the substituent, as well as a pronounced degree of charge-transfer (helicene to substituent, and intra-substituent). The presence of CT character helps rationalizing the strong absorption intensity and low energy of the excitation. The enhancement of CT transition character due to the helicene $\pi$-electron system is nicely illustrated by a comparison of UV-vis spectra calculated for $\mathbf{H 4}$ with two model systems - the pristine substituent HCCPhCHCHPhCN (1) and its phenyl

PhCCPhCHCHPhCN (2) derivatives (compare SI, Figures S14 and S15). Other notable excitations with strong CD are excitations no. 3 of $\mathbf{H 0}$ and $\mathbf{H 1}$. The strong CD intensities results from the involvement of orbitals that extend over the full length of the helical chromophore (unlike excitation no. 1 in $\mathbf{H 4}$ where only a small part of the helicene moiety is involved). Excitations no. 2 of $\mathbf{H 2}$ and $\mathbf{H 3}$, with strong positive rotatory strengths and at lower energy than the intense transitions of $\mathbf{H 0}$ and $\mathbf{H 1}$, are predominantly HOMO to LUMO and represent somewhat of a midpoint between $\mathbf{H 0 / H 1}$ on the one hand and $\mathbf{H 4}$ on the other: the excitations have helicene $\pi$ to $\pi^{*}$ character but only involve part of the helicene (reducing the CD intensity relative to the intense low-energy transitions in $\mathbf{H 0}$ and $\mathbf{H 1}$ ), along with some clear helicene to ligand CT which is accompanied by an energy-lowering and a significant increase of the electric transition dipoles (boosting the intensities in the UV-Vis the absorption spectra). For H4, the electric transition dipole moment of excitation no. 1 is exceptionally strong due to the particularly pronounced CT character, as evident from the intense absorption spectrum in Fig. 9, while simultaneously involving part of the helicene chromophore. As a result, its rotatory strength is larger than those of excitations no. 2 of H2 and H3. In summary, the spectra afford very clear systematic trends related to the presence and nature of the substituents, the extent of $\pi$-conjugation between the helicene moiety and the substituents, and the possibility of low-energy CT excitations that partially involve the helicene chromophore.

## CONCLUSION

This case study of carbo[6]helicenes bearing extended $\pi$-conjugated cyano substituents nicely illustrates how the electronic and optical properties of an [6]helicene can be molecularly engineered by simply grafting a $\pi$-conjugated arm of different vinyl or ethynyl substituents and of different lengths therefore enabling to modify the chiroptical properties of helicenic systems. In the future, the ability of these phenyl-ethynyl and/or vinyl substituted carbo[6]helicenes bearing cyano groups to be used as ligands ${ }^{27,64-}$ ${ }^{67}$ for helicene-based coordination chemistry will be investigated.

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Fig. 8. Comparison of experimental and TDDFT LC-PBE0/SV(P) CD spectra of H1-H4 $P$-(+)-enantiomers in their BP/SV(P) (BP), BP-D3/DZ(P) (BP-D), and MP2/cc-pVDZ (MP2) geometries. No spectral shift has been applied.


Fig. 9. Comparison of TDDFT LC-PBE0/SV(P) UV-vis spectra of $P-\mathbf{H 0}$ (black line), $P$-H1 (red), $P-\mathbf{H} \mathbf{2}$ (green), $P$ H3 s-trans (blue), and $P$-H4 s-trans (purple). MP2/cc-pVDZ / BP-D3/DZ(P) geometries used for H1-H3 / H4. No spectral shift has been applied.


Fig. 10. Comparison of TDDFT LC-PBE0/SV(P) CD spectra of $P-\mathbf{H 0}$ (black line), $P$ - $\mathbf{H} \mathbf{1}$ (red line), $P-\mathbf{H} \mathbf{2}$ (green), $P$-H3 s-trans (blue), and $P$-H4 s-trans (purple). See also caption of Fig. 9. Numbered excitations correspond to those analyzed in Table 2.

Table 2. Dominant occupied (occ) - unoccupied (unocc) MO pair contributions (greater than 10\%) of selected transitions of $\mathbf{H 0} \mathbf{- H 4}$, excitation energies $E$ and rotatory strengths $R$. TDDFT LC-PBE0/SV(P) calculations for MP2/cc-pVDZ (H0-H3) and BP-D3/DZ(P) (H4) geometries.

| Excitation | $E / \mathrm{eV}$ | $R / 10^{-40} \mathrm{cgs}$ | occ no. | unocc. no | \% |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $P-\mathrm{HO}$ |  |  |  |  |  |
| \#3 | 4.22 | 808.30 | 86 | 88 | 48 |
|  |  |  | 85 | 87 | 36 |
| P-H1 |  |  |  |  |  |
| \#2 | 3.91 | 53.69 | 91 | 93 | 64 |
|  |  |  | 92 | 94 | 24 |
| \#3 | 4.12 | 907.08 | 91 | 94 | 37 |
|  |  |  | 92 | 93 | 27 |


|  |  |  | 92 | 94 | 15 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| P-H2 |  |  |  |  |  |
| \#1 | 3.61 | 38.34 | 118 | 120 | 30 |
|  |  |  | 117 | 121 | 17 |
|  |  |  | 118 | 119 | 14 |
| \#2 | 3.74 | 470.89 | 118 | 119 | 52 |
|  |  |  | 117 | 119 | 17 |
|  |  |  | 117 | 121 | 10 |
| \#3 | 3.94 | 220.67 | 117 | 120 | 58 |
|  |  |  | 118 | 121 | 11 |
| \#5 | 4.28 | $-282.53$ | 116 | 119 | 20 |
|  |  |  | 117 | 121 | 19 |
|  |  |  | 118 | 120 | 13 |
|  |  |  | 117 | 119 | 10 |
| P-H3 s-trans |  |  |  |  |  |
| \#2 | 3.77 | 454.33 | 119 | 120 | 67 |
| \#3 | 3.95 | 267.99 | 118 | 121 | 63 |
| \#5 | 4.29 | -321.68 | 118 | 120 | 16 |
|  |  |  | 117 | 120 | 15 |
|  |  |  | 118 | 122 | 14 |
|  |  |  | 117 | 121 | 12 |
|  |  |  | 119 | 121 | 11 |
| P-H4 s-trans |  |  |  |  |  |
| \#1 | 3.56 | 671.79 | 145 | 146 | 63 |
| \#3 | 3.95 | -65.09 | 144 | 147 | 41 |
| \#4 | 4.11 | -373.95 | 144 | 148 | 40 |
|  |  |  | 145 | 147 | 17 |
|  |  |  | 143 | 146 | 10 |
| \#6 | 4.49 | 203.70 | 142 | 147 | 27 |



H2


H3 s-trans


H4 s-trans


Fig. 11. HOMO and LUMO isosurfaces (0.04 au) of $\mathbf{H 0} \mathbf{- H 4}$. LC-PBE0/SV(P) calculations for MP2/cc-pVDZ (H0H3) and BP-D2/DZ(P) (H4) structures.

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[^0]:    ${ }^{a} \mathrm{X}$ indicates the theoretical level used for the geometry optimization. AO-L calculations. ${ }^{b}$ Measured in $\mathrm{CH}_{2} \mathrm{Cl}_{2}$. Concentrations: $0.03 \mathrm{~g} / 100 \mathrm{~mL}$. Error of $5-10 \%$. ${ }^{c}$ From Ref. 62 . Recently, a value of 12348 was reported in Ref. 24. ${ }^{d}$ No experimental data available. ${ }^{e}$ MP2 optimizations did not converge.

